ESTATÍSTICA I



Licenciatura em Gestão do Desporto

2nd year/1st Semester 2025/2026

CONTACT

Professor: Elisabete Fernandes

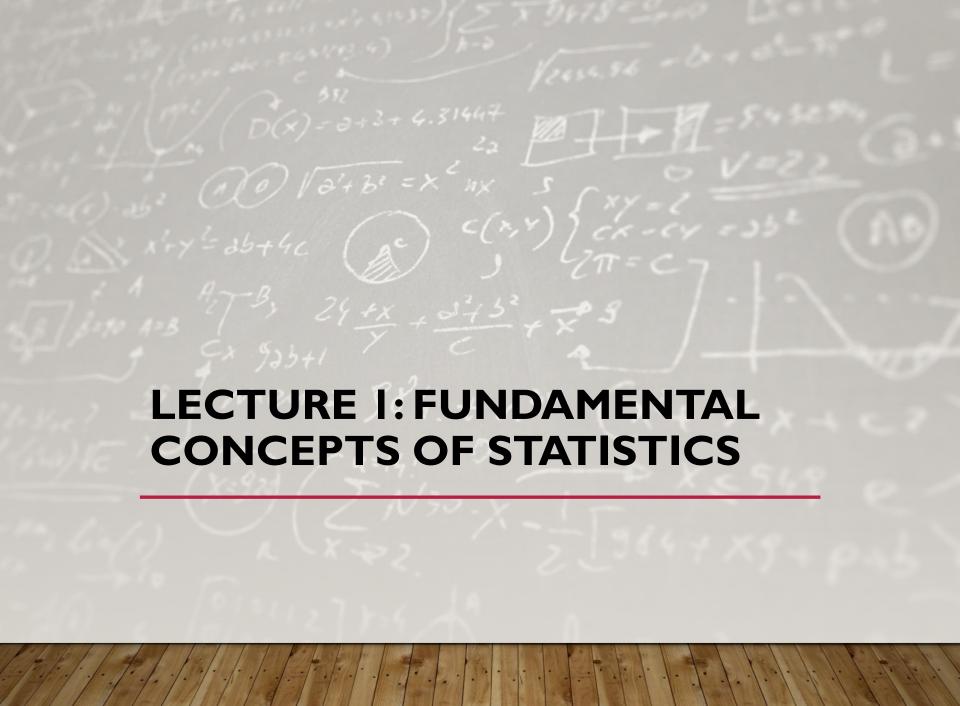
E-mail: efernandes@iseg.ulisboa.pt



https://doity.com.br/estatistica-aplicada-a-nutricao



https://basiccode.com.br/produto/informatica-basica/







WHAT IS STATISTICS?

- The science of collecting, organizing, analysing, and interpreting data.

- Applications: **Economics, Management**, Healthcare, Social Sciences, Engineering, and more.



- Purpose in **Management and Economics**: support decision-making under uncertainly, identify patterns, and predict trends.

STEPS OF A STATISTICAL STUDY

Problem Definition

 Define the research question(s).

Definition of the Measure

- Identify the variables of interest.
- Decide on appropriate indicators, scales, or metrics.

Data Collection

 Choose sampling method (random, stratified, cluster, etc.).

Description and Summarization of Data

 Use descriptive statistics, tables, and charts to organize and summarize data.

Statistical Inference

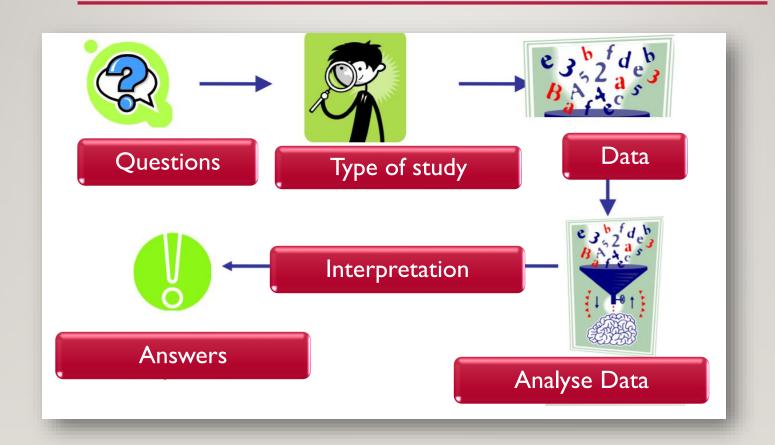
 Make generalizations from the sample to the population.

