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REGRESSIONS

Regression

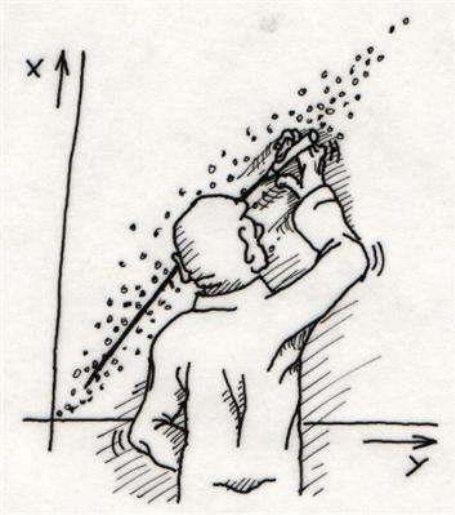
- Statistical processes for estimating the relationships among variables.
- Dependent variable, outcome variable, target
- Independent variables, predictor, covariates, or features

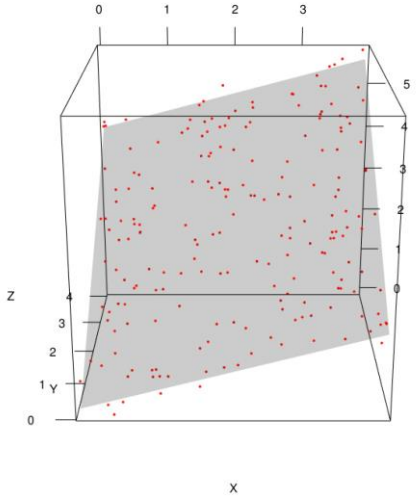
Regression

- simple regression/multivariate regression

$$Y_i = \beta_0 + \beta_1 X_i + e_i$$

$$Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + e_i.$$

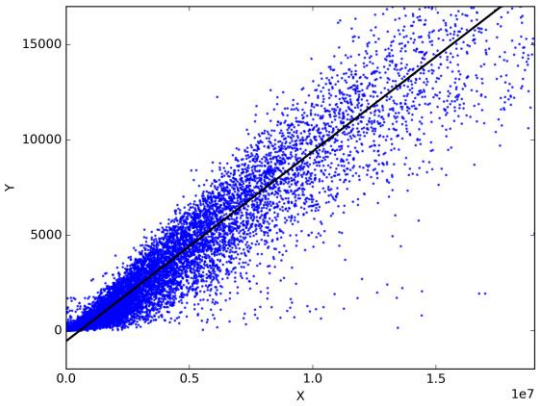




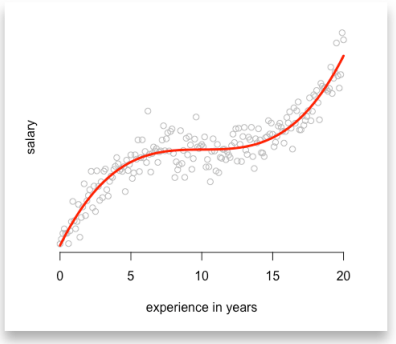
Regression

- .Linear/non linear

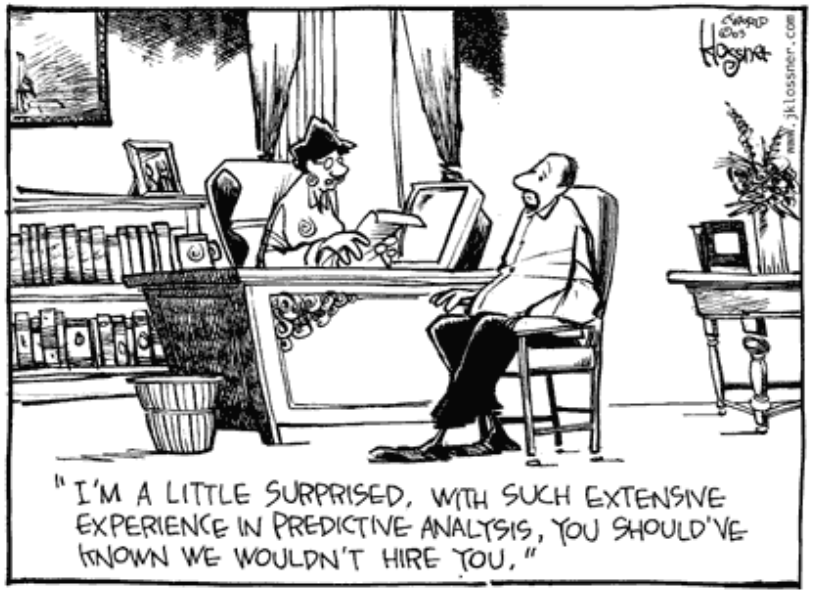
$$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i, \quad i = 1, \ldots, n.$$

