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- dimensionality reduction seek and exploit the inherent structure in the data,
- unsupervised learning



- Feature Extraction
- Feature Selection



- Feature Extraction
 - PCA (principal Components analysis)
 - LDA (Linear Discriminant Analysis)
 - NMF (Non-negative Matrix Factorization)
 - TSVD (Truncate Singular Value Decomposition)



PCA

- Principal Component Analysis, or PCA, is a dimensionality-reduction method
- It is often used to reduce the dimensionality of large data sets
- The purpose is transforming a large set of variables into a smaller
- Containing most of the information in the large set.
- When data is linearly inseparable using PCA extension using kernels



PCA

- Standardization
- Covariance Matrix computation.
- Compute the eigenvectors and eigenvalues of the covariance matrix to identify the principal components
- Feature Vector
- Recast the Data Along the Principal Components Axes



```
1 # Load libraries
```

```
2 from sklearn import datasets
```

```
3 from sklearn.decomposition import PCA
```

```
1 # Load the Iris flower dataset:
2 iris = datasets.load_iris()
3 X = iris.data
4 y = iris.target
```

```
1 # Create an PCA that will reduce the data down to 2 feature
2 PCAModel = PCA(n_components=2)
3 
4 # run an PCA and use it to transform the features
5 XPCA = PCAModel.fit(X).transform(X)
```

```
1 # Print the number of features
2 print('Original number of features:', X.shape[1])
3 print('Reduced number of features:', XPCA.shape[1])
```

Original number of features: 4 Reduced number of features: 2

```
1 ## View the ratio of explained variance
```

```
2 PCAModel.explained_variance_ratio_
```

```
array([0.92461621, 0.05301557])
```



LDA

- Linear Discriminant Analysis (LDA)
- Is a linear transformation techniques that is commonly used for dimensionality reduction (like PCA)
- Reducing features by maximizing class separation



```
1 # Load libraries
```

```
2 from sklearn import datasets
```

3 **from** sklearn.discriminant_analysis **import** LinearDiscriminantAnalysis

```
1 # Load the Iris flower dataset:
2 iris = datasets.load_iris()
3 X = iris.data
```

4 y = iris.target

1 # Create an LDA that will reduce the data down to 1 feature

```
2 ldaModel = LinearDiscriminantAnalysis(n_components=2)
3
```

```
4 # run an LDA and use it to transform the features
```

5 XLda = ldaModel.fit(X, y).transform(X)

1 # Print the number of features
2 print('Original number of features:', X.shape[1])
3 print('Reduced number of features:', XLda.shape[1])

```
Original number of features: 4
Reduced number of features: 2
```

1 ## View the ratio of explained variance
2 ldaModel.explained variance ratio

```
array([0.99147248, 0.00852752])
```



)

NMF

- Non-negative Matrix Factorization
- Performs matrix factorization
- It can be applied for:
 - Recommender Systems,
 - Collaborative Filtering
 - topic modelling
 - dimensionality reduction.
- Does not provides the explained variance



NMF

1 # Load libraries

- 2 from sklearn import datasets
- 3 from sklearn.decomposition import NMF

1 # Load the Iris flower dataset: 2 iris = datasets.load_iris() 3 X = iris.data

1 # Create an NMF that will reduce the data down to 2 feature 2 NMFModel = NMF(n_components=2) 3 4 # run an LDA and use it to transform the features 5 XNMF = NMFModel.fit(X).transform(X) 6 7 # Print the number of features 8 print('Original number of features:', X.shape[1]) 9 print('Reduced number of features:', XNMF.shape[1])



.