Study Report

- Present results in a clear and structured way.
- Highlight conclusions, implications, and limitations.

Purpose: Transform raw data into meaningful information.

STEPS OF A STATISTICAL STUDY: VISUAL REPRESENTATION



MEANINGS OF "STATISTICS"







Scientific Discipline

Measure:

Numerical summaries that describe characteristics of a dataset.

Examples: mean, variance, and percentages.

Data:

Synonym for numerical information in specific areas.

Examples: heath statistics, industrial statistics, and employment statistics.



Population/universe: All elements of interest in a study or research.

Types of Population: real vs hypothetical; finite vs infinite.

POPULATION AND SAMPLE

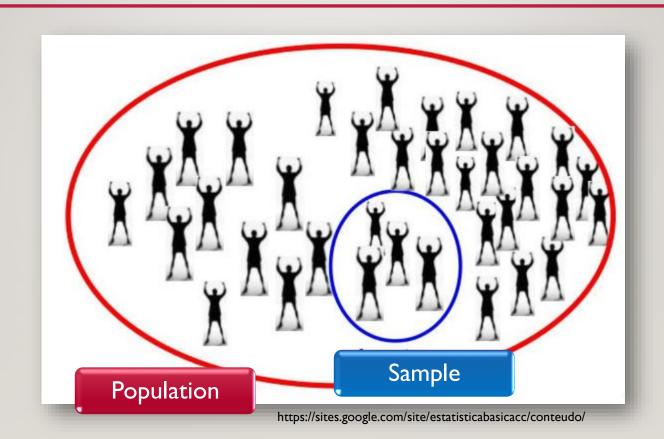


Sample: A representative subset of a population, used to draw conclusions about the whole.



Example: all customers of a company (population) vs 50 selected customers (sample).

POPULATION AND SAMPLE: VISUAL REPRESENTATION



Data summarization and reduction

- Organize and condense large datasets into understandable forms
- Examples: frequency tables, charts, and summary measures (mean, median, standard deviation)

Inference to other datasets

- •Make predictions or generalizations about a population based on sample data
- Example: estimating total sales based on a sample of transactions

$Identification \ of \ relationships \ between \ datasets$

- •Discover correlations, associations, or causal links between variables
- Example: analyzing the relationship between marketing spend and customer acquisition

Dimensionality reduction

- •Simplify data by reducing the number of variables while retaining essential information
- Example: principal component analysis in multivariate data

Classification and discrimination

- •Assign data points to categories or groups based on characteristics
- Example: categorizing customers into segments (loyal, occasional, new)

Data clustering

- •Group similar data points together to identify patterns or natural groupings
- **Example**: grouping products based on sales patterns or customer behavior

OBJECTIVES OF STATISTICAL ANALYSIS

TYPES OF STATISTICS

- Descriptive Statistics: organizes and summarizes data using tables, graphs, and measures.
- Inferential Statistics: draws conclusions about a population from a sample through estimation and hypothesis testing.
- Example: average revenue (descriptive)
 vs sales forecast (inferential).

IMPORTANCE OF SAMPLING STUDIES



Sampling: More efficient, less costly, and less time-consuming than surveying the entire population.



Census: Covers entire population, but is expensive, time-consuming, and often impractical.



Example: Surveying 1,000 households from a city (sampling) vs all households in the entire country (census).

Types of studies: census vs sampling – advantages and disadvantages

DATA COLLECTION



Sources: surveys, interviews, administrative databases, sensors, and company records.



Processes: coding, recording, and validating data.

Data Coding: transforming answers into numerical or categorical codes. **Data Recording**: storing information systematically (Excel, SPSS, SQL).

