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ECONOMICS \&
MANACㅋMㅂNㅍ
Corporate Investment Appraisal
Masters in Finance
2014-2015
Fall Semester
Clara C Raposo
Problem Set ${ }^{0}$ 1:
Basic Concepts of Game Theory (Definition of Equilibrium)
HAND IN SOLUTIONS - CLASS OF OCTOBER 1st, 2014

Problem 1: Compute all the Nash Equilibria of the game "Matching Pennies". Explain your answer.

Problem 2: What are the Nash equilibria of the following game, after elimination of dominated strategies? Explain the steps followed in order to reach your results.

Player B

|  | Left | Center | Right |  |
| :--- | :--- | :---: | :--- | :---: |
| Top | 3,3 | 0,4 | 0,1 |  |
| Player A | Middle | 3,0 | 1,2 | 0,2 |
|  | Bottom | 0,0 | 1,0 | 2,1 |

Problem 3: Two Californian teenagers, Bill and Ted, are playing a game with the following pay-offs matrix:

|  | Ted |  |
| :--- | :--- | :---: |
|  | Left | Right |
| Bill | Top | $-1,-1$ |
| Bottom | 0,0 | 2,2 |

(a) Determine all equilibria in pure strategies. Explain.
(b) Determine all equilibria in mixed strategies. Explain.
(c) What's the probability of both players having positive pay-offs? Explain.

Problem 4: Consider the following coordination game:

|  | Player B |
| :--- | :--- |
| Left | Right |

Top $3,3 \quad-1,-1$

Player A
Bottom $\quad-1,-1 \quad 1,1$
(a) Compute all pure stratregy equilibria of this game. Explain.
(b) Do any of these strategies dominate any of the others? Explain.
(c) Now suppose that Player A plays first, committing to choose either Top or Bottom. Are the strategies of question (a) still Nash equilibria?
(d) What are the "subgame perfect" equilibria of this game?

Problem 5: Consider the previous question's game, in which the players choose their strategies simultaneously.
(a) Represent the game in extensive form.
(b) Describe the perfect Bayesian equilibria (PBE) of this game.

