



LISBON  
SCHOOL OF  
ECONOMICS &  
MANAGEMENT

UNIVERSIDADE DE LISBOA

# Economics II

Lecture 05

2018/2019, 2nd semester

# Lecture 05

## 3. Economic Growth, Productivity and Living Standards

### 3.1. Economic growth and living standards ; empirical analysis

#### 3.2. The importance of the growth rate

#### 3.3. The crucial role of average labor productivity

### Readings:

Frank, R. and Bernanke, B. (2011, Brief Ed.), *Principles of Macroeconomics*, McGraw-Hill. Chapter 7

Louçã, Caldas (2010), Ch 9

## After this lecture the student should be able to:

- ✓ recognize industrialization as a time of unparalleled economic growth
- ✓ Understand the concept of real convergence
- ✓ Define and calculate growth rates
- ✓ Understand why accumulated small differences in growth rates have a very large impact on value
- ✓ Understand the crucial role of average labor productivity on determinant of GDP per capita growth rate.

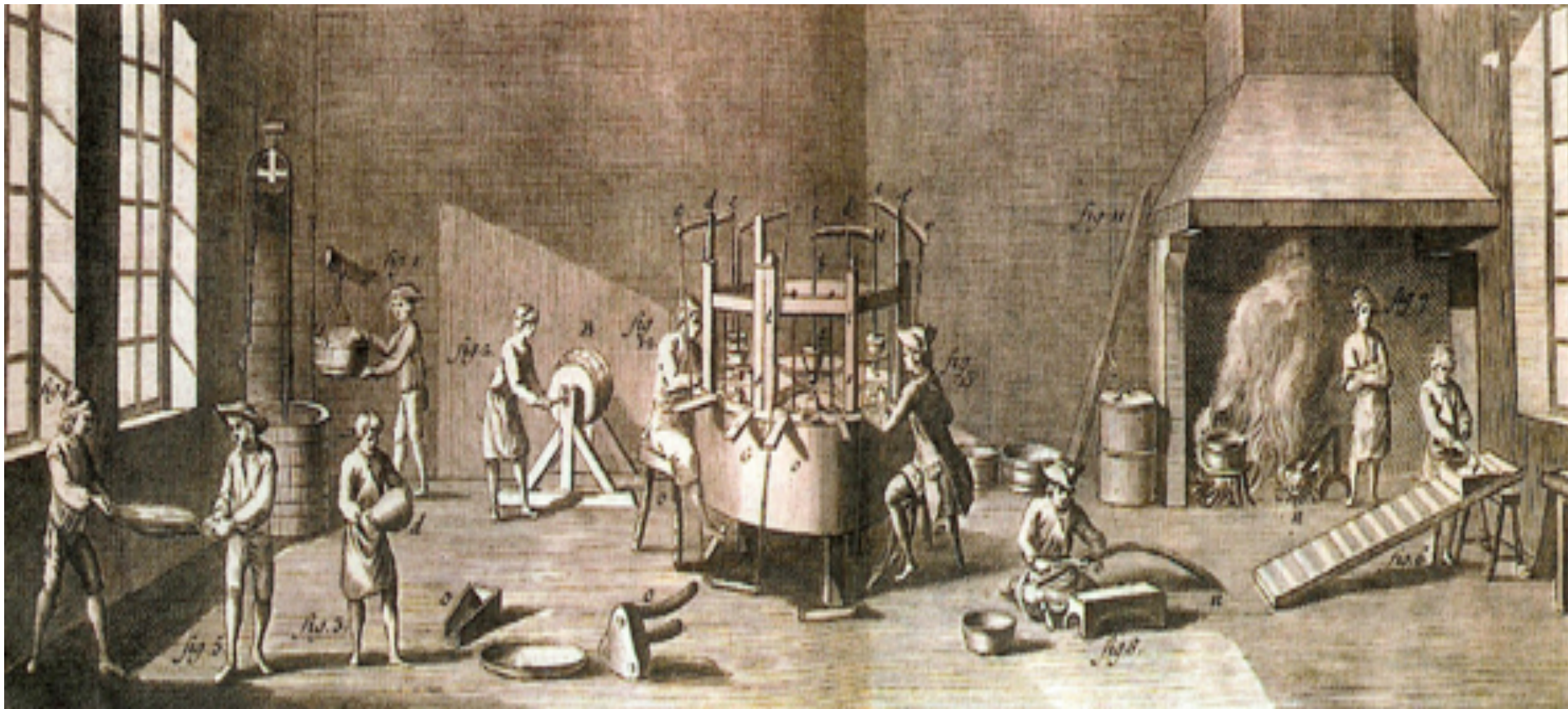
# **3. Economic Growth, Productivity and Living Standards**