Data Validation: checking consistency, completeness, and accuracy before analysis.

TYPES OF DATA



I. Cross-Sectional Data

Observations for multiple units collected at **one point in time** (one or more variables).

Example: survey of customer satisfaction across 100 stores in January 2025.



2. Time Series Data

Observations collected **over time** for a single unit (one or more variables).

Example: monthly sales revenue of a company from January 2020 to December 2024.



3. Panel Data (Longitudinal Data)

Combines cross-sectional and time series data.
Observations for multiple units over multiple periods.

Example: annual income of 500 households from 2018 to 2024.

STATISTICAL UNIT, PARAMETER, AND STATISTICS



STATISTICAL UNIT:

Each element of the population or sample.



Sample: $(x_1, x_2, ..., x_n)$



PARAMETERS:

Characteristics of the population.

Example: population mean μ and population standard deviation σ .



STATISTICS:

Measures calculated from a sample.

Example: sample mean \bar{x} and sample standard deviation s.

RANDOM EXPERIMENT

A random experiment is a process or action whose outcome cannot be predicted with certainty in advance, even under identical conditions.

Characteristics:

- Multiple possible outcomes
- Repeatable under same conditions
- Set of all possible outcomes = Sample Space

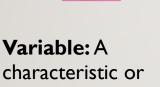
Examples:

- Roll a Die → Outcomes: 1, 2, 3, 4, 5, 6
- Coin Toss (Coin Flip) → Outcomes: Heads or Tails
- Selecting a Random Employee → Outcome: Age of selected person



VARIABLES





property observed in a random experiment.



Random variable:

Theoretical concept that assigns values to the outcomes of a random experiment.

Examples: weekly sales and number of defective items.



Empirical

variable: Observed in practice, based on collected data.

Examples: age, weight, and number of products sold.

Random Variable (X) vs Empirical Variable (x) Sample: $(x_1, x_2, ..., x_n)$

LEVELS OF MEASUREMENT

Nominal

- Categories without order.
- Examples: gender and nationality.

Ordinal

- Ordered categories.
- Example: education level.

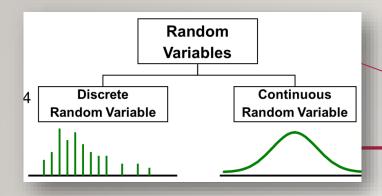
Interval

- Differences between values are meaningful, but there is no absolute zero.
- **Example:** temperature in Celsius °C (0 °C ≠ no temperature).

Ratio

- An **absolute zero exists**, and ratios are meaningful.
- **Examples:** income, age, and weight. (0 kg = no weight).





CLASSIFICATION OF VARIABLES

$$Y = ax + b$$

Number of Values

Discrete Variables:

- Take finite or countable values.
- **Examples:** Number of children and number of defective items.

Continuous Variables:

- Can take infinite values within a range.
- Examples: Height and weight.

Explanatory Orientation

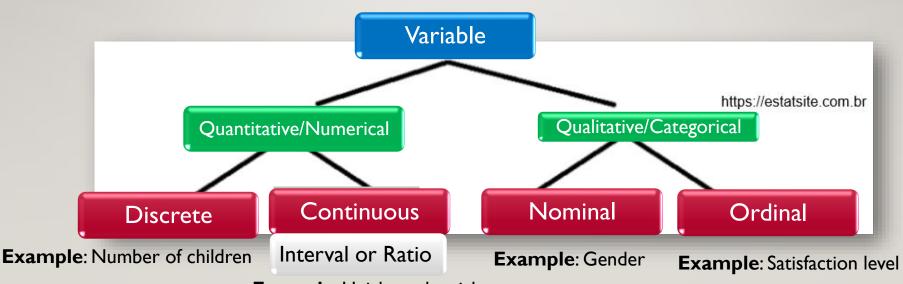
Explanatory Variable (Independent / Predictor Variable)

- A variable used to explain or predict changes in another variable.
- Represents the potential cause, influence, or input.
- Usually placed on the x-axis in graphs.
- **Examples:** marketing expenditure, study hours, and product price.