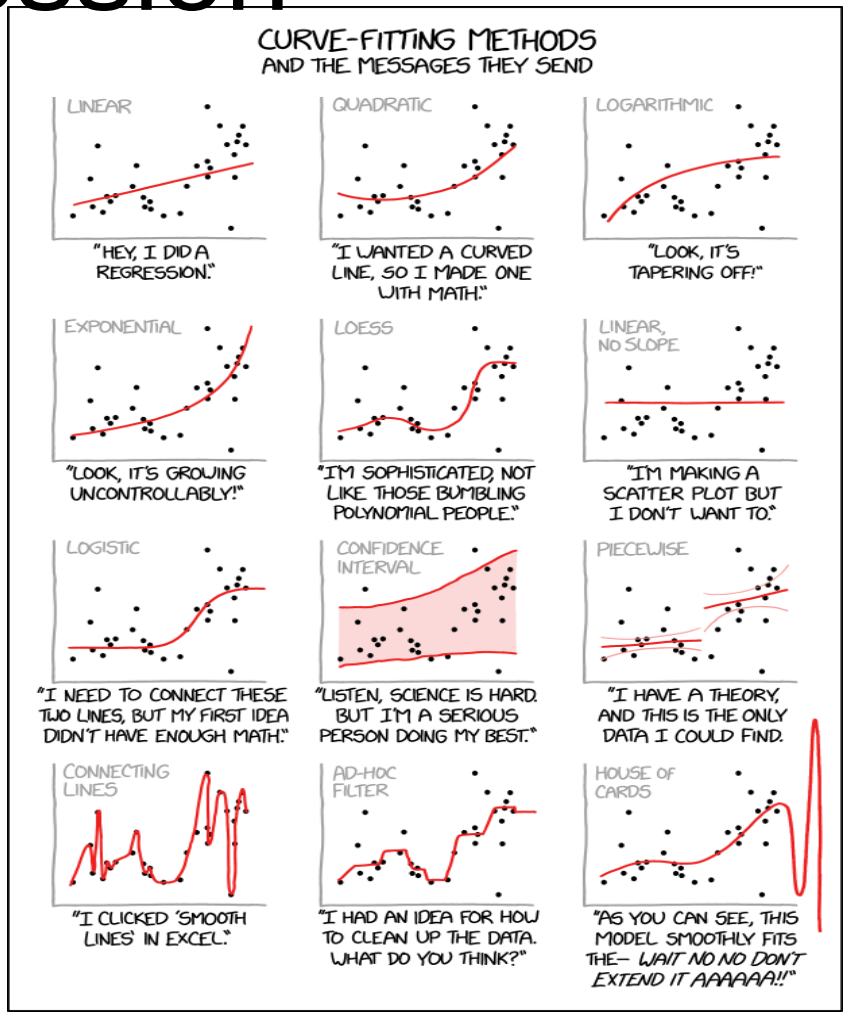


$$y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \varepsilon_i, \; i = 1, \ldots, n.$$



Regression


"I'M A LITTLE SURPRISED, WITH SUCH EXTENSIVE EXPERIENCE IN PREDICTIVE ANALYSIS, YOU SHOULD'VE KNOWN WE WOULDN'T HIRE YOU."


