



## FIXED INCOME PRODUCTS AND MARKETS

### *III – Fixed Income Derivatives and Models*

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### **III – Fixed Income Derivatives and Models**

1. Swaps, Fra's and Short Term Interest Rate Futures
2. Bond Futures
3. Credit Spread Dynamics
4. Bonds with embedded options and Bond Options
5. Futures Options, Caps, Floors and Swaptions
6. Exotic Options and Credit Derivatives



## 6. Exotic Options and Credit Derivatives



### 6.1 Interest-Rate Exotic Options



- Interest-rate exotic options usually are

- *Path-dependent*
- *Correlation-dependent*
- *Time-dependent*

#### - **Path-dependent options**

option payoffs are a function of the path that interest rates follow over the option life

#### - **Correlation-dependent options**

option payoffs are based on the relationship between several interest rates

#### - **Time-dependent options**

the buyer has the right to choose an option characteristic as a function of time



## Barrier Caps and Floors



- **Up-and-in barrier cap:** this cap is activated when the reference rate reaches or goes above the barrier during a certain period of time (American style) or is equal or above the barrier at expiry (European style)

- **Up-and-out barrier cap:** cap is deactivated when the reference rate reaches or goes above the barrier during a certain period of time (American style) or is equal or above the barrier at expiry (European style)

- **Down-and-in barrier floor:** this floor is activated when the reference rate reaches or falls below the barrier (American style) or is equal or below the barrier at expiry (European style)

- **Down-and-out barrier floor:** this floor is deactivated when the reference rate reaches or falls below the barrier (American style) or is equal or below the barrier at expiry (European style)

Note that the barrier level is higher (lower) than the strike price for the caps (floors)



## Bounded Caps e Floors



**Bounded Caps e Floors (B-Caps e B-Floors)** – are caps and floors whose payout is limited to a particular amount of money

### Cancelable Swaps

A callable (puttable) swap is a structure where the fixed-rate payer (receiver) of a swap buys a receiver (payer) swaption, so that it has the right to cancel the swap at maturity (European style) or at some specified dates during the swap life (Bermudan style)

### Captions e Floortions

Caption – is an option that gives the buyer the right to buy or sell a cap at the maturity date and for a specified premium

Floortion – is an option that gives the buyer the right to buy or sell a floor at the maturity date and for a specified premium



### *Contingent Premium Caps e Floors*



A contingent premium cap (floor) is a standard cap (floor) where the buyer pays a smaller premium than for a cap (floor), but may have to pay an additional premium if the reference rate goes above (below) a specified contingent level on any one reset date

### *Extendible Swaps*

An extendible swap is a plain-vanilla swap where one party has the right at a determined date, or at several future dates, to extend the swap maturity for a specified period

### *Incremental Fixed Swap*

It's a swap the fixed part can be transformed into a combination of fixed and variable part, depending on the value assumed by the floating rate. When the floating rate decreases, the proportion of the variable component also decreases



### *Choosercaps and Flexicaps-and-Floors*



Choosercaps (floors) and flexicaps (floors) offer the buyer a maximum (minimum) interest rate for a limited number  $n$  of caplets (floorlets) and not for all the caplets (floorlets) that constitute the cap (floor)

With a flexicap (floor), the guaranteed maximum (minimum) rate applies to the first  $n$  number of fixings that are greater than the strike rate (after which no more protection)

With a choosercap (floor), the buyer decides to exercise  $n$  caplets (floorlets) in the money amongst all the caplets (floorlets) in the money



## 6.2 Credit Derivatives



Credit derivatives can be defined as arrangements that allow one party (protection buyer or originator) to transfer credit risk of a reference asset, which it may or may not own, to one or more other parties (the protection sellers)

### Tipology

1. Credit Default Derivatives (designed as hedging vehicles for default risk)
  - Credit Default Swap (CDS)
  - Credit Linked Notes (CLN)
2. Credit Spread Derivatives (based on differences in creditworthiness)
  - Credit Spread Forward
  - Credit Spread Options
3. Products that synthetically replicate the performance of the underlying
  - Total Return Swap