Explained Variable (Dependent / Response Variable)

- The variable whose variation we want to understand or predict.
- Represents the effect, outcome, or result.
- Usually placed on the **y-axis** in graphs.
- **Examples:** sales revenue, exam score, and demand for a product.

CLASSIFICATION OF VARIABLES: VISUAL REPRESENTATION



Example: Height and weight

EXERCISE 1.1

- 1.1 A mortgage company randomly samples accounts of their time-share customers. State whether each of the following variables is categorical or numerical. If categorical, give the level of measurement. If numerical, is it discrete or continuous?
 - a. The original purchase price of a customer's time-share unit
 - b. The state (or country) of residence of a time-share owner
 - c. A time-share owner's satisfaction level with the maintenance of the unit purchased (1: very dissatisfied to 5: very satisfied)
 - d. The number of times a customer's payment was late

Newbold et al (2013)



EXERCISE I.I: SOLUTION



Answers:

- a. **Numerical, Continuous (Ratio)** → Purchase price, any value, true zero.
- b. Categorical (Nominal) → State/country, categories with no order.
- c. Categorical (Ordinal) \rightarrow Satisfaction scale 1–5, ordered categories.
- d. **Numerical, Discrete (Ratio)** → Number of late payments, count values.

EXERCISE 1.2

- 1.2 Visitors to a supermarket in Singapore were asked to complete a customer service survey. Are the answers to the following survey questions categorical or numerical? If an answer is categorical, give the level of measurement. If an answer is numerical, is it discrete or continuous?
 - a. Have you visited this store before?
 - b. How would you rate the level of customer service you received today on a scale from 1 (very poor) to 5 (very good)?
 - c. How much money did you spend in the store today?

Newbold et al (2013)



EXERCISE 1.2: SOLUTION



Answers:

- a. Categorical (Nominal) \rightarrow Yes/No, no natural order.
- b. Categorical (Ordinal) \rightarrow Rating scale 1–5, ordered categories.
- c. **Numerical, Continuous (Ratio)** → Money spent, decimal values possible, true zero.

EXERCISE 1.5

- A number of questions were posed to a random sample of visitors to a London tourist information center. For each question below, describe the type of data obtained.
 - a. Are you staying overnight in London?
 - b. How many times have you visited London previously?
 - c. Which of the following attractions have you visited?

Tower of London **Buckingham Palace** Big Ben Covent Garden

Westminster Abbey

d. How likely are you to visit London again in the next 12 months: (1) unlikely, (2) likely, (3) very likely?

Newbold et al (2013)



EXERCISE 1.5: SOLUTION



Answers:

- .a. Are you staying overnight in London?
 - Categorical (Nominal) → Yes/No, no inherent order.
- b. How many times have you visited London previously?
 - Numerical, Discrete (Ratio) → Count of visits, zero possible, only integer values.
- c. Which of the following attractions have you visited?
 - Categorical (Nominal, Multiple Response) → Each attraction is a yes/no question; categories with no order.
- d. How likely are you to visit London again in the next 12 months?
 - Categorical (Ordinal) → Likert-type scale (e.g., very unlikely → very likely), ordered categories.