CURVE-FITTING METHODS
AND THE MESSAGES THEY SEND
LINEAR
"HEY, I DID A REGRESSION."
QUADRATIC
"I WANTED A CURVED LINE, SO I MADE ONE WITH MATH."
LOGARITHMIC
"LOOK, IT'S TAPERING OFF!"
EXPONENTIAL
"LOOK, IT'S GROWING UNCONTROLLABLY!"
LOESS
"I'M SOPHISTICATED, NOT LIKE THOSE BUMBLING POLYNOMIAL PEOPLE."
LINEAR, NO SLOPE
"I'M MAKING A SCATTER PLOT BUT I DON'T WANT TO."
LOGISTIC
"I NEED TO CONNECT THESE TWO LINES, BUT MY FIRST IDEA DIDN'T HAVE ENOUGH MATH."
CONFIDENCE INTERVAL
"LISTEN, SCIENCE IS HARD. BUT I'M A SERIOUS PERSON DOING MY BEST."
PIECEWISE
"I HAVE A THEORY, AND THIS IS THE ONLY DATA I COULD FIND.
CONNECTING LINES
"I CLICKED 'SMOOTH LINES' IN EXCEL."
AD-HOC FILTER
"I HAD AN IDEA FOR HOW TO CLEAN UP THE DATA. WHAT DO YOU THINK?"
HOUSE OF CARDS
"AS YOU CAN SEE, THIS MODEL SMOOTHLY FITS THE— WAIT NO NO DON'T EXTEND IT AAAAAA!!"

Regression

- OLS

$$\sum_{i=1}^{M} (y_i - \hat{y}_i)^2 = \sum_{i=1}^{M} \left(y_i - \sum_{j=0}^{p} w_j \times x_{ij} \right)^2$$

- Ridge

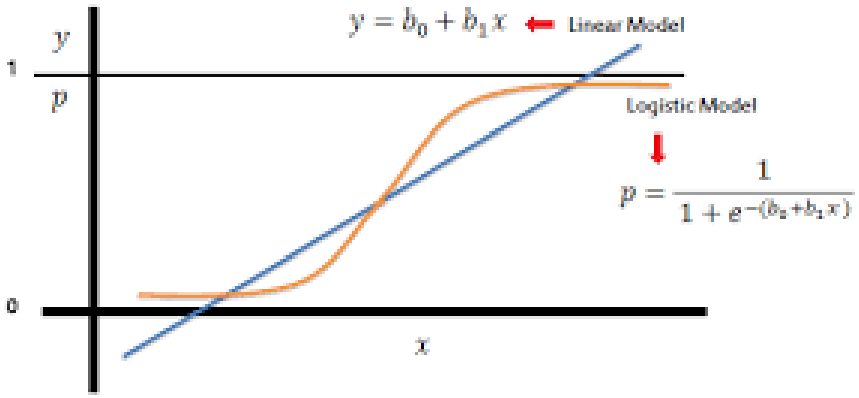
$$\sum_{i=1}^{M} (y_i - \hat{y}_i)^2 = \sum_{i=1}^{M} \left(y_i - \sum_{j=0}^{p} w_j \times x_{ij} \right)^2 + \lambda \sum_{j=0}^{p} w_j^2$$

- Lasso

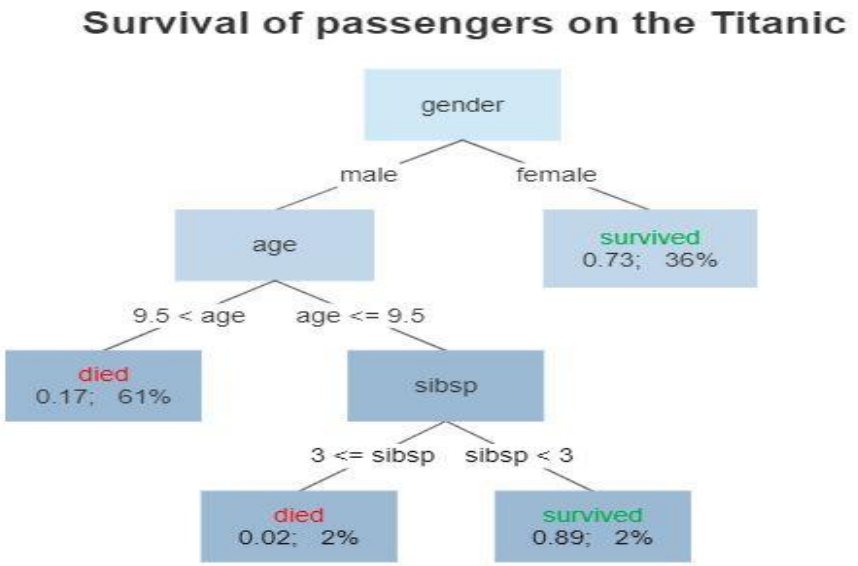
$$\sum_{i=1}^{M} (y_i - \hat{y}_i)^2 = \sum_{i=1}^{M} \left(y_i - \sum_{j=0}^{p} w_j \times x_{ij} \right)^2 + \lambda \sum_{j=0}^{p} |w_j|$$

