

## FORMULAE

(following Berk and DeMarzo's "Corporate Finance" sequence)

### GESTÃO FINANCEIRA II / CORPORATE FINANCE II

$$PV(\text{growing perpetuity}) = \frac{C}{r - g} \quad (4.10)$$

$$PV(\text{annuity of } C \text{ for } N \text{ periods with interest rate } r, \text{ growing at rate } g) = C \times \frac{1}{r - g} \left( 1 - \left( \frac{1 + g}{1 + r} \right)^N \right) \quad (4.11)$$

$$\text{Equivalent } n - \text{period discount rate} = (1 + r)^n - 1 \quad (5.1)$$

$$1 + EAR = \left( 1 + \frac{APR}{k} \right)^k \quad (5.3)$$

$$\text{Free Cash Flow} = EBIT(1 - T_C) + \text{Depreciation} - \text{CapEx} - \Delta \text{NWC} \quad (8.5)$$

$$YTM_n = \left( \frac{FV}{P} \right)^{\frac{1}{n}} - 1 \quad (6.3)$$

$$P = CPN \times \frac{1}{y} \left( 1 - \frac{1}{(1 + y)^n} \right) + \frac{FV}{(1 + y)^n} \quad (6.5)$$

$$P = PV(\text{Bond cash Flows}) = \frac{CPN}{1 + YTM_1} + \frac{CPN}{(1 + YTM_2)^2} + \dots + \frac{CPN + FV}{(1 + YTM_N)^N} \quad (6.6)$$

$$f_n = \frac{(1 + YTM_N)^N}{(1 + YTM_{N-1})^{N-1}} - 1 \quad (6A.2)$$

$$(1 + f_1) \times (1 + f_{12}) \times \dots \times (1 + f_n) = (1 + YTM_n)^n \quad (6A.3)$$

$$r_E = \frac{Div_1}{P_0} + \frac{P_1 - P_0}{P_0} \quad (9.2)$$

$$P_0 = \frac{Div_1}{1+r_E} + \frac{Div_2}{(1+r_E)^2} + \dots + \frac{Div_N}{(1+r_E)^N} + \frac{P_N}{(1+r_E)^N} \quad (9.4)$$

$$P_0 = \frac{Div_1}{r_E - g} \quad (9.6)$$

$$Div_t = EPS_t \times \text{Dividend Payout Rate}_t \quad (9.8)$$

$$g = \text{Retention rate} \times \text{Return on New Investment} \quad (9.12)$$

$$P_0 = \frac{PV(\text{Future Total Dividends and Repurchases})}{\text{Shares Outstanding}_0} \quad (9.16)$$

$$\text{Expected Return} = E(R) = \sum_R p_R \times R \quad (10.1)$$

$$Var(R) = E \left[ (R - E(R))^2 \right] = \sum_R p_R \times (R - E(R))^2 ; \quad SD(R) = \sqrt{Var(R)} \quad (10.2)$$

$$\bar{R} = \frac{1}{T} (R_1 + R_2 + \dots + R_T) = \frac{1}{T} \sum_{t=1}^T R_t \quad (10.6)$$

$$Var(R) = \frac{1}{T-1} \sum_{t=1}^T (R_t - \bar{R})^2 \quad (10.7)$$

$$x_i = \frac{\text{value of investment } i}{\text{total value of portfolio}} \quad (11.1)$$

$$E(R_p) = \sum_i x_i E(R_i) \quad (11.3)$$

$$cov(R_i, R_j) = E[(R_i - E(R_i))(R_j - E(R_j))] \quad (11.4)$$

$$cov(R_i, R_j) = \frac{1}{T-1} \sum_t (R_{i,t} - \bar{R}_i)(R_{j,t} - \bar{R}_j) \quad (11.5)$$

$$corr(R_i, R_j) = \frac{cov(R_i, R_j)}{SD(R_i)SD(R_j)} \quad (11.6)$$

$$\begin{aligned} Var(R_p) &= x_1^2 Var(R_1) + x_2^2 Var(R_2) + 2x_1 x_2 cov(R_1, R_2) = \\ &= x_1^2 Var(R_1) + x_2^2 Var(R_2) + 2x_1 x_2 corr(R_1, R_2) SD(R_1) SD(R_2) \end{aligned} \quad (11.8 \text{ and } 11.9)$$

$$Sharpe Ratio = \frac{\text{Portfolio Excess Return}}{\text{Portfolio Volatility}} = \frac{E(R_p) - r_f}{SD(R_p)} \quad (11.17)$$

$$\beta_i^p = \frac{SD(R_i)corr(R_i, R_p)}{SD(R_p)} \quad (11.19)$$

$$E(R_i) = r_i = r_f + \beta_i \times (E[R_{Mkt}] - r_f) \quad (11.22)$$

$$\beta_p = \frac{cov(R_p, R_{Mkt})}{Var(R_{Mkt})} = \sum_i x_i \beta_i \quad (11.24)$$

$$r_d = y - pL \quad (12.7)$$

$$r_u = \frac{E}{E+D} r_E + \frac{D}{E+D} r_D = Pre-tax WACC \quad (12.8), (14.6), (18.6)$$

$$\beta_U = \frac{E}{E+D} \beta_E + \frac{D}{E+D} \beta_D \quad (12.9), (14.8)$$

$$r_{WACC} = \frac{E}{E+D} r_E + \frac{D}{E+D} r_D (1 - T_C) \quad (12.12), (18.1)$$

$$r_E = r_u + \frac{D}{E} (r_u - r_D) \quad (14.5), (18.10)$$

$$\beta_E = \beta_U + \frac{D}{E} (\beta_U - \beta_D) \quad (14.9)$$

$$\tau^* = 1 - \frac{(1 - T_C)(1 - T_E)}{(1 - T_i)} \quad (15.7)$$

$$\tau_{ex}^* = \frac{T_E - T_i}{1 - T_i} \quad (15.9)$$

$$\begin{aligned} V^L &= V^U + PV(\text{Interest Tax Shield}) - PV(\text{Financial Distress Costs}) - PV(\text{Agency Costs of Debt}) \\ &\quad + PV(\text{Agency Benefits of Debt}) \end{aligned} \quad (16.3)$$

$$Net Borrowing Date t = D_t - D_{t-1} \quad (18.8)$$

$$FCFE = FCF - (1 - T_C) \times Interest Payments + Net Borrowing \quad (18.9)$$