FORMAL REPRESENTATION OF DATA

 $(x_1, x_2, x_3, ..., x_n)$ ou $x_i (i = 1, 2, ..., n)$

observations of one variable n observations of two variables

 $[(x_1, y_1), (x_2, y_2), (x_3, y_3), ..., (x_n, y_n)]$

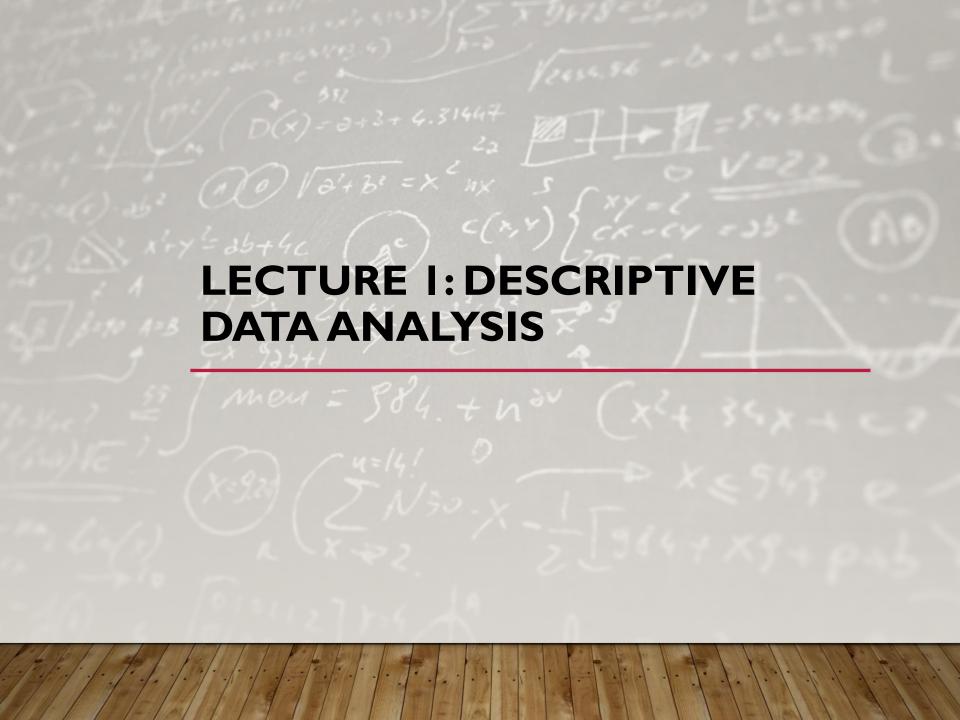
$$\mathbf{X} = \left[egin{array}{ccccc} x_{11} & x_{12} & ... & x_{1p} \ x_{21} & x_{22} & ... & x_{2p} \ ... & ... & ... & ... \ x_{n1} & x_{n2} & ... & x_{np} \end{array}
ight]$$

n observations of p variables

Contingency tables

	Ge		
Movies Attended	Men	Women	Total
0	20	40	60
1	40	30	70
2 or more	10	10	20
Total	70	80	150

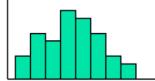
E.g. A survey of 150 adults classified each as to gender and the number of movies attended last month. Each respondent is classified according to two criteria—the number of movies attended and gender.



DESCRIPTIVE STATISTICS

- Present data
 - e.g., Tables and graphs





Summarize data

- e.g., Sample mean =
$$\frac{\sum X_i}{n}$$

Newbold et al (2013)



- **Tables**: frequency distributions.

DATA REPRESENTATION

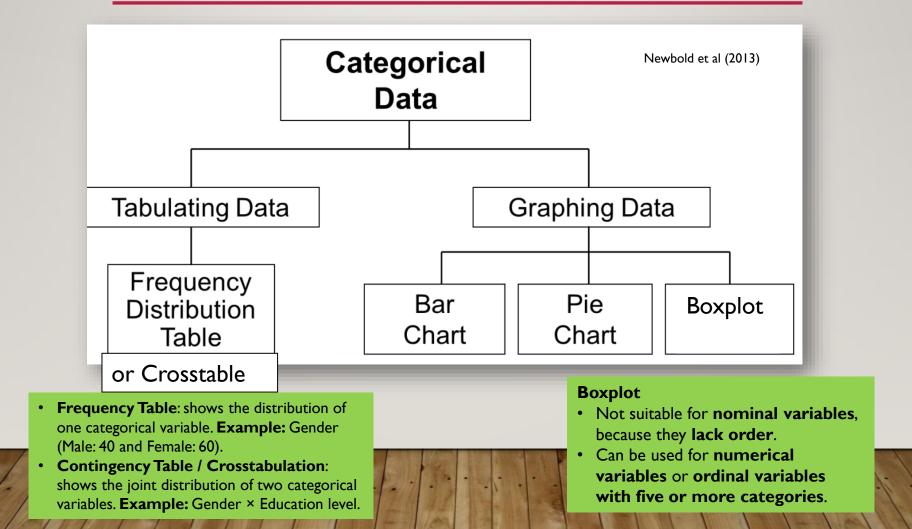


- **Graphs**: bar chart, pie chart, histogram, boxplot, line chart, etc.



