risk premium fair game risk averse utility certainty equivalent rate

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risk neutral risk lover mean-variance (M-V) criterion indifference curve complete portfolio risk-free asset capital allocation line reward-to-volatility ratio passive strategy capital market line

KEY TERMS

- 1. Which of the following choices best completes the following statement? Explain. An investor with a higher degree of risk aversion, compared to one with a lower degree, will prefer investment portfolios
 - a. with higher risk premiums.
 - b. that are riskier (with higher standard deviations).
 - c. with lower Sharpe ratios.
 - d. with higher Sharpe ratios.
 - e. None of the above is true.
- 2. Which of the following statements are true? Explain.
 - a. A lower allocation to the risky portfolio reduces the Sharpe (reward-to-volatility) ratio.
 - b. The higher the borrowing rate, the lower the Sharpe ratios of levered portfolios.
 - c. With a fixed risk-free rate, doubling the expected return and standard deviation of the risky portfolio will double the Sharpe ratio.
 - d. Holding constant the risk premium of the risky portfolio, a higher risk-free rate will increase the Sharpe ratio of investments with a positive allocation to the risky asset.
- 3. What do you think would happen to the expected return on stocks if investors perceived higher volatility in the equity market? Relate your answer to Equation 6.12.
- 4. Consider a risky portfolio. The end-of-year cash flow derived from the portfolio will be either \$70,000 or \$200,000 with equal probabilities of .5. The alternative risk-free investment in T-bills pays 6% per year.
 - a. If you require a risk premium of 8%, how much will you be willing to pay for the portfolio?
 - b. Suppose that the portfolio can be purchased for the amount you found in (a). What will be the expected rate of return on the portfolio?
 - c. Now suppose that you require a risk premium of 12%. What is the price that you will be willing to pay?
 - d. Comparing your answers to (a) and (c), what do you conclude about the relationship between the required risk premium on a portfolio and the price at which the portfolio will sell?
- 5. Consider a portfolio that offers an expected rate of return of 12% and a standard deviation of 18%. T-bills offer a risk-free 7% rate of return. What is the maximum level of risk aversion for which the risky portfolio is still preferred to bills?
- 6. Draw the indifference curve in the expected return–standard deviation plane corresponding to a utility level of .05 for an investor with a risk aversion coefficient of 3. (*Hint:* Choose several possible standard deviations, ranging from .05 to .25, and find the expected rates of return providing a utility level of .05. Then plot the expected return–standard deviation points so derived.)
- 7. Now draw the indifference curve corresponding to a utility level of .04 for an investor with risk aversion coefficient A = 4. Comparing your answers to Problems 6 and 7, what do you conclude?

PROBLEM SETS

Quiz

Problems

- 8. Draw an indifference curve for a risk-neutral investor providing utility level .05.
- 9. What must be true about the sign of the risk aversion coefficient, A, for a risk lover? Draw the indifference curve for a utility level of .05 for a risk lover.

For Problems 10 through 12: Consider historical data showing that the average annual rate of return on the S&P 500 portfolio over the past 80 years has averaged roughly 8.5% more than the Treasury bill return and that the S&P 500 standard deviation has been about 20% per year. Assume these values are representative of investors' expectations for future performance and that the current T-bill rate is 5%.

10. Calculate the expected return and variance of portfolios invested in T-bills and the S&P 500 index with weights as follows:

W_{bills}	W _{index}
0 11 2 11	1.0
0.2	0.8
0.4	6,0
0.6	0.4
0.8	0.2
1:0	0

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- 11. Calculate the utility levels of each portfolio of Problem 10 for an investor with A=3. What do you conclude?
- 12. Repeat Problem 11 for an investor with A = 5. What do you conclude?

Use these inputs for Problems 13 through 22: You manage a risky portfolio with expected rate of return of 18% and standard deviation of 28%. The T-bill rate is 8%.

- Your client chooses to invest 70% of a portfolio in your fund and 30% in a T-bill money market fund. What is the expected value and standard deviation of the rate of return on his portfolio?
- 14.)Suppose that your risky portfolio includes the following investments in the given proportions:

Stock A	25%
Stock B	32%
Stock C	43%

What are the investment proportions of your client's overall portfolio, including the position in T-bills?