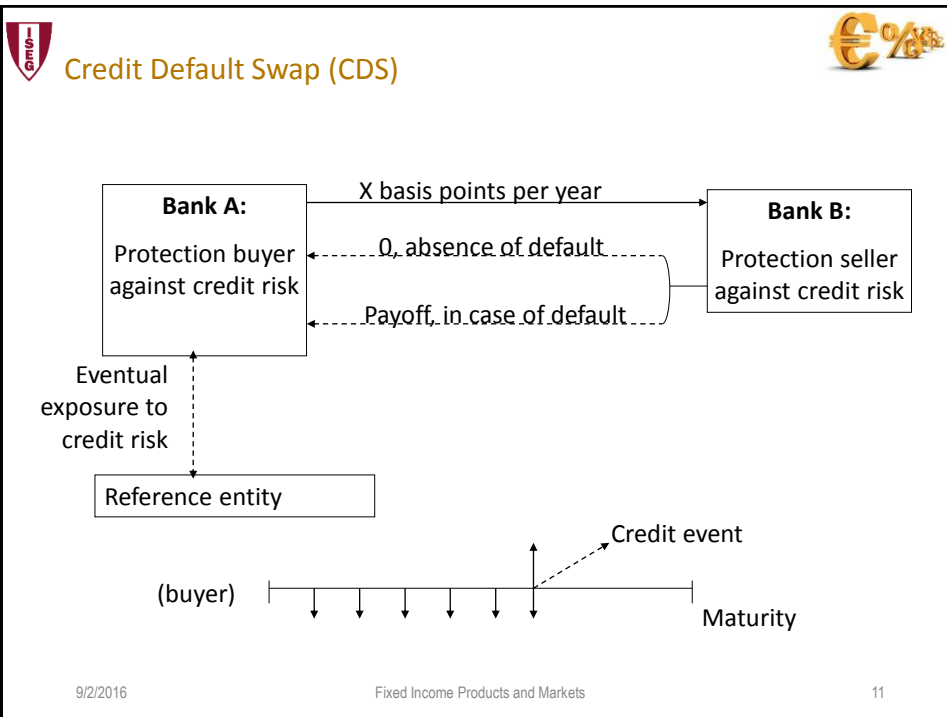
## Credit Default Swap (CDS)



Allows to transfer synthetically the credit risk of a reference entity

The CDS buyer (the protection buyer) pays a periodic premium to the CDS seller (the protection seller), in return the CDS seller will make a payment to the CDS buyer upon the happening of a specified credit event

*Building block of the credit derivatives market*



- Credit Default Swap (CDS) – contract elements**
- Reference Entity – Exact name of the entity against which we want to hedge or assume the credit risk
  - Obligations – Definition of the obligations over which we can observe a credit event. ISDA\* definitions
    - *Payment* – covers all payments (present and futures) of the RE
    - *Borrowed Money* – financial debt of the RE
    - *Bond or Loan*
    - *Bond Only*; - *Loan Only*; - *Reference Obligation Only*
  - Credit Events – Credit event definitions - ISDA\*:
    - Bankruptcy
    - Failure to pay
    - Restructuring
    - Obligation acceleration
    - Repudiation/Moratorium (for sovereign risk)
- \*International Swaps and Derivatives Association
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## Credit Default Swap (CDS) – contract elements



- Settlement

- Physical

The buyer delivers to the seller the bond of the RE (*Deliverable Obligations*) in return e receives the notional value

- Cash

The seller pays to the buyer par value (100%) less the post-default bond observed value

- Fixed pay-out

The seller pays a pre-determined fraction of par value



## Credit Default Swap (CDS) – pricing



$$PV(\text{premiums}) = \sum_{j=1}^n Z(0, T_j) (1 - Q(0, T_j)) \delta_j S_n$$

$$PV(\text{protection}) = \sum_{j=1}^n Z(0, T_j) (Q(0, T_j) - Q(0, T_{j-1})) (1 - X)$$

$Z(0, T_j)$  - Discount factor (risk-free)