- Choice depends on: type of variable & analysis purpose.

TABLES AND GRAPHS FOR CATEGORICAL VARIABLES



FREQUENCY DISTRIBUTION TABLE EXAMPLE

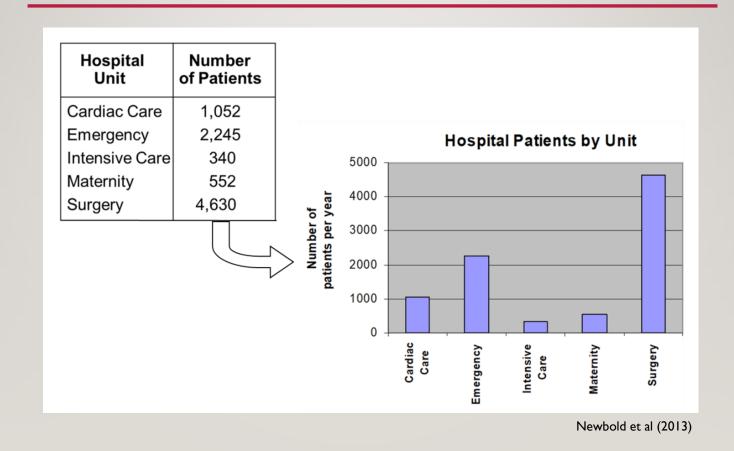
Summarize data by category Example: Hospital Patients by Unit

Hospital Unit	Number of Patients	Percent (rounded)
Cardiac Care	1,052	11.93
Emergency	2,245	25.46
Intensive Care	340	3.86
Maternity	552	6.26
Surgery	4,630	52.50
Total:	8,819	100.0

(Variables are categorical)

Newbold et al (2013)

BAR CHART EXAMPLE



PIE CHART EXAMPLE

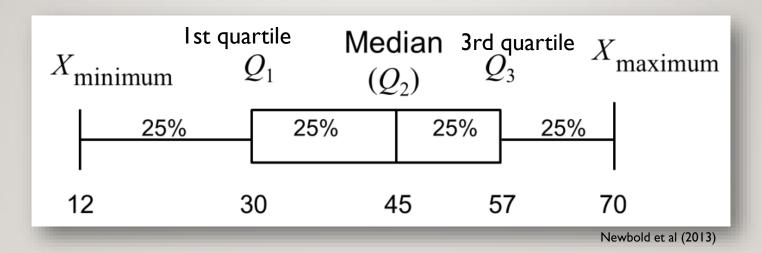
Newbold et al (2013)

Hospital Unit	Number of Patients	% of Total	Hamital Dationto by Unit
Cardiac Care Emergency	1,052 2,245	11.93 25.46	Hospital Patients by Unit Cardiac Care
Intensive Care Maternity	340 552	3.86 6.26	12%
Surgery	4,630	52.50	Emergeney
			Surgery 53%
		(Percentages are rounded the nearest	
		percent)	 Bar charts and Pie charts

used for qualitative (categorical) data. Height of bar or size of pie slice shows the frequency or percentage for each

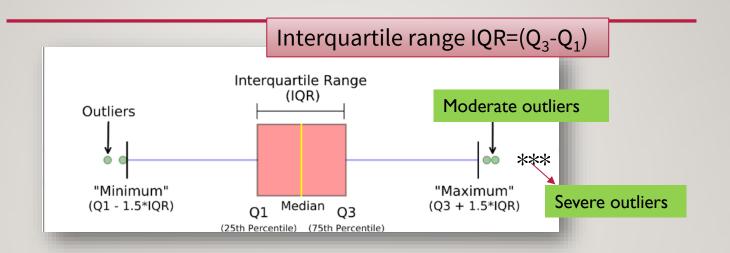
category.