Logistics Regression

- Logistic regression is a statistical model that in its basic form uses a logistic function to model a binary dependent variable, although many more complex extensions exist



Decision Tree

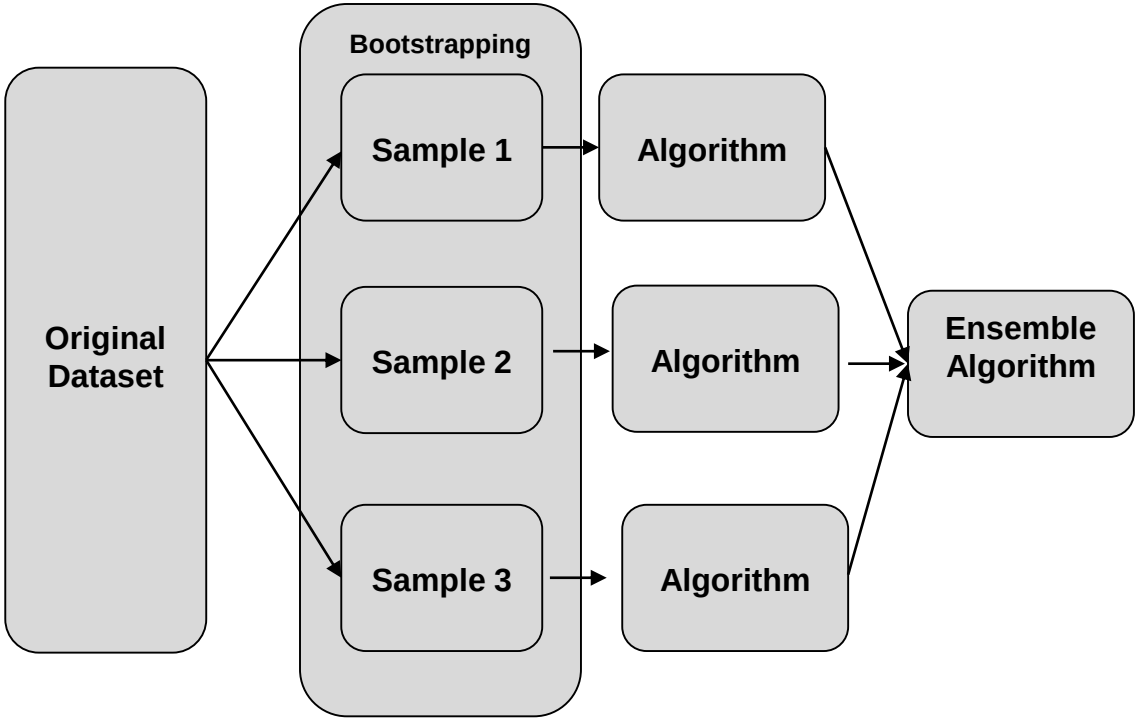


- Classification or Regression
- breaks down a data set into smaller and smaller subsets
- final result is a tree with decision nodes and leaf nodes.