$1 - Q(0, T_j)$  - Survival probability until  $T_j$ , for the reference entity

$\delta_j$  - Premium fraction received at date  $T_j$

$(Q(0, T_j) - Q(0, T_{j-1}))$  - Default probability between  $T_{j-1}$  e  $T_j$

$X$  - Recovery rate

$S_n$  - Premium of CDS with maturity at  $T_n$

Note: accrued premium is not considered



## Credit Default Swap (CDS) – pricing



CDS value for the protection buyer:

$$\begin{aligned}
V^{CDS}(0, T_n) &= PV(\text{protection}) - PV(\text{premiums}) \\
&= \sum_{j=1}^n Z(0, T_j) (Q(0, T_j) - Q(0, T_{j-1})) (1 - X) \\
&\quad - \sum_{j=1}^n Z(0, T_j) (1 - Q(0, T_j)) \delta_j S_n
\end{aligned}$$

The premium,  $S_n$ , is established so as to make the CDS value equal zero:

$$S_n = \frac{\sum_{j=1}^n Z(0, T_j) (Q(0, T_j) - Q(0, T_{j-1})) (1 - X)}{\sum_{j=1}^n Z(0, T_j) (1 - Q(0, T_j)) \delta_j}$$

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## Credit Default Swap (CDS) – pricing



Example:

Maturity: 1 year

Quarterly payments ( $\delta_j = 0,25$ )

Recovery rate: 40% ( $X = 0,4$ )

$T_j$ (years)	$Z(0, T_j)$	$1 - Q(0, T_j)$	$\frac{Q(0, T_j) - Q(0, T_{j-1})}{Q(0, T_{j-1})}$	$(1 - X)$	CF act * Prob	$(0,25) * (2) * (3)$
0,25	0,99628	0,99253	0,00747	0,6	0,004466	0,247209
0,5	0,99161	0,98511	0,00742	0,6	0,004412	0,244212
0,75	0,98671	0,97775	0,00736	0,6	0,004358	0,241189
1	0,98039	0,97045	0,00731	0,6	0,004297	0,237854
					<b>0,017534</b>	<b>0,970464</b>

$$S = \frac{0,017534}{0,970464} = 0,01807 \quad S = 181 \text{ bp}$$

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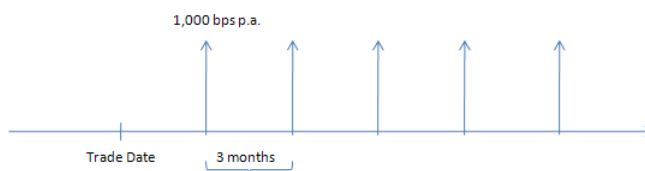


## Credit Default Swap (CDS) – pricing

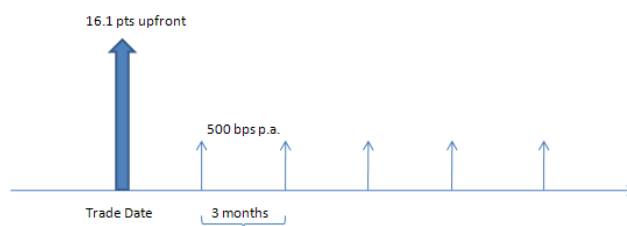


Running CDS Spread vs Upfront CDS with fixed Running Spread

### CDS with Running Spread



### CDS with Upfront Fee + Running Spread



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## Credit Linked Notes (CLN)