BOX-AND-WHISKER PLOT/ BOXPLOT EXAMPLE



The plot can be oriented horizontally or vertically.

BOXPLOT AND OUTLIERS



Moderate outliers (marked with a circle)

$$(Q_1-1,5 \times IQR; Q_3+1,5 \times IQR)$$
 Inner fences

Severe outliers (marked with an asterisk)

$$(Q_1-3 \times IQR; Q_3+3 \times IQR)$$
 Outer fences

CROSSTABLE EXAMPLE

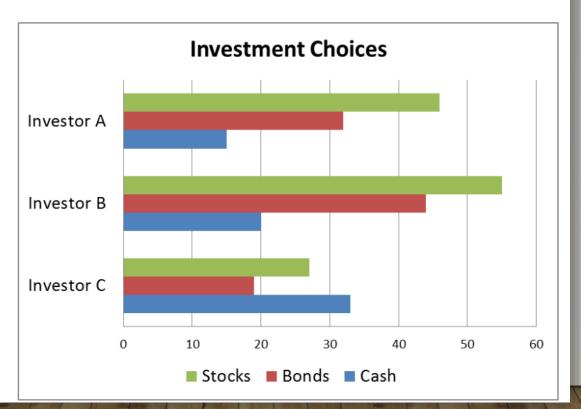
 3×3 Cross Table for Investment Choices by Investor (values in \$1000's)

Investment Category	Investor A	Investor B	Investor C	Total
Stocks	46	55	27	128
Bonds	32	44	19	95
Cash	15	20	33	68
Total	93	119	79	291

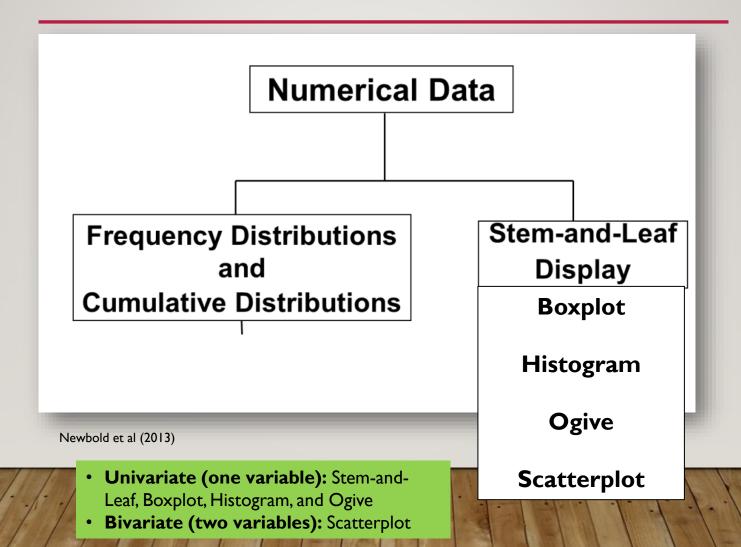
Newbold et al (2013)

GRAPHING MULTIVARIATE CATEGORICAL DATA

Side by side horizontal bar chart



GRAPHS TO DESCRIBE NUMERICAL VARIABLES



FREQUENCY DISTRIBUTION EXAMPLE

Data in ordered array:

12, 13, 17, 21, 24, 24, 26, 27, 27, 30, 32, 35, 37, 38, 41, 43, 44, 46, 53, 58

Interval	Frequency	Relative Frequency	Percentage
10 but less than 20	3	.15	15
20 but less than 30	6	.30	30
30 but less than 40	5	.25	25
40 but less than 50	4	.20	20
50 but less than 60	2	.10	10
Total	20	1.00	100

Newbold et al (2013)

