## Production and Operations

## Quiz 1: Version A

## THIS QUIZ HAS DURATION OF EXACTLY ONE HOUR AND THIRTY MINUTES.

Clearly mark your answer with the symbol " $X$ " in the designated column. Wrong or misplaced answers receive 0 points. Pages 9 and 10 have been intentionally left blank and are to be used for ancillary computations.

## Group I

1. Consider the project ISEGNL with network diagram, expected activity durations and standard deviations presented below:


| Activities | A | B | C | D | E | F | G |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Expected <br> duration <br> (days) | 5 | 4 | 3 | 4 | 3 | 6 | 2 |
| Standard <br> deviation <br> (days) | 2 | 1 | 2 | 3 | 1 | 3 | 2 |

[2 val.] Identify the critical path of project ISEGNL.

| 1 |  | $A-E-F-G$ |
| :--- | :--- | :--- |
| 2 |  | A - C - F - G |
| 3 |  | B-C - F - G |
| 4 |  | B - D - G |

[2 val.] If the late start (LS) time for activity $D$ is 10, its Slack (S) is:

| 1 |  | 5 days |
| :--- | :--- | :--- |
| 2 |  | 4 days |
| 3 |  | 1 days |
| 4 |  | 6 days |


| [1 val.] Please consider a new project with expected activity |  |
| :--- | :--- |
| durations and standard deviations identical to those displayed |  |
| in the previous table. Assume now precedencies are different |  |
| from before. If the new critical path is ACDG what is the |  |
| probability that the project duration is lesser than 12 days? |  |
| 1 | 0.7486 |
| 2 | 0.3300 |
| 3 | 0.5432 |
| 4 | 0.2514 |

Consider the following data from project NOW:

| Activities | A | B | C | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Normal <br> time <br> (weeks) | 6 | 5 | 4 | 3 | 5 | 4 | 3 | 3 |
| Crash time <br> (weeks) | 5 | 4 | 2 | 2 | 2 | 4 | 3 | 2 |
| Normal <br> cost <br> (euros) | 1200 | 600 | 1000 | 500 | 600 | 800 | 500 | 800 |
| Crash cost <br> (euros) | 1600 | 700 | 2100 | 950 | 1200 | 800 | 500 | 1100 |

After a network diagram was drawn the following paths were identified:

| ACH |
| :--- |
| BCDE |
| BFGH |
| ACDH |


| val.] Estimate the impact of crashing activity $\mathbf{E}$ by three weeks <br> on the total duration of the project. |  |  |
| :--- | :--- | :---: |
| 1 |  |  |
| 2 |  |  |
| Project duration is shortened by one week |  |  |
| 3 |  |  |
| 4 | Project duration is shortened by two weeks |  |

[2 val.] If the duration of the NOW project is crashed by two weeks what is the minimum total project cost?

| 1 |  | 6550 |
| :--- | :--- | :--- |
| 2 |  | 6450 |
| 3 |  | 6300 |
| 4 |  | 6000 |

## Group II

For the purposes of Group II please consider companies to work 50 weeks per year, and 5 days per week.

| $[1$ | val.] Annual demand for TVPLUS television sets at |
| :--- | :--- |
| ELECTRICA store is of 10000 units. The order cost is of 30 |  |
| euros and the weekly holding cost per unit is 0.50 euros. How |  |
| many orders should ELECTRICA make in a year? |  |
| 1 | 65 orders |
| 2 | 9 orders |
| 3 | 10 orders |
| 4 | 24 orders |

VIGILANTE manufactures surveillance systems, namely the VG1 model, which has an yearly demand of 40000 units. Currently, VIGILANTE has a production capacity of 1000 VG1 units per week, a set-up cost of 100 euros and an yearly holding cost of 10 euros per unit.

| [2 val.] Please identify the correct production order quantity: |  |  |
| :--- | :--- | :--- |
| 1 |  | 894 units |
| 2 |  | 2000 units |
| 3 |  | 1000 units |
| 4 |  | 800 units |


| [2 val.] Assuming ELECTRICA produces a lot size of 3000 units what is the duration of the production phase in which only inventory consumption takes place? |  |
| :---: | :---: |
| 1 | 3.75 weeks |
| 2 | 0.75 weeks |
| 3 | 2.5 weeks |
| 4 | 0.5 weeks |

