

Densidades de Probabilidade

Binomial	$\{0, \dots, n\}$	$\mathbb{P}(X = k) = C_k^n p^k (1-p)^{n-k}$
Poisson	$\{0, 1, 2, \dots\}$	$\mathbb{P}(X = k) = e^{-\lambda} \frac{\lambda^n}{n!}, \quad \lambda > 0$
Gaussiana	\mathbb{R}	$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}, \quad \sigma > 0, \mu \in \mathbb{R}$
Exponencial	$[0, +\infty[$	$f(t) = \lambda e^{-\lambda t}, \quad \lambda > 0$
Gamma	$[0, +\infty[$	$f(t) = \lambda e^{-\lambda t} \frac{(\lambda t)^{n-1}}{(n-1)!}, \quad n \geq 1$

Processo de Nascimento

$$p_0(t) = e^{-\lambda_0 t}$$

$$p_n(t) = \lambda_{n-1} e^{-\lambda_n t} \int_0^t e^{\lambda_n s} p_{n-1}(s) ds, \quad n = 1, 2, \dots$$

Se $\lambda_i \neq \lambda_j$ para $i \neq j$, então

$$p_n(t) = \lambda_0 \cdots \lambda_{n-1} \sum_{k=0}^n \left(\prod_{j=0, j \neq k}^n \frac{1}{\lambda_j - \lambda_k} \right) e^{-\lambda_k t}, \quad n = 1, 2, \dots$$

Processo de Nascimento e Morte

$$\theta_0 = 1, \quad \theta_n = \frac{\lambda_0 \cdots \lambda_{n-1}}{\mu_1 \cdots \mu_n}, \quad n = 1, 2, \dots$$

$$\pi_n = \frac{\theta_n}{\sum_{n=0}^{\infty} \theta_n}, \quad n = 0, 1, 2, \dots$$

Fila de Espera M/M/1

$$\rho = \frac{\lambda}{\mu}, \quad \pi_n = (1 - \rho) \rho^n, \quad n \geq 0.$$

$$L = \frac{\rho}{1 - \rho}, \quad L = \lambda W$$

$$L_0 = \frac{\rho^2}{1 - \rho}, \quad L_0 = \lambda W_0$$

Fila de Espera M/M/s

$$\rho = \frac{\lambda}{s\mu}, \quad \pi_n = \theta_n \left(\frac{s^s}{s!} \frac{\rho^s}{1 - \rho} + \sum_{n=0}^{s-1} \frac{s^n}{n!} \rho^n \right)^{-1}, \quad n \geq 0,$$

$$\theta_n = \begin{cases} \frac{s^n}{n!} \rho^n, & n < s \\ \frac{s^s}{s!} \rho^n, & n \geq s \end{cases}$$

$$L = \lambda W, \quad W = W_0 + \frac{1}{\mu}$$

$$L_0 = \frac{s^s}{s!} \frac{\rho^{s+1}}{(1 - \rho)^2} \pi_0, \quad W_0 = \frac{L_0}{\lambda}$$