Corresponds to the CDS financed version

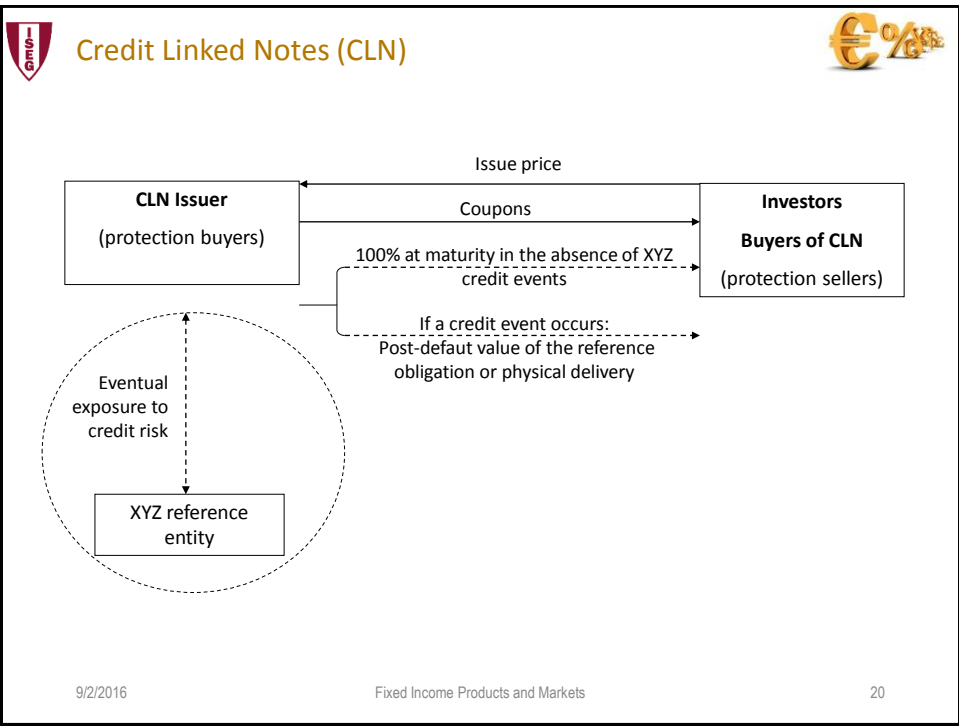
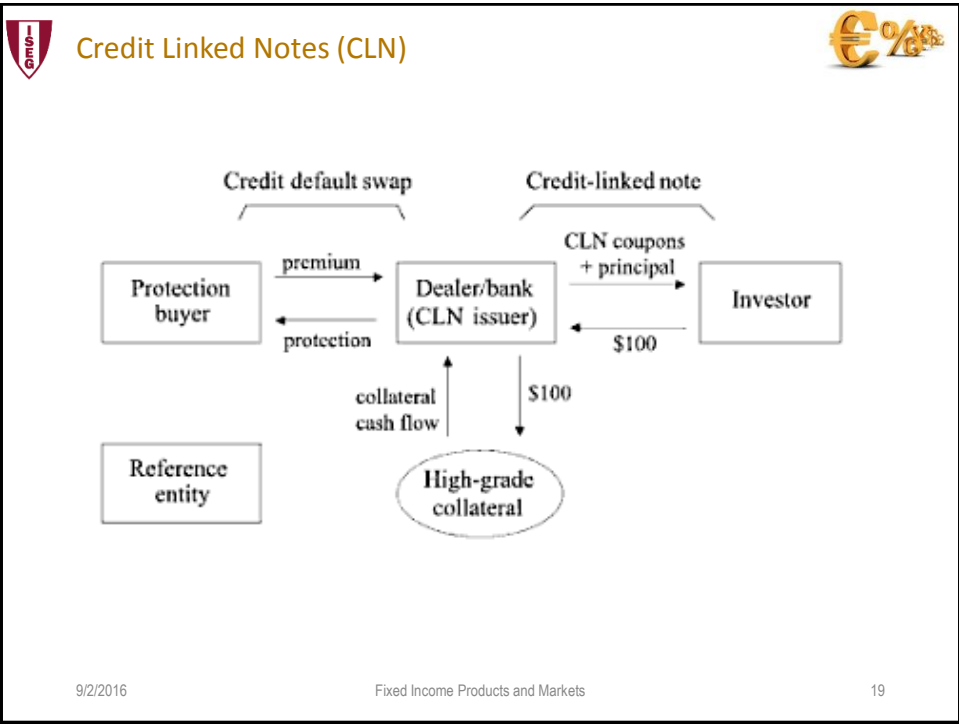
It's a bond whose coupon and notional redemption payments are conditional to the absence of credit events

Allows the buyer to take a bond position of the reference entity

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## Total Return Swap (TRS)



Allows to transfer the full economic result of financial security for a given period of time

