## Corporate Investment Appraisal <br> Masters in Finance <br> 2012-2013 <br> Fall Semester <br> Clara C Raposo

## Problem Set 3: Valuation of Financial Options

1. The annual volatility of the return of company CJ's stock is $50 \%$. Currently CJ's stock price is $€ 4.25$. The risk-free interest rate is $3 \%$ per annum (continuous).
(a) Compute the risk neutral probability of the scenario "up" in the context of the binomial model (1 year time step).

| u | 1.648721271 |
| :--- | ---: |
| d | 0.60653066 |
| p | 0.406762323 |

(b) What is the value of a European call option on a share of company CJ , with a strike price of $€ 5.25$ and time to maturity of 1 year? Use the binomial model.

| Call |  |
| :--- | ---: |
| K | 5.25 |
| T | 1 |


| Stock Tree | Year | 0 | 1 |
| :--- | :--- | ---: | ---: |
|  |  | 4.25 | 7.0070654 |
|  |  |  | 2.577755304 |
| Call |  |  |  |
| Tree | Year | 0 | 1 |
|  |  | 0.693585191 | 1.7570654 |
|  |  |  | 0 |

(c) Estimate the value of a put option on a share of company CJ, with expiry date in 3 years' time and an exercise price of €5.0.

| K | 5 |
| :--- | :--- |
| T | 3 |


| Stock Tree | Year |  | 0 | 1 | 2 | 3 |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: |
|  |  | 4.25 | 7.0070654 | 11.55269777 | 19.04717855 |  |
|  |  |  | 2.577755304 | 4.25 | 7.0070654 |  |
| Put Tree |  |  |  | 1.563487625 | 2.577755304 |  |
|  |  |  |  |  | 0.948303181 |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  | 3 |  |
|  |  | 1.723817963 | 0.802819283 | 0 | 0 |  |
|  |  | 2.443808705 | 1.394498028 | 0 |  |  |
|  |  |  | 3.288740043 | 2.422244696 |  |  |
|  |  |  |  | 4.051696819 |  |  |

2. The shares of firm MC have an annual volatility of $40 \%$ and are currently priced at \$4.0. There is no expectation of a dividend in the coming year. The riskless annual interest rate is 3\% (continuous).
(a) What is the value (BS) of a call option on share of firm MC, for a maturity of 1 year and an exercise price of $\$ 6.0$ ?


Using Black-Scholes

| d1 | -0.73866277 |
| :--- | :--- |
| d2 | -1.13866277 |
| $N(d 1)$ | 0.230055899 |
| $N(d 2)$ | 0.127421918 |
| Call | 0.178287407 |

(b) What is the value (BS) of a European put option on a share of Firm MC, with expiry date in 8 months time, and with an exercise price of $\$ 6.0$ ?

| Put |  |
| :--- | ---: |
| T | 0.67 |
| K | 6 |


| d1 | 1.016941719 |
| :--- | ---: |
| d2 | 1.343540352 |


| $N(d 1)$ | 0.154590578 |
| :--- | :--- |
| $N(d 2)$ | 0.089548535 |


| Call | 0.09 |
| :--- | :--- |
| Put | 1.97 |

3. Consider again the data of problem 1, regarding company CJ: The annual stock volatility is $50 \%$ and the stock price is currently $€ 4.25$. No dividend is expected for the coming year. The riskless annual interest rate is 3\% (continuous).

Re-compute the value of a call option with maturity of 1 year, with an exercise price of $€ 5.25$, based on the binomial model, considering intervals of four months (each branch is 4 months long).

| Stock |  |
| :--- | ---: |
| Sigma | 0.5 |
| S | 4.25 |
| Rf | $3 \%$ |


| Number of intervals | N | 3 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Time to maturity | T | 1 | Dt | $\begin{array}{r} 0.33 \\ 3333 \\ 333 \end{array}$ | Time Step |
| Strike <br> Price | K | 5.25 |  |  |  |
| u 1.334658074 <br> d 0.749255573 |  |  |  |  |  |


| p | 0.445496208 |
| :--- | :--- |


| Stock <br> Tree |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Month | 0 | 4 | 8 | 12 |
|  | 4.25 | 5.672296814 | 7.57057674 | 10.10413137 |
|  |  | 3.184336186 | 4.25 | 5.672296814 |
|  |  |  | 2.385881634 | 3.184336186 |
|  |  |  |  | 1.787635111 |

Call Tree

| Month | 0 | 4 | 8 | 12 |
| ---: | ---: | ---: | ---: | ---: |
|  | 0.55180128 | 1.148816044 | 2.372815113 | 4.85413137 |
|  | 0.08215234 | 0.186259688 | 0.422296814 |  |
|  |  | 0 | 0 |  |
|  |  |  |  | 0 |