Weekly demand for wholegrain flour at GOODBUY supermarket follows a Normal distribution with mean of 60 packages and standard deviation of 10 packages. The yearly holding cost of each package is 2 euros. The lead time is 8 weeks. Currently the supermarket owner orders batches of 500 packages.

| [2 val.] Assuming the GOODBUY supermarket owner follows a |
| :--- |
| safety stock of 70 packages, what is the service level provided |
| to the customers? |
| 1 |$\quad$| $99.32 \%$ |  |
| :--- | :--- |
| 2 |  |
| 3 | $95.0 \%$ |
| 4 | $81.06 \%$ |

[2 val.] Assuming the GOODBUY supermarket owner follows a safety stock of 70 packages, what is the yearly holding cost associated with this inventory policy?

| 1 |  | 640 euros/year |
| :--- | :--- | :--- |
| 2 |  | 500 euros/ year |
| 3 |  | 1140 euros/ year |
| 4 |  | 140 euros/ year |

## Group III

The following data was retrieved from the aggregate production plan of ELECTRICA washing machines for the months of May through July:

|  |  |  | Capacity |  |
| :--- | :--- | :--- | :--- | :--- |
| Month | Demand <br> (machines) | Regular <br> time <br> production <br> (machines) | Overtime <br> production <br> (machines) | Subcontracting |
| May | 1000 | 800 | 100 | 50 |
| June | 800 | 700 | 100 | 50 |
| July | 1300 | 1300 | 100 | 50 |

Initial Inventory: 200 machines
Costs:

Regular time Cost
Overtime Cost
Subcontracting Cost
Holding Cost
Backorder Cost

200€ /machine
220€/machine
250€/machine 10€/machine/month 25€/machine/month

Consider the following production plan:

|  |  | May |  | June |  | July |  | a |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Init } \\ & \text { Inven } \end{aligned}$ |  | $200 \quad 0$ |  |  | 10 |  | 20 |  | 200 |
| May | RT1 | $800 \quad 200$ |  |  | 210 |  | 220 |  | 800 |
|  | OT1 |  | 220 | 50 | 230 |  | 240 |  | 100 |
|  | SUB1 |  | 250 |  | 260 |  | 270 |  | 50 |
| June | RT2 |  | 225 | 700 | 200 |  | 210 |  | 700 |
|  | OT2 |  | 245 |  | 220 |  | 230 |  | 100 |
|  | SUB2 |  | 275 |  | 250 |  | 260 |  | 50 |
| July | RT3 |  | 250 | 50 | 225 | 1250 | 200 |  | 1300 |
|  | OT3 |  | 270 |  | 245 | 50 | 220 |  | 100 |



| [1 val.] <br> (respectively): | Flease choose the text/values of cells $\mathbf{a}$ and $\mathbf{b}$ <br> For <br> mul |
| :--- | :--- |
| 1 | Ending Inventory; 350 |
| as |  |

[2 val.] What are the regular time costs, holding costs, and backorder costs for the given production plan in the month June?

| 1 | $140000 ; 11500 ; 11250$ |
| :--- | :--- |
| 2 | $150000 ; 500 ; 1250$ |
| 3 | $150000 ; 0 ; 11250$ |
| 4 | $22750 ; 500 ; 1250$ |

## Inventory Management

## EOQ

$$
Q=\sqrt{\frac{2 D S}{H}} ; \mathrm{N}=\mathrm{D} / \mathrm{Q} ; \quad \mathrm{ROP}=\mathrm{d} \times \mathrm{L} ; \quad \mathrm{TC}=\frac{\mathrm{Q}}{2} \times \mathrm{H}+\frac{\mathrm{D}}{\mathrm{Q}} \times \mathrm{S}+\mathrm{P} \times \mathrm{D}
$$

POQ
$Q=\sqrt{\frac{2 D S}{H\left(1-\frac{d}{p}\right)}}$
$T C=\frac{Q}{2}\left(1-\frac{d}{p}\right) \times H+\frac{D}{Q} \times S+P \times D$
$\mathrm{t}_{\mathrm{p}}=\mathrm{t}_{1}=\frac{\mathrm{Q}}{\mathrm{p}}$
$T=\frac{Q}{D}$
$I_{\text {máx }}=M=Q\left(1-\frac{d}{p}\right)$