"Square root rule for the number of classes: The number of classes (k) can be estimated as the square root of the number of observations (n):

$$k \approx \sqrt{n}$$

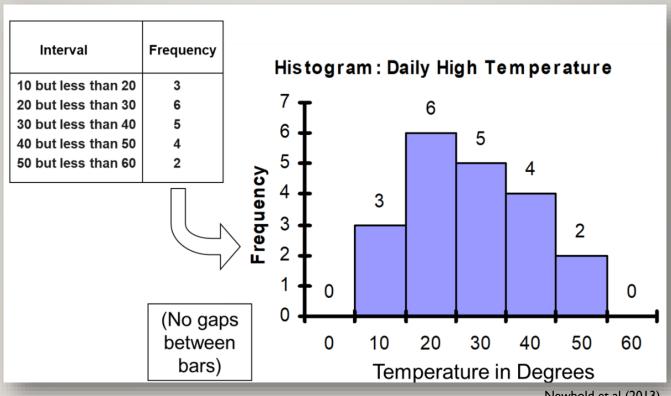
n = 20 (sample size)
k =
$$\sqrt{20}$$
 =
4.47 ~ 5 (number of classes)

CLASS INTERVALS

- Each class grouping has the same width
- Determine the width of each interval by $w = \text{interval width} = \frac{\text{largest number} \text{smallest number}}{\text{number of desired intervals}}$
- Use at least 5 but no more than 15-20 intervals
- Intervals never overlap
- Round up the interval width to get desirable interval endpoints

Newbold et al (2013)

HISTOGRAM EXAMPLE



Newbold et al (2013)

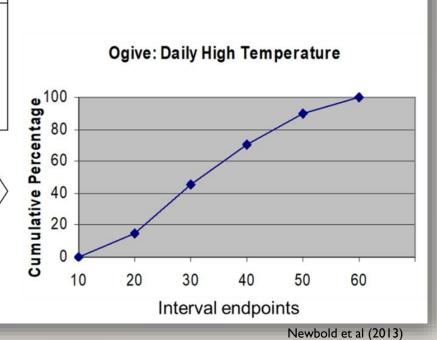
n = 20 (sample size)

 $k = \sqrt{20} = 4.47 \sim 5$ (number of classes)

Width of each interval = $(58 - 12) / 5 = 9.2 \sim 10$

THE OGIVE GRAPHING CUMULATIVE FREQUENCIES

Interval	Upper interval endpoint	Cumulative Percentage
Less than 10	10	0
10 but less than 20	20	15
20 but less than 30	30	45
30 but less than 40	40	70
40 but less than 50	50	90
50 but less than 60	60	100



STEM-AND-LEAF DIAGRAM EXAMPLE

Data in ordered array:

21, 24, 24, 26, 27, 27, 30, 32, 38, 41

Completed stem-and-leaf diagram:

Stem	Leaves						
2	1	4	4	6	7	7	
3	0	2	8				
4	1						

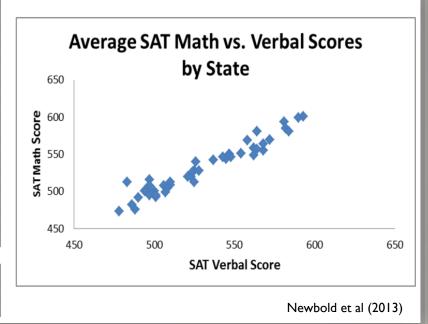
A simple way to see distribution details in a data set.

Method: Separate the sorted data series into leading digits (the stem) and the trailing digits (the leaves)

Newbold et al (2013)

SCATTER DIAGRAM /SCATTERPLOT EXAMPLE

Average SAT scores by state: 1998					
	Verbal	Matl			
Alabama	562	558			
Alaska	521	52			
Arizona	525	52			
Arkansas	568	55			
California	497	510			
Colorado	537	54			
Connecticut	510	50			
Delaware	501	49			
D.C.	488	47			
Florida	500	50			
Georgia	486	48			
Hawaii	483	51			
• • •					
W.Va.	525	51			
Wis.	581	59			
Wyo.	548	54			



Scatter Diagrams are used for paired observations taken from two numerical variables.

One variable is measured on the vertical axis and the other variable is measured on the horizontal axis.

THANKS!

Questions?