## 3.1. Economic growth and living standards - empirical analysis

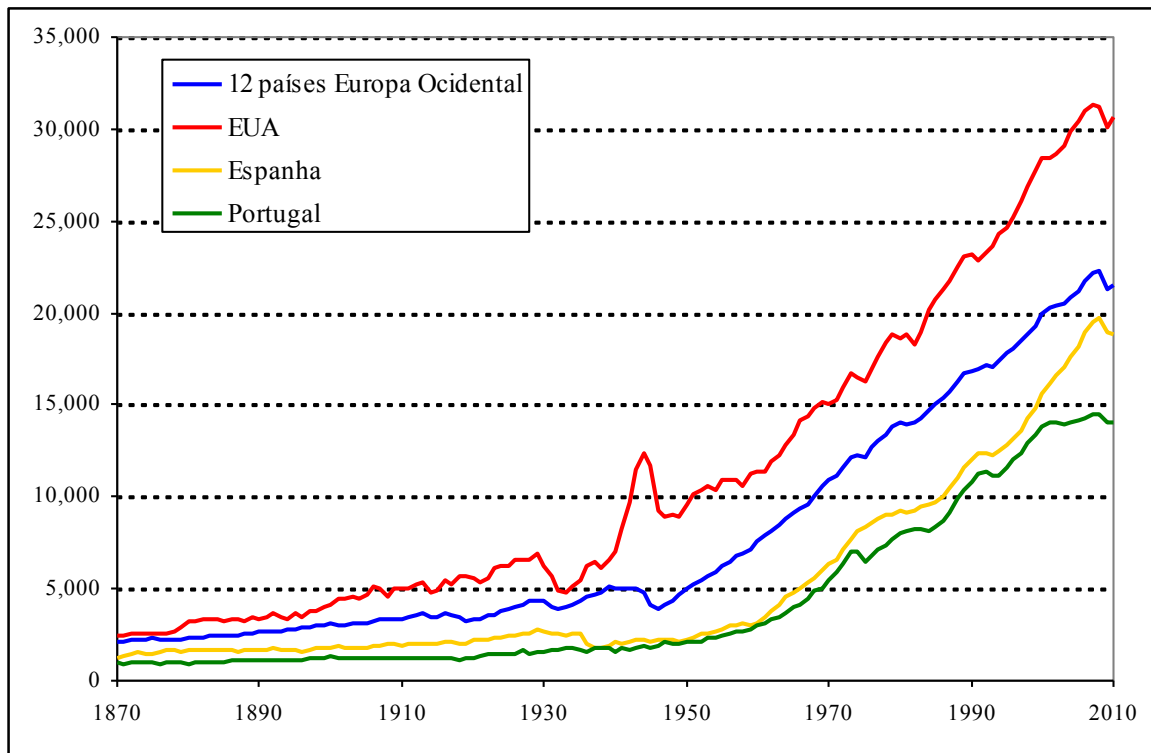
- During the last two centuries there was a dramatic increase on living standards in industrialized countries,
- The real GDP per capita mirrors that increase:
  - It measures the volume of final goods and services available for a average resident in a country during a certain period.