- 15. What is the reward-to-volatility ratio (S) of your risky portfolio? Your client's?
- 16. Draw the CAL of your portfolio on an expected return-standard deviation diagram. What is the slope of the CAL? Show the position of your client on your fund's CAL.
- 17. Suppose that your client decides to invest in your portfolio a proportion y of the total investment budget so that the overall portfolio will have an expected rate of return of 16%.
 - a. What is the proportion y?
 - b. What are your client's investment proportions in your three stocks and the T-bill fund?
 - c. What is the standard deviation of the rate of return on your client's portfolio?
- 18. Suppose that your client prefers to invest in your fund a proportion y that maximizes the expected return on the complete portfolio subject to the constraint that the complete portfolio's standard deviation will not exceed 18%.
 - a. What is the investment proportion, y?
 - b. What is the expected rate of return on the complete portfolio?
- 19. Your client's degree of risk aversion is A = 3.5.
 - a. What proportion, y, of the total investment should be invested in your fund?

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- 20. Look at the data in Table 6.8 on the average risk premium of the S&P 500 over T-bills, and the standard deviation of that risk premium. Suppose that the S&P 500 is your risky portfolio.
 - a. If your risk-aversion coefficient is A = 4 and you believe that the entire 1926–2005 period is representative of future expected performance, what fraction of your portfolio should be allocated to T-bills and what fraction to equity?
 - b. What if you believe that the 1986-2005 period is representative?
 - c. What do you conclude upon comparing your answers to (a) and (b)?
- 21. Consider the following information about a risky portfolio that you manage, and a risk-free asset: $E(r_p) = 11\%$, $\sigma_p = 15\%$, $r_f = 5\%$.
 - a. Your client wants to invest a proportion of her total investment budget in your risky fund to provide an expected rate of return on her overall or complete portfolio equal to 8%. What proportion should she invest in the risky portfolio, P, and what proportion in the risk-free asset?
 - b. What will be the standard deviation of the rate of return on her portfolio?
 - c. Another client wants the highest return possible subject to the constraint that you limit his standard deviation to be no more than 12%. Which client is more risk averse?

For Problems 22 through 25: Suppose that the borrowing rate that your client faces is 9%. Assume that the S&P 500 index has an expected return of 13% and standard deviation of 25%, that $r_f = 5\%$, and that your fund has the parameters given in Problem 21.

- 22. Draw a diagram of your client's CML, accounting for the higher borrowing rate. Superimpose on it two sets of indifference curves, one for a client who will choose to borrow, and one who will invest in both the index fund and a money market fund.
- 23. What is the range of risk aversion for which a client will neither borrow nor lend, that is, for which y = 1?
- 24. Solve Problems 22 and 23 for a client who uses your fund rather than an index fund.
- 25. What is the largest percentage fee that a client who currently is lending (y < 1) will be willing to pay to invest in your fund? What about a client who is borrowing (y > 1)?

For Challenge Problems 26 and 27: You estimate that a passive portfolio, that is, one invested in a risky portfolio that mimics the S&P 500 stock index, yields an expected rate of return of 13% with a standard deviation of 25%. You manage an active portfolio with expected return 18% and standard deviation 28%. The risk-free rate is 8%.

Challenge Problems

- 26. Draw the CML and your funds' CAL on an expected return-standard deviation diagram.
 - a. What is the slope of the CML?
 - b. Characterize in one short paragraph the advantage of your fund over the passive fund.
- Your client ponders whether to switch the 70% that is invested in your fund to the passive portfolio.
 - a. Explain to your client the disadvantage of the switch.
 - b. Show him the maximum fee you could charge (as a percentage of the investment in your fund, deducted at the end of the year) that would leave him at least as well off investing in your fund as in the passive one. (*Hint:* The fee will lower the slope of his CAL by reducing the expected return net of the fee.)
- 28. Consider again the client in Problem 19 with A = 3.5.
 - a. If he chose to invest in the passive portfolio, what proportion, y, would he select?
 - b. Is the fee (percentage of the investment in your fund, deducted at the end of the year) that you can charge to make the client indifferent between your fund and the passive strategy affected by his capital allocation decision (i.e., his choice of y)?