:

2

TSVD

- Truncate Singular Value Decomposition
- Used in sparce feature matrix



TSVD

```
1 # Load libraries
```

- 2 from sklearn.preprocessing import StandardScaler
- 3 from sklearn.decomposition import TruncatedSVD
- 4 from scipy.sparse import csr matrix
- 5 from sklearn import datasets
- 6 import numpy as np

```
1 # Load the data
2 digits = datasets.load_digits()
3 # Standardize the feature matrix
4 X = StandardScaler().fit transform(digits.data)
```

- 5 # Make sparse matrix
- 6 X sparse = csr matrix(X)

1 # Create a TSVD
2 tsvdModel = TruncatedSVD(n components=10)

```
1 # Conduct TSVD on sparse matrix
2 X_sparse_tsvd = tsvdModel.fit(X_sparse).transform(X_sparse)
```

```
1 # Show results
2 print('Original number of features:', X_sparse.shape[1])
3 print('Reduced number of features:', X_sparse tsvd.shape[1])
```

```
Original number of features: 64
Reduced number of features: 10
```

1 # Sum of first three components' explained variance ratios
2 tsvdModel.explained variance ratio [0:3].sum()

0.3003938538627934



- Feature Selection
 - Thresholding numerical features variance
 - Thresholding binary features variance
 - Handling high correlated features
 - Removing irrelevant features for Classification
 - RFEC



Thresholding numerical features variance

• The dataset has set of numerical features

Approach:

- Remove those with the low variance
- Low variance likely contains little information



Thresholding numerical features variance

1 from sklearn import datasets

2 from sklearn.feature selection import VarianceThreshold

```
1 # Load iris data
```

```
2 iris = datasets.load iris()
```

```
4 # Create features and target
```

```
5 X = iris.data
```

3

4

```
6 y = iris.target
```

1 # Create VarianceThreshold object with a variance with a

```
2 #threshold of 0.5
```

```
3 thresholder = VarianceThreshold(threshold=.5)
```

```
5 # Conduct variance thresholding
```

```
6 XHighVariance = thresholder.fit_transform(X)
```

1 # View first five rows with features with variances above

```
2 # threshold
```

```
3 XHighVariance[0:5]
```

array([[5.1, 1.4, 0.2], [4.9, 1.4, 0.2], [4.7, 1.3, 0.2], [4.6, 1.5, 0.2], [5., 1.4, 0.2]])



Handling high correlated features

- 1 # Load libraries 2 import pandas as pd
- 3 import numpy as np

```
1 # Create feature matrix with two highly correlated features
 2 X = np.array([[6, 12, 1]])
 3
                  [5, 10, 0],
 4
                  [4, 8, 1],
 5
                  [3, 3, 0],
 6
                  [2, 5, 1],
 7
                 [1, 2, 0],
 8
                 [3, 6, 1],
 9
                 [5, 10, 0],
10
                  [9, 19, 1]])
11
12 # Convert feature matrix into DataFrame
13 df = pd.DataFrame(X)
```

```
1 # Create correlation matrix
```

```
2 corr_matrix = df.corr().abs()
```

```
3 # Select upper triangle of correlation matrix
```

- 4 upper = corr_matrix.where(np.triu(np.ones(corr_matrix.shape), k=1).astype(np.bool))
- 5 # Find index of feature columns with correlation greater than 0.95
- 6 to_drop = [column for column in upper.columns if any(upper[column] > 0.95)]

```
1 # Drop features
```

2 df.drop(df[to_drop], axis=1)



Removing irrelevant features for Classification

Categorical features:

 Calculate Chi-square statistic between each feature and target

Quantitative features:

 Calculate ANOVA F-Value between each feature and target



Recursive Eliminating Feature

```
1 # Load libraries
2 from sklearn.datasets import make_regression
3 from sklearn.feature_selection import RFECV
4 from sklearn import datasets, linear_model
5 import warnings
6
7 # Suppress an annoying but harmless warning
8 warnings.filterwarnings(action="ignore", module="scipy", message="^internal gelsd")
```

1 # Create a linear regression
2 olsModel = linear model.LinearRegression()

```
1 # Create recursive feature eliminator that scores features by mean squared errors
2 rfecvModel = RFECV(estimator=olsModel, step=1, scoring='neg_mean_squared_error')
3 
4 # Fit recursive feature eliminator
5 rfecvModel.fit(X, y)
6 
7 # Recursive feature elimination
8 rfecvModel.transform(X)
```

- 1 # Number of best features
- 2 rfecvModel.n features