# Adam Smith and the industrial revolution in the UK

The pin factory (“The Wealth of Nations”, 1774)



# PORTUGAL and U.S. Real per capita GDP (1990 prices, international dollars Geary-Khamis )



- Legend:
- 12 European countries (\*)**
  - US**
  - Spain**
  - Portugal**
  - (\*)
  - Germany
  - Austria
  - Belgium
  - Denmark
  - Finland
  - France
  - Netherlands
  - Italy
  - Norway
  - UK
  - Sweden
  - Switzerland

Sources: European Commission (2012) and GGDC (2012)

## PORTUGAL and U.S. Real per capita GDP (1990 prices, international dollars Geary-Khamis )

- On the Figure, GDP per capita is measured in *real* and *international* terms.
  - *Real* (“1990 dollars”) , because price level changes across time;
  - “*International* dollars” (Geary-Khamis: Roy Geary, 1958 & Hanna Khamis, 1970) because the prices change across countries, even when measured using the same currency.



**During last two centuries the Portuguese per capita GDP :**

- had a dramatic increase
- in 2011 value = approximately 15 x 1820
- it was always less than Western Europe, Spain and US per capita GDP .

## **Real convergence**

- approximation of the average standard of living in Portugal in terms of living standards that characterizes richer economies (e.g. Western Europe, USA).

# Real Convergence

**Real convergence can be measured by 2 ways:**

- analyzing the average annual growth rate;
- analyzing the relative per capita GDP.

**Convergence period :**

- depends on the difference between the Portuguese growth rate and the US and Europe growth rate;
- between 1950 and 2001 the Portuguese growth rate was higher than US and Europe

# Average annual growth rate of per capita GDP, before the recession

	1820-1850	1850-1870	1870-1913	1913-1950	1950-1979	1979-2001	2001-2011
Portugal	0.0%	0.3%	0.6%	1.4%	4.6%	2.7%	-0.1%
12 Oc Europe	1.0%	1.2%	1.3%	0.8%	3.6%	1.7%	0.8%
US	1.2%	1.5%	1.8%	1.6%	2.4%	1.9%	0.8%
SPAIN	0.2%	0.6%	1.2%	0.2%	5.0%	2.7%	1.5%

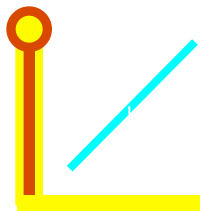
Sources: European Commission (2012) and GGDC (2012)

- **In period 1950-2001** the per capita GDP of Portugal was closer the richer countries.

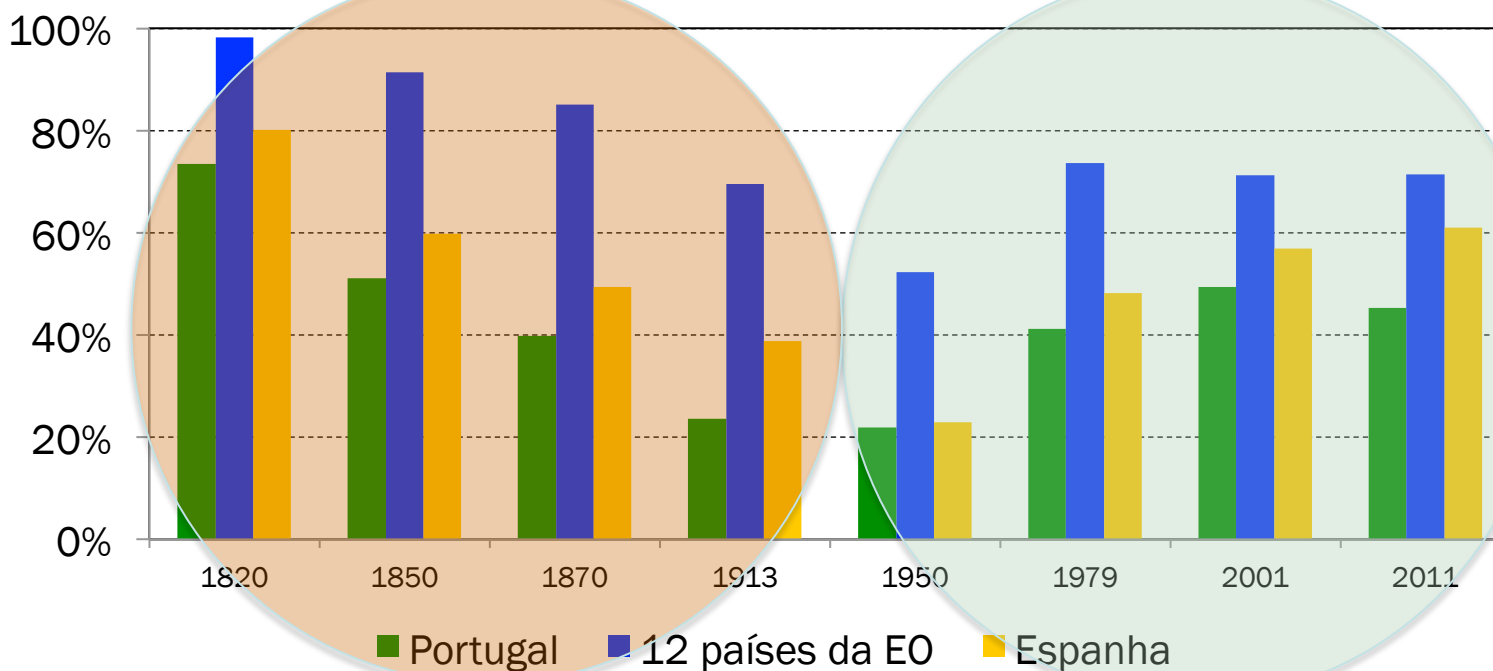
- This happened, because the Portuguese per capita GDP growth rate was higher (compared with other economies)

