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UNIVERSIDADE DE LISBOA

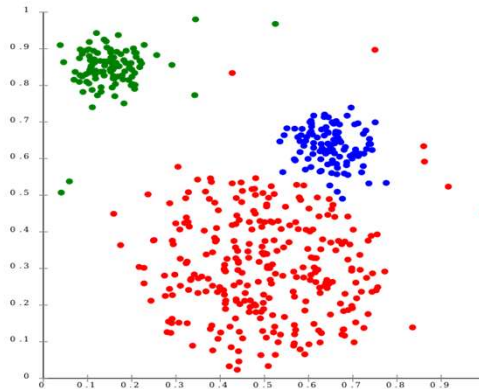
Carlos J. Costa

CLUSTERS ANALYSIS



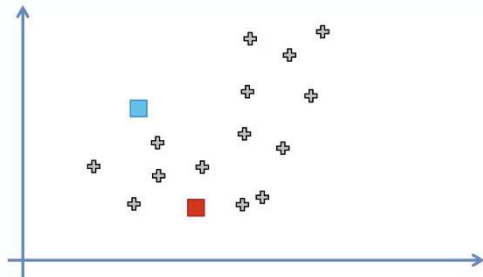
Cluster Analysis

- Cluster analysis is a multivariate method
- aims to classify a sample of subjects (or objects) into several different groups such that similar subjects are placed in the same group
- based on a set of measured variables



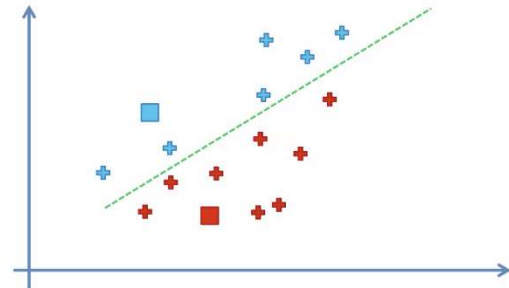
K-means Clustering

- 1. Select K (i.e. 2) random points as cluster centres called centroids

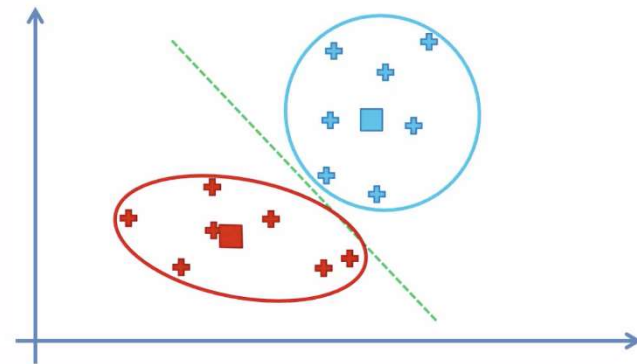
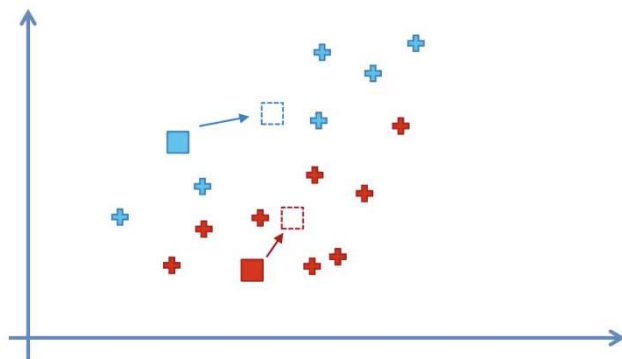


- 2. Assign each data point to the closest cluster by calculating its distance with respect to each centroid

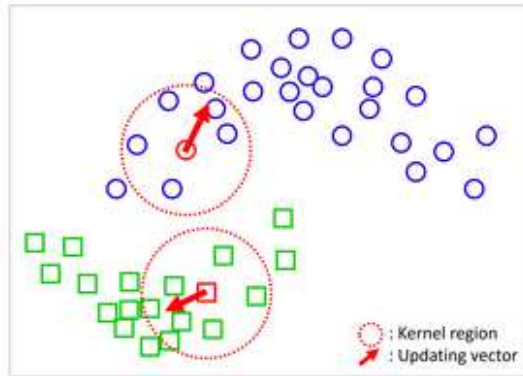
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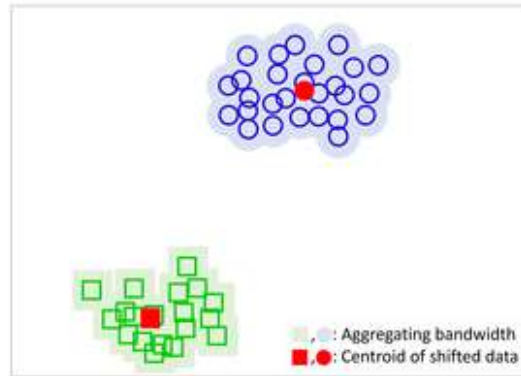
- 3. Determine the new cluster centre by computing the average of the assigned points



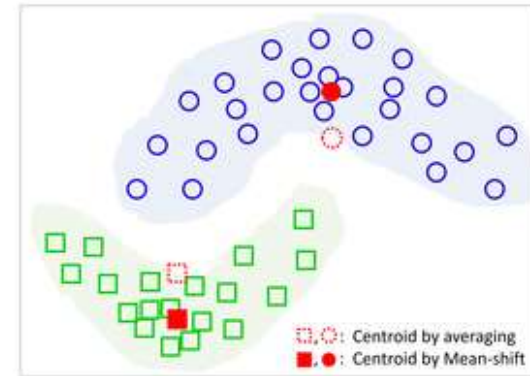
Means Shift Clustering



Updates (shifts) all data point toward high density region until all the points converge



Aggregate the nearby shifted data points into a cluster whose centroid is their average



Assign the original data into the according clusters, But keep the centroid calculated with shifted data

WCSS

- Within-Cluster-Sum-of-Squares (WCSS)- Implicit **objective function in k-Means** measures sum of distances of observations from their cluster centroids.

$$WCSS = \sum_{i \in n} (X_i - Y_i)^2$$

Y_i is centroid for observation X_i .

- Given that k-Means has no in-built preference for right number of clusters, following are some of the common ways k can be selected:
 - Domain Knowledge
 - Rule of Thumb
 - Elbow-Method using WCSS
 - Cluster Quality using Silhouette Coefficient