$$
\mathrm{SS}=\mathrm{Z}
$$

$$
\mathrm{ROP}={ }_{\mathrm{LT}} \times{ }_{\mathrm{d}}+\mathrm{SS}
$$

$$
\operatorname{ROP}=\mathrm{LT} \times{ }_{\mathrm{d}}+\mathrm{SS}
$$

$$
\begin{gathered}
d L T=\sqrt{\mu_{d}^{2} \times{ }_{\text {LT }}^{2}+{ }_{\text {LT }} \times{ }_{d}^{2}} \\
d L T=\sqrt{L T} \times{ }_{d}
\end{gathered}
$$

$$
\mathrm{ROP}={ }_{\mathrm{LT}} \times \mathrm{d}+\mathrm{SS}
$$

$$
\mathrm{dLT}=\sqrt{\mathrm{d}^{2} \times{ }_{\mathrm{LT}}^{2}}
$$

$=\mathrm{P}(\mathrm{X}>$ ROP $)=$ probability of stockout

$$
T C=\left(\frac{Q}{2}+S S\right) \times H+\frac{D}{Q} \times S+P \times D
$$

## Project Management

$E F=E S+$ Activity time
Expected activity time $=\mathrm{t}=\frac{a+4 m+b}{6}$
Variance of activity completion time $=$

$$
[(b-a) / 6]^{2}
$$

Slack = LS - ES or Slack = LF-
EF

Crash cost per period $=\frac{C C-N C}{N T-C T}$

## The Normal Distribution

## Cumulative Standard Table

| $\mathrm{P}(\mathrm{Z} \leq \mathrm{z})=\Phi(\mathrm{z})$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| 0.0 | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
| 0.1 | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| 0.2 | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| 0.3 | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| 0.4 | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| 0.5 | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
| 0.6 | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
| 0.7 | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
| 0.8 | 0.7881 | 0.7910 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
| 0.9 | 0.8159 | 0.8186 | 0.8212 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
| 1.0 | 0.8413 | 0.8438 | 0.8461 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
| 1.1 | 0.8643 | 0.8665 | 0.8686 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
| 1.2 | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.9015 |
| 1.3 | 0.9032 | 0.9049 | 0.9066 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.9177 |
| 1.4 | 0.9192 | 0.9207 | 0.9222 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.9319 |
| 1.5 | 0.9332 | 0.9345 | 0.9357 | 0.9370 | 0.9382 | 0.9394 | 0.9406 | 0.9418 | 0.9429 | 0.9441 |
| 1.6 | 0.9452 | 0.9463 | 0.9474 | 0.9484 | 0.9495 | 0.9505 | 0.9515 | 0.9525 | 0.9535 | 0.9545 |
| 1.7 | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | 0.9616 | 0.9625 | 0.9633 |
| 1.8 | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
| 1.9 | 0.9713 | 0.9719 | 0.9726 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
| 2.0 | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
| 2.1 | 0.9821 | 0.9826 | 0.9830 | 0.9834 | 0.9838 | 0.9842 | 0.9846 | 0.9850 | 0.9854 | 0.9857 |
| 2.2 | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
| 2.3 | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
| 2.4 | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
| 2.5 | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
| 2.6 | 0.9953 | 0.9955 | 0.9956 | 0.9957 | 0.9959 | 0.9960 | 0.9961 | 0.9962 | 0.9963 | 0.9964 |
| 2.7 | 0.9965 | 0.9966 | 0.9967 | 0.9968 | 0.9969 | 0.9970 | 0.9971 | 0.9972 | 0.9973 | 0.9974 |
| 2.8 | 0.9974 | 0.9975 | 0.9976 | 0.9977 | 0.9977 | 0.9978 | 0.9979 | 0.9979 | 0.9980 | 0.9981 |
| 2.9 | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |
| 3.0 | 0.9987 | 0.9987 | 0.9987 | 0.9988 | 0.9988 | 0.9989 | 0.9989 | 0.9989 | 0.9990 | 0.9990 |


| $\boldsymbol{\alpha}$ | 0.400 | 0.300 | 0.200 | 0.100 | 0.050 | 0.025 | 0.020 | 0.010 | 0.005 | 0.001 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $Z_{\alpha}$ 0.253 0.524 0.842 1.282 1.645 1.960 2.054 2.326 <br> 2.576 3.090        <br> $Z_{\alpha / 2}$ 0.842 1.036 1.282 1.645 1.960 2.240 2.326 2.576 2.807 | 3.291 |  |  |  |  |  |  |  |  |  |

## ANCILLARY COMPUTATIONS