Ensemble

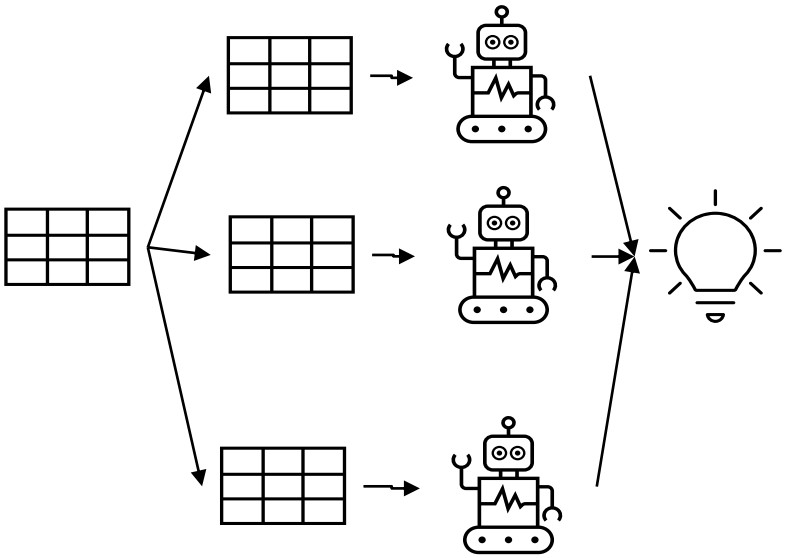
- Ensemble is a Machine Learning concept in which the idea is to train multiple models using the same learning algorithm.
- classification, regression and other tasks
- multitude of decision trees at training time
- outputting the class that is the mode of the classes (classification) or mean prediction (regression) of the individual trees

Ensemble

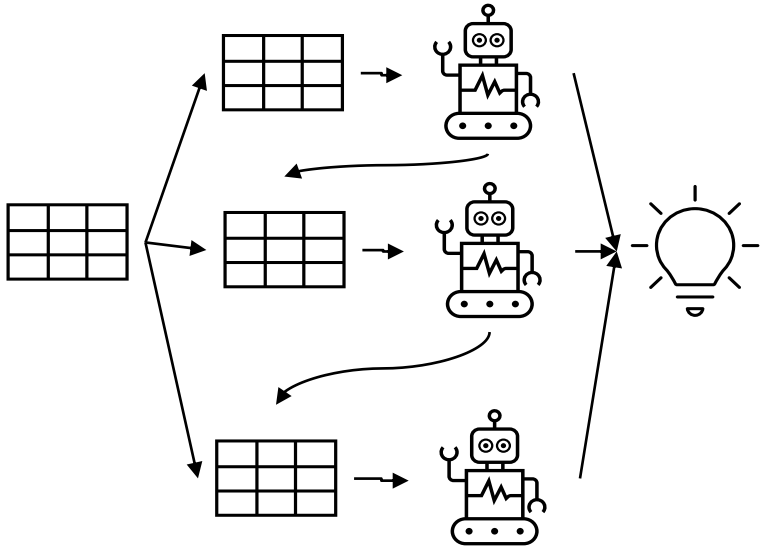

Bootstrapping
Original Dataset
Sample 1
Sample 2
Sample 3
Algorithm
Algorithm
Algorithm
Ensemble Algorithm

Bagging vs. Boosting

Bagging



Boosting



Bagging vs. Boosting

- classification, regression and other tasks
- multitude of decision trees at training time
- outputting the class that is the mode of the classes (classification) or mean prediction (regression) of the individual trees.

Bagging

- **create multiple bootstrap samples**
- **fit a weak learner**
- **aggregate** -> “average” their
- outputs is an ensemble model with less variance that its components..

$$s_L(.) = \frac{1}{L}\sum_{l=1}^{L} w_l(.) \qquad \text{(simple average, for regression problem)}$$

$$s_L(.) = \arg\max_k [card(l|w_l(.) = k)] \qquad \text{(simple majority vote, for classification problem)}$$

Boosting

- in fitting sequentially multiple weak learners in a very adaptative way
- each new model focus its efforts on the most difficult observations to fit up to now
- at the end of the process, is obtained a strong learner with lower bias
- Boosting can also have the effect of reducing variance

$$(c_l, w_l(.)) = \underset{c,w(.)}{\arg\min} E(s_{l-1}(.) + c \times w(.)) = \underset{c,w(.)}{\arg\min} \sum_{n=1}^{N} e(y_n, s_{l-1}(x_n) + c \times w(x_n))$$

Random Forest

- is a bagging method where deep trees, fitted on bootstrap samples, are combined to produce an output with lower variance
- classification, regression and other tasks
- multitude of decision trees at training time
- outputting the class that is the mode of the classes (classification) or mean prediction (regression) of the individual trees.

Python Libraries