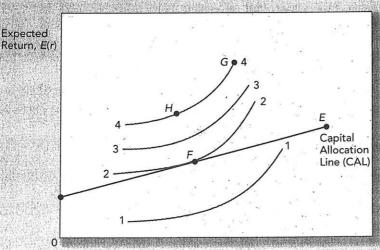
Use the following data in answering CFA Problems 1–3:

Utility Formula Data

Investment	Expected Return, E(r)	Standard Deviation, o
Olever Holes	.12	.30
2	.15	.50
3.	.21	.16
4	.24	.21

- 1. Based on the utility formula above, which investment would you select if you were risk averse with A = 4?
- 2. Based on the utility formula above, which investment would you select if you were risk neutral?
- 3. The variable (A) in the utility formula represents the:
- a. investor's return requirement.
- b. investor's aversion to risk.
- c. certainty equivalent rate of the portfolio.
- d. preference for one unit of return per four units of risk.

Use the following graph to answer CFA Problems 4 and 5.



- Risk, c
- 4. Which indifference curve represents the greatest level of utility that can be achieved by the investor?
- 5. Which point designates the optimal portfolio of risky assets?
- 6. Given \$100,000 to invest, what is the expected risk premium in dollars of investing in equities versus risk-free T-bills based on the following table?

Action	Probability	Expected Return
Invest in		\$50,000
equities	.4 —	
Invest in risk-free		
T-bills	1.0	\$ 5,000

- 7. The change from a straight to a kinked capital allocation line is a result of the:
 - a. Reward-to-volatility ratio increasing.
 - b. Borrowing rate exceeding the lending rate.
 - c. Investor's risk tolerance decreasing.
 - d. Increase in the portfolio proportion of the risk-free asset.
- 8. You manage an equity fund with an expected risk premium of 10% and an expected standard deviation of 14%. The rate on Treasury bills is 6%. Your client chooses to invest \$60,000 of her portfolio in your equity fund and \$40,000 in a T-bill money market fund. What is the expected return and standard deviation of return on your client's portfolio?
- 9. What is the reward-to-volatility ratio for the equity fund in CFA Problem 8?
 - 1. Go to www.mhhe.com/edumarketinsight (Have you remembered to bookmark this page?) and link to Company, then Population. Select a company of interest to you and link to the Stock Reports page. Observe the menu of company information reports on the left. Link to the Recent News and review the most recent Business Wire articles. What recent event or information release had an apparent impact upon your company's stock price? (You can find a history of stock prices under Excel Analytics.)
 - 2. Go to www.mhhe.com/edumarketinsight and link to Industry. From the pull-down menu, link to an industry that is of interest to you. From the menu on the left side, select the S&P 500 report under Industry GICS Sub-Industry Financial Highlights. How many companies from this industry are in the S&P 500? What percentage of the Main Industry Group does this Industry Group represent in the S&P 500? Look at the ratios provided for the industry and their comparisons to the GICS Sub-Industry Benchmarks. How did the industry perform relative to S&P 500 companies during the last year?

STANDARD &POOR'S

Risk Aversion

E-Investments

There is a difference between an investor's willingness to take risk and his or her ability to take risk. Take the quizzes offered at the Web sites below and compare the results. If they are significantly different, which one would you use to determine an investment strategy?

http://mutualfunds.about.com/library/personalitytests/blrisktolerance.htm http://mutualfunds.about.com/library/personalitytests/blriskcapacity.htm

SOLUTIONS TO CONCEPT CHECKS

1. The investor is taking on exchange rate risk by investing in a pound-denominated asset. If the exchange rate moves in the investor's favor, the investor will benefit and will earn more from the U.K. bill than the U.S. bill. For example, if both the U.S. and U.K. interest rates are 5%, and the current exchange rate is \$2 per pound, a \$2 investment today can buy 1 pound, which can be invested in England at a certain rate of 5%, for a year-end value of 1.05 pounds. If the year-end exchange rate is \$2.10 per pound, the 1.05 pounds can be exchanged for $1.05 \times \$2.10 = \2.205 for a rate of return in dollars of 1 + r = \$2.205/\$2 = 1.1025, or r = 10.25%, more than is

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