- **In period 2001-2011**, the Portuguese per capita GDP moved away from the per capita GDP of the richest countries.

- This happened because the Portuguese per capita GDP had a slightly decrease , despite the richer countries per capita GDP have grown slightly
- This is considered a ‘lost decade’ in the Portuguese growth .



## PIB por Habitante em Proporção do dos EUA



Fontes: [Comissão Europeia \(2012\)](#) e [GGDC \(2012\)](#)



## 3.3. The importance of growth rate

What is the annual growth rate (of a variable  $y$ )?

$y_t$  = is the value at year  $t$

$y_{t-1}$  = is the value at year  $t-1$

$\Delta y_t = y_t - y_{t-1}$  = is the change on year  $t$

Annual growth rate is computed as:

$$g_{y,t} = \frac{\Delta y_t}{y_{t-1}}$$

From the previous relation:

$$y_t = (1 + g_{y,t}) \cdot y_{t-1}$$

Therefore, by replacing successive we have:

$$\begin{aligned} y_t &= (1 + g_{y,t}) \cdot (1 + g_{y,t-1}) \dots (1 + g_{y,t-n+1}) \cdot y_{t-n} = \\ &= y_{t-n} \cdot \prod_{s=0}^{n-1} (1 + g_{y,t-s}) \end{aligned}$$

- $n$  is the number of years between  $t$  and  $t-n$
- $t$  is the last year;  $t-n$  is the initial year

The same final end (final) value  $y_t$  can be obtained from the same initial value ( $y_{t-n}$ ) if the variable had grown at a constant growth rate  $g_y$ .

(Initial value  $y_{t-n}$  and final value  $y_t$ )

$$y_t = y_{t-n} \cdot \prod_{s=0}^{n-1} (1 + \bar{g}_y) = (1 + \bar{g}_y)^n \cdot y_{t-n}$$



Consequently, solving in order to  $g_y$ :

$$\bar{g}_y = \left( \frac{y_t}{y_{t-n}} \right)^{\frac{1}{n}} - 1 = \sqrt[n]{\frac{y_t}{y_{t-n}}} - 1$$

This growth rate is called Average Growth Rate of variable  $y$  in period between  $t-n$  and  $t$ .

Observation: This is different from the simple arithmetic mean of the rates for each year ( a wrong way of computing growth rate).

# Small differences in average growth rates have large effects in the long run

To double GDPpcapita in:	The required average growth rate must be equal to:
5 years	14.9%
10 years	7.2%
<b>15 years</b>	<b>4.7%</b>
20 years	3.5%
<b>25 years</b>	<b>2.8%</b>
30 years	2.3%
40 years	1.7%
50 years	1.4%
60 years	1.2%
70 years	1.0%


### 3.3. The importance of average labor productivity

The average labor productivity is measured as the created value (at constant prices) by units of labor allocated.

