

## CHAPTER 2: Ricardian model:

- Only one factor of production: labor
- Labor is mobile across sectors
- ➔ Everyone gains from trade

## CHAPTER 3:

- We have more than one factor of production
- What if these factors are NOT mobile across sectors?
- ➔ Then there may be losers and winners!  
(unequal effects of globalization)

## CHAPTER 3:

- Setting up the specific factor model
- Change in production and employment
- Aggregate gains from trade
- Effect on labor wages
- Effect on returns to K and Land

# 1 Setup of Factor-Specific Model

- Two countries: Home and Foreign.
- Two sectors: Manufacturing and Agriculture
- Manufacturing uses labor and **capital**
- Agriculture uses labor and **land**.

# 1 Setup of Factor-Specific Model

- Two countries: Home and Foreign.
- Two sectors: Manufacturing and Agriculture
- Manufacturing uses labor and **capital**
- Agriculture uses labor and **land**.
- *Diminishing returns* for labor in each industry:  
*The marginal product of labor declines if the amount of labor used in the industry increases.*

# 1 Setup of Factor-Specific Model

Alternative interpretation

*NOTE:*

*We can also use the same model and interpret “capital” and “land” as fixed labor:*

**Capital:** equivalent to Labor that is stuck in manufacturing

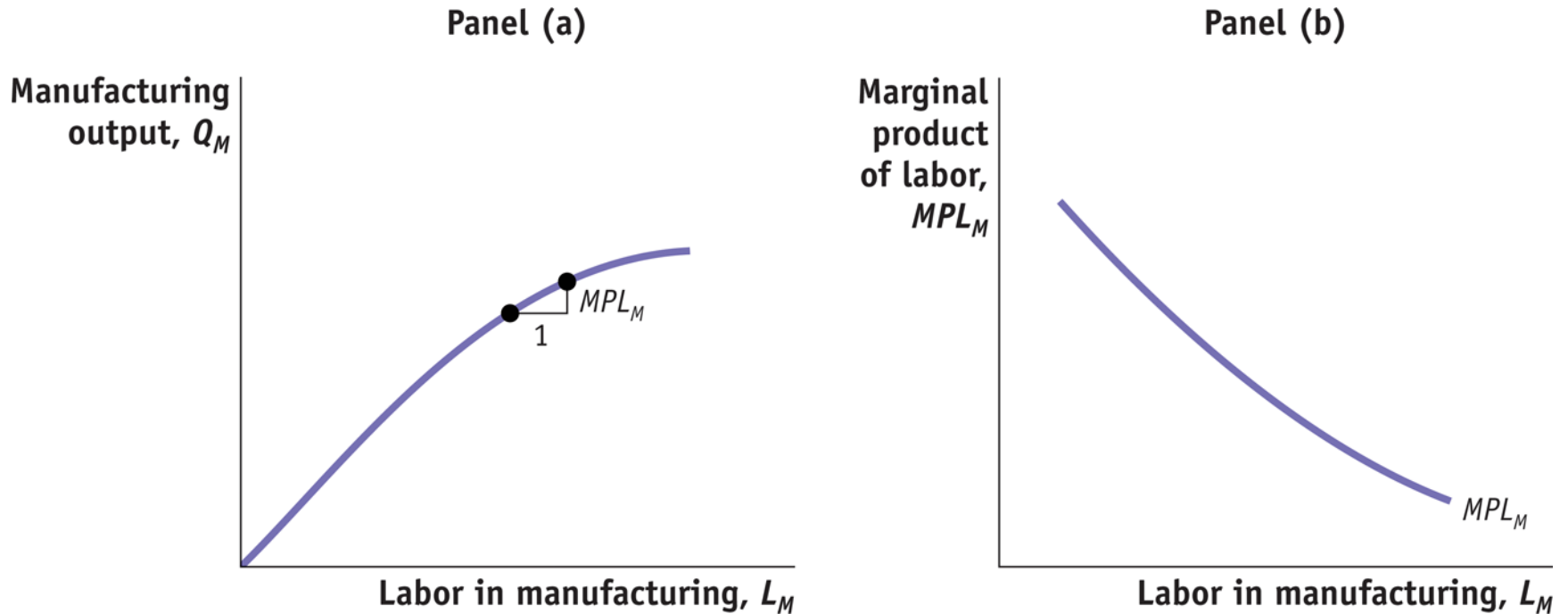
**Land:** equivalent to Labor that is stuck in Agriculture

**Labor:** Labor that is mobile across industries

→ Three types of labor depending on its mobility

# 1 Setup of Factor-Specific Model

*Diminishing returns* for labor in each industry:



(same for Agriculture:  $MPL$  decreases with production)

# 1 Setup of Factor-Specific Model

Example of production function:

- Manufactures:  $Y_M = a_M K^{1/3} L_M^{2/3}$
- Agriculture:  $Y_A = a_A T^{1/3} L_A^{2/3}$

Marginal product of Labor:

- MPL in Manufactures:  $MPL_M = \frac{2}{3} a_M (K/L_M)^{1/3}$   
Increases with  $K/L_M$
- MPL in Agriculture:  $MPL_A = \frac{2}{3} a_A (T/L_A)^{1/3}$   
Increases with  $T/L_A$

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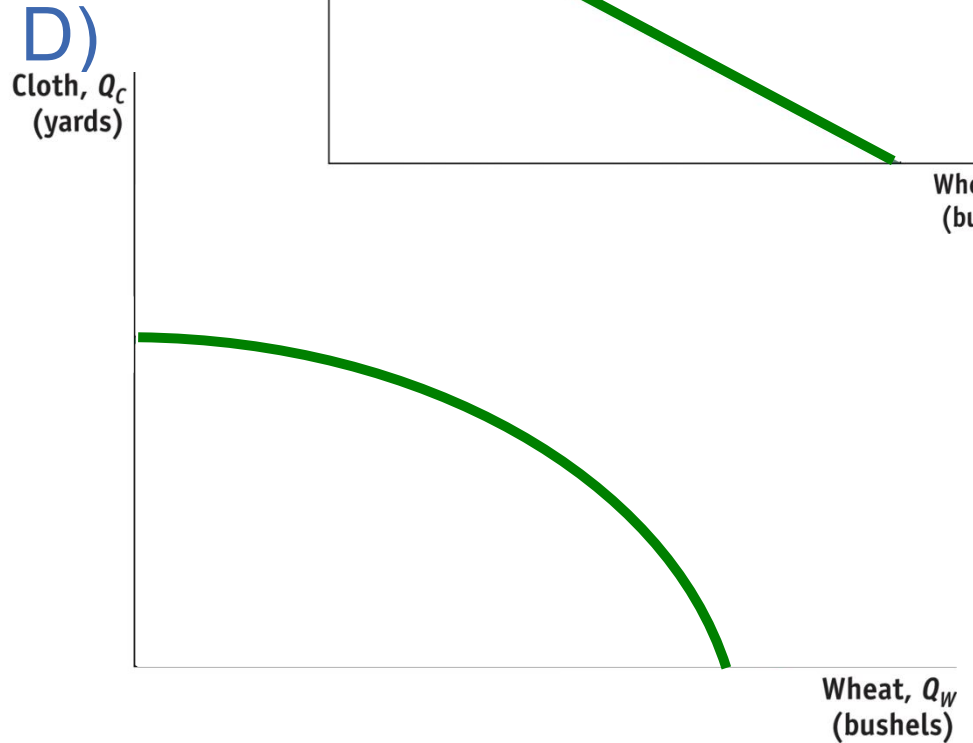
