

3.

$$a) \mathcal{I}_x(k) = (1 - 0.4B)^2 \mathcal{I}_y(k) \quad \text{e} \quad \mathcal{I}_w(k) = (1 - 2.5B)^2 \mathcal{I}_v(k)$$

4.

$$a) Y_t = 2Y_{t-1} - Y_{t-2} + \varepsilon_t - \theta_1 \varepsilon_{t-1} - \theta_2 \varepsilon_{t-2} - \theta_3 \varepsilon_{t-3}$$

$$b) \hat{Y}_t(m) = 2\hat{Y}_t(m-1) - \hat{Y}_t(m-2), \quad m > 3$$

6.

$$\hat{Y}_{49}(1) = 32.6; \quad \hat{Y}_{49}(2) = 33.12; \quad \hat{Y}_{49}(3) = 33.25; \quad \hat{Y}_{49}(4) = 33.28$$

7.

$$a) Y_t = \sum_{j=0}^{\infty} \psi_j \varepsilon_{t-j} \quad \text{con} \quad \psi_0 = 0.3 \quad \text{e} \quad \psi_j = 0.3\psi_{j-1} + 0.6\psi_{j-2}, \quad j > 1$$

$$b) \phi_{11} = 0.75; \quad \phi_{22} = 0.6; \quad \phi_{kk} = 0, \quad k > 3$$

8. a) 20 b) No

9.

$$a) Y_t(1) = 2 - 0.6\varepsilon_t; \quad Y_t(m) = 2, \quad m > 2$$

$$b) \text{Var}(\varepsilon_t(1)) = 0.01; \quad \text{Var}(\varepsilon_t(m)) = 0.0136, \quad m > 2$$

10. See W. Wei (2007, p. 95)

11.

$$a) Y_t = Y_{t-1} + Y_{t-12} - Y_{t-13} + \varepsilon_t - \theta_1 \varepsilon_{t-1} - \theta_2 \varepsilon_{t-12} + \theta_1 \theta_2 \varepsilon_{t-13}$$

$$b) \hat{Y}_{100}(1) = Y_{100} + Y_{89} - Y_{88} - 0.33\hat{\varepsilon}_{100} - 0.82\hat{\varepsilon}_{89} + 0.27\hat{\varepsilon}_{88}$$

$$\hat{Y}_{100}(2) = \hat{Y}_{100}(1) + Y_{90} - Y_{89} - 0.82\hat{\varepsilon}_{90} + 0.27\hat{\varepsilon}_{89}$$

$$\hat{Y}_{100}(3) = \hat{Y}_{100}(2) + Y_{91} - Y_{90} - 0.82\hat{\varepsilon}_{91} + 0.27\hat{\varepsilon}_{90}$$

$$\hat{Y}_{100}(m) = \hat{Y}_{100}(m-1) + \hat{Y}_{100}(m-12) - \hat{Y}_{100}(m-13)$$

$$+ E(\varepsilon_{100+m} | Y_{100}, Y_{99}, \dots) - 0.33 E(\varepsilon_{100+m-1} | \dots) \\ - 0.82 E(\varepsilon_{100+m-12} | \dots) + 0.27 E(\varepsilon_{100+m-13} | \dots)$$