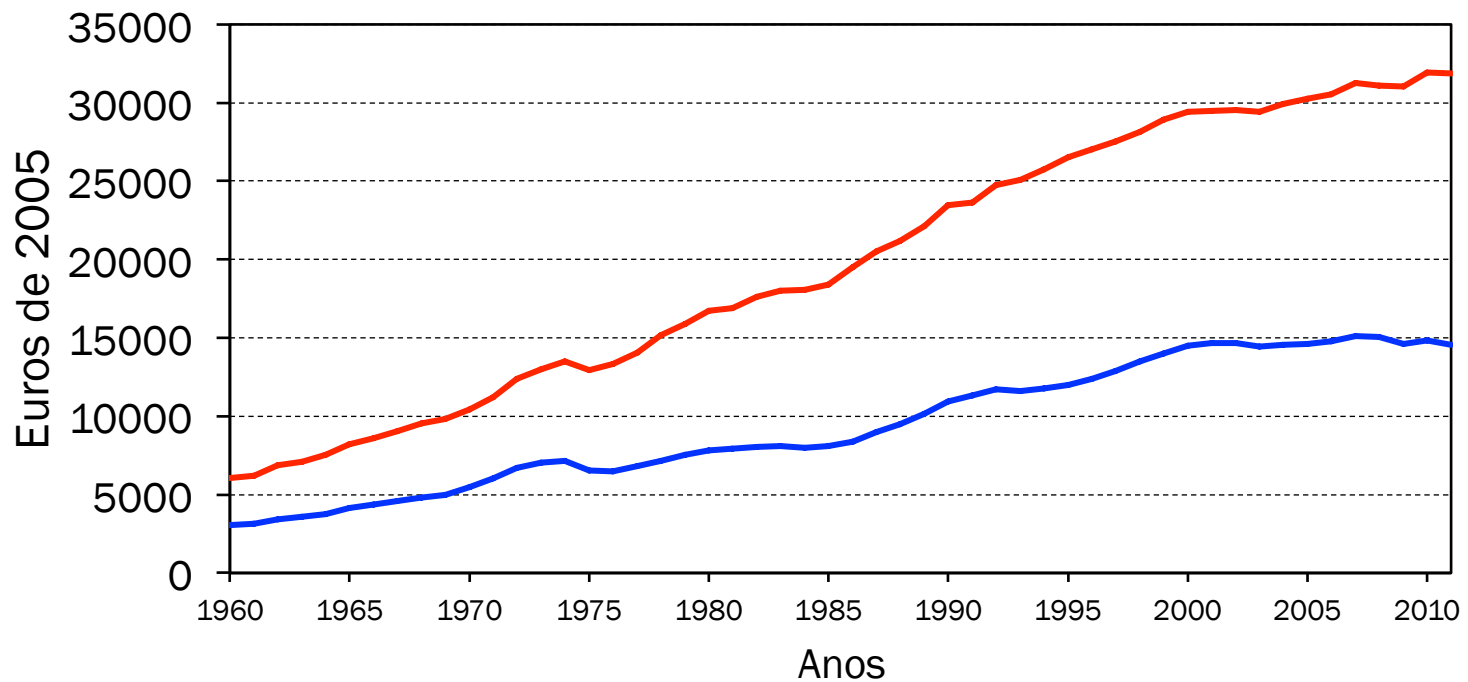
- A first approach is to compute to a country  $X$  and during a period  $t$ :

$$PMeL_t = \frac{Y_t}{N_t}$$

- Where  $N$  represents the Employment (stock) in the period.
- It would be better to measure  $N$  as the number of hours worked (flow), but it is difficult obtain them.



## PIB Real Anual por Habitante e por Trabalhador em Portugal: 1960-2011



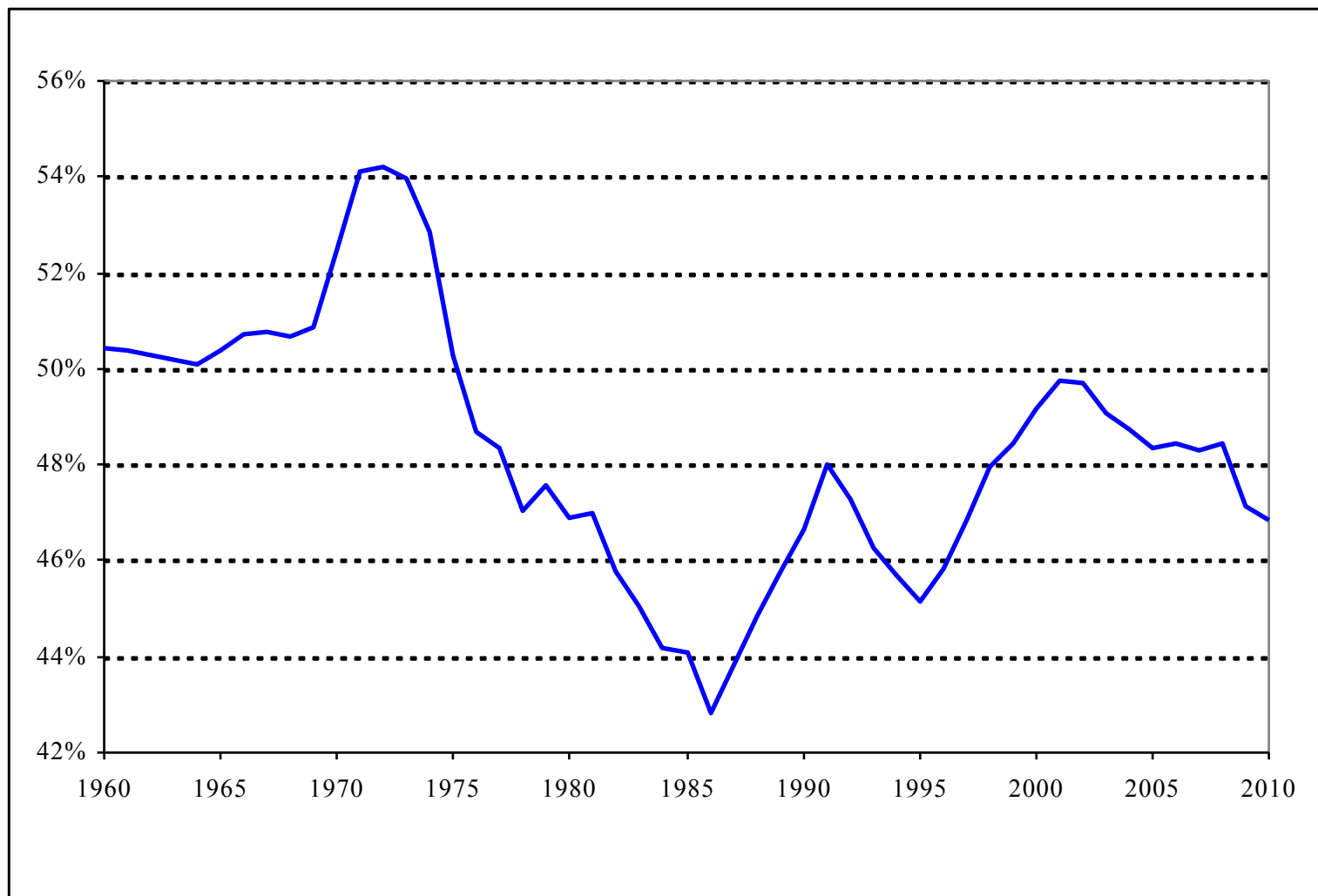
— PIB real per capita

— PIB real por trabalhador

Fonte: [Comissão Europeia \(2012\)](#)



# Share of the Portuguese Population Employed in Total Population Portugal 1960 - 2010



Source: [European Commission \(2012\)](#)

- The real per capita GDP can be represented as the product of multiplying two factors:

the average labor productivity

the percentage of the population that is working

$$\frac{Y_t}{POP_t} = \underbrace{\frac{Y_t}{N_t}}_{\text{PMeL}_t} \times \frac{N_t}{POP_t}$$

Average Labor Productivity

## Real per capita GDP increases if :

- average labor productivity increases;
- the percent of the population that is working increases.

### – In the long run:

- increases in output per person arise mainly from increases in average labor productivity.