Instituto Superior de Economia e Gestão
unversidnoe técnca de usboa

## CORPORATE INVESTMENT APPRAISAL

MASTERS IN FINANCE
EXAM

## 30 JANUARY 2013

## 2 HOURS

## INSTRUCTIONS TO READ BEFORE STARTING ANSWERING THE QUESTIONS

1. Please fill in your name and student number.
2. The exam has 5 groups of questions, with marks clearly indicated.
3. You may use one A4 sheet of paper with notes.
4. The cumulative Normal distribution table is attached at the end.
5. You may un-staple the Normal table, and the scrap paper. Nothing else.

## Good Luck!

Name $\qquad$ No. $\qquad$

PROFESSOR CLARA RAPOSO'S VIP AREA:

| GROUP | GRADE | COMMENT |
| :---: | :--- | :--- |
| I |  |  |
| II |  |  |
| III |  |  |
| IV |  |  |
| $\mathbf{V}$ |  |  |
| TOTAL |  |  |

## GROUP I (4 points)

Over the last couple of years firm MILAN has invested 250000 in the development of a new prototype. In order to launch the new product in the market, MILAN is considering investing in a new line of production, for which it has developed the following financial projections:

| New Project | Year 1 |
| :--- | ---: |
| Revenues | $€ 1280000$ |
| Costs of Goods Sold | 590000 |
| Depreciation | 300000 |
| Interest Payments | 50000 |
| Earnings Before Taxes | 340000 |
| Net Income | $€ 221000$ |

The project requires an immediate capital expenditure of $€ 900000$ in equipment with a life of 3 years, which is the time period for which the project will last. Revenues and Costs of Goods Sold are expected to grow 2\% per year. Annual net working capital is $10 \%$ of next year's revenues. Consider a discount rate of $15 \%$ for this project.
(I.a) (1.5 points) Compute the Free Cash Flows of the project. Show your computations.

| Tc | 0,35 |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
| t | 0 | 1 | 2 | 3 |
| Revenues | 0 | 1280000 | 1305600 | 1331712 |
| Costs of Goods |  |  |  |  |
| Sold | 0 | 590000 | 601800 | 613836 |
| Depreciation | 0 | 300000 | 300000 | 300000 |
| EBIT | 0 | 390000 | 403800 | 417876 |
| EBIT(1-Tc) | 0 | 253500 | 262470 | 271619,4 |
| Oper CF | 0 | 553500 | 562470 | 571619,4 |
| CapEx | 900000 | 0 | 0 | 0 |
| NWC | 128000 | 130560 | 133171,2 | 0 |
| Change in NWC | 128000 | 2560 | 2611,2 | -133171 |
| FCF | -1028000 | 550940 | 559858,8 | 704790,6 |

(I.b) (1.5 points) Read the following statement made your partner, Ms. K: "Forget this project! A 3-year project with annual Net Income around 220000 will surely offer an internal rate of return well below the $15 \%$ required by investors for a 900000 Capital Expenditure".
Do you agree with the statement made by Ms. K? Explain why you do, or do not, agree.

Investment decisions are not based on net income versus capital expenditure. Instead, they are based on FCF (as computed in part I.a).
Based on these FCF one may compute the NPV (using the $15 \%$ required by investors). In this case:
NPV €337.823,21
For this reason (NPV>0) MILAN should invest in the project.
Indeed, the IRR>15\%, since NPV>0 and cash flow structure (negative first, and then only one change of sign).
If we wanted we could check that
IRR 33\%
For all these reasons we must disagree with Ms. K's statement.
(I.C) (1 point) To make a final decision your boss Mr. WAKI asks you to compute the Modified Internal Rate of Return (instead of the "normal" IRR) in order to compare this project to others that the company has in its pipeline.
Compute the Modified IRR and explain why this could be a better criterion for decision-making.

Compounded CFt=2 728618,15 643837,6 704790,6
Final Value 2077246
MIRR 26,42\%

This can be a better criterion (especially when choosing from a portfolio of mutually exclusive projects) since "normal" IRR may overestimate the return of the project by assuming reinvestment of intermediate cash flows at the IRR itself. The Modified IRR considers reinvestment of cash flows of the project at the "normal" rate of return of $15 \%$.

## GROUP II (5 points)

Firm MILAN considers investing in new project IRA (same industry as usual for the company), for which the free cash flows have already been estimated:

| $t$ | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: |
| $\mathrm{FCF}_{\mathrm{t}}$ | -1000 | 530 | 725 |

We know that MILAN is financed with a ratio $\mathrm{D} / \mathrm{E}=0.25$, the beta of its shares is 1.5 , and the firm is subject to corporate taxation at rate $30 \%$. The firm's debt has an annual cost of $4 \%$, which is $1 \%$ higher than the risk-free interest rate, and the market risk premium is $4.5 \%$.

MILAN

| D/E | 0,25 | $D /(D+E)$ |
| :--- | ---: | ---: |
| Be | 1,5 | 0,2 |
| Tc | $30 \%$ |  |
| Rd | $4 \%$ |  |
| Rm-Rf | $5 \%$ |  |
| Rf | $3 \%$ |  |

(II.a) (1.75 points) Assuming that the project is financed exclusively with equity, how good is it? Show your computations and explain your answer.

APV method

| $R e$ | $9,75 \%$ |
| :--- | :--- |
| $R u$ | $8,60 \%$ |

NPV 102,7509 €
(II.b) (1.75 points) If the company decides to finance the project with a target ratio of leverage $D / E=0.5$, the cost of debt would remain the same. What would happen to the NPV of the project? Explain your answer showing your computations.

Old capital Structure
D/E
0,25

Pre-Tax Wacc 8,60\%

New Capital Structure

D/E 0,5

| New Rd | $4,00 \%$ | same |
| :--- | ---: | ---: |
| New Re | 0,109 |  |
| New WACC |  | 0,082 |

(II.c) (1.5 points) Assume that the cost of debt remains equal to 4\%, and that MILAN will get a loan for 2 years, with annual interest payments and full reimbursement in the end. What loan should MILAN get in order to see the present value of the project increase to 1115 ? Explain your answer showing all your steps.

```
Vu
    €1.102,75
Vu+PV(ITS) 1115
PV(ITS) €12,25
EA(4%,2) 6,494424989 ITS
    21,6480833 Interest
    541,2020825 Loan
```


## GROUP III (3 points)

According to the trade-off theory, which are the main factors that explain the choice of capital structure made by a firm? Explain your arguments based on empirical evidence, numerical examples and/or graphs.

Explain main factors that influence choice of capital structure, and in what direction: different types of taxes, costs of financial distress, agency costs and benefits of debt.

VL=Vu+.......etc

Should give examples (e.g., tax advantage of debt, what are financial distress costs, etc), can show a graph with "optimal capital structure" and the effects of different factors, can discuss empirical evidence on differences across industries, countries, etc.

## GROUP IV (4 points)

Firm MILAN has just announced a new issue of convertible bonds. 5000 bonds will be placed in the market at their nominal value, which is $€ 1000$. The bonds promise to pay an annual coupon of $7 \%$. Each bond may be converted into shares at maturity for a price of $€ 10$ per share, which takes place in three years time. By then the company wishes to see its equity value increase by $€ 5,000,000$ (if conversion takes place). The current stock price of MILAN is $€ 8$, and its market capitalization is $€ 80,000,000$. The firm currently has no debt. We have estimated an annual volatility of $15 \%$ for MILAN's assets. The risk-free interest rate is $3 \%$ (continuous compounding) and the yield-tomaturity (continuous time) of the straight bonds issued by companies similar to MILAN is 6\%.

| \#convertibles m | 5000 proceeds | 5000000 |  | price convertible | 1000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| F | 5000000 | K | 10 |  |  |
| T | 3 |  |  |  |  |
| P | 8 |  |  |  |  |
| Pn | 80000000 |  |  |  |  |
| N | 10000000 | $\mathrm{mrK}=\mathrm{F}$ |  |  |  |
|  |  | 5000r10 | 5000000 |  |  |
|  |  | r | 100 |  |  |
| Sigma | 15\% |  |  |  |  |
| Rf | 3\% |  |  |  |  |
| Y | 6\% coupon | 7\% |  |  |  |

(IV.a) (2.5 points) What is the value of the convertible bonds issue at the time of its announcement? Comment briefly.
Straight Bond Component

| t | 1 | 2 | 3 |
| :--- | ---: | ---: | ---: |
| Coupon | 350000 | 350000 | 350000 |
| Reimbursement | 0 | 0 | 5000000 |
| PV(Coup) | 329617,59 | 310422,15 | 292344,57 |
| PV(Princ) | 0,00 | 0,00 | 4176351,06 |
|  | $932.384,31$ |  |  |
| Total(coup) | $€$ |  |  |
| 5.108.735,37 € | Total Straight |  |  |
| lambda | 0,047619048 |  |  |
| Warrants=lambda*Call |  |  |  |
| F/lambda | 105000000 |  |  |
| d1 | $-0,37946895$ |  |  |
| d2 | $-0,63927658$ |  |  |
| N(d1) | 0,352169827 |  |  |
| N(d2) | 0,261321512 |  |  |
| Call | 4528940,35 |  |  |
| Warrants | 215663,8263 | Assuming zero NPV investment of the proceeds. |  |
| Convertibles | 5324399,20 | Sold too cheaply. |  |

(IV.b) (1.5 points) What is the expected price of the shares immediately after the convertibles are issued? Comment briefly.

```
Keeping the same assumptions
P 7,96756008
price goes down since the bonds are sold too cheaply.
```


## GROUP V (4 points)

In the framework of Merton's model, consider the following data of company MILAN: Equity has a market cap of 15 and a volatility of $30 \%$. In 2 years' time, a loan of 100 reaches its maturity (ignore intermediate cash flows). Additionally we know that the risk-free interest rate is $3 \%$ per year (continuous time), and that the bankruptcy costs are approximately $25 \%$ of the value of the assets at liquidation.

You are told that the value of MILAN's Assets follows a binomial model, for which we have the following information:

| TODAY | Year 1 | Year 2 |
| :---: | :---: | :---: |
| 104.2596 | 107.2925 | 110.4137 |
|  | 101.3124 | 104.2596 |
|  |  | 98.4485 |

(V.a) (2 points) Is it credible to you that the Tree for the Value of the Assets of company MILAN is the one in the previous table? Show your computations and explain your answer.

Market Parameters

| Stock Price: | 15 | r: | 3\% |
| :---: | :---: | :---: | :---: |
| B/Ruptcy |  |  |  |
| Stock Vol: | 30\% | Cost: | 25\% |
| Debt Par: | 100 |  |  |

Tree Parameters

| Dt: | 1 |
| ---: | ---: |
| u: | 1,02909 |
| d: | 0,971732 |
| p: | 1,023785 |

Stock Value Tree

| 11,3696 | 10,8817 | 10,4137 |
| ---: | ---: | ---: |
|  | 4,4937 | 4,2596 |
|  |  | 0,0000 |

11.37 different from the market cap of 15 . Not consistent with market values.
(V.b) (2 points) Consider the same tree for MILAN's assets, but adjust your analysis to accommodate Anderson and Sundaresan's 1996 model of strategic debt service. Consider again that the firm has a loan of 100 to be repaid at time 2 (CS2) and no debt service is planned for time 1. To simplify, consider that the cash flows of the firm each period coincide with the value of the assets ( $\mathrm{ft}=\mathrm{Vt}$ ). Bankruptcy costs are $25 \%$ of the value of the firm at liquidation, and the risk-free rate (continuous time) is $3 \%$ per year.
What is the debt service that will be chosen by the shareholders in equilibrium at time 2 (in each scenario), and what is the present value of the loan at time 0 ? Explain.
CS1=0
CS2 $=100$
$\mathrm{ft}=\mathrm{Vt}$
Beta=1
p: 1,023785
Asset Value Tree

| 104,2596 | 107,2925 | 110,4137 |
| ---: | ---: | ---: |
|  | 101,3124 | 104,2596 |
|  |  | 98,4485 |

Cash Fow Tree
104,2596 107,2925 110,4137
101,3124 104,2596 98,4485

Debt Service S2

| S2++ | 82,8103 |
| :--- | ---: |
| S2+-=S2-+ | 78,19469 |
| S2-- | 73,83637 |

$B(t=0) \quad 78,19469$

ADDITIONAL SPACE TO ANSWER ANY QUESTION, IF REQUIRED

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SCRAP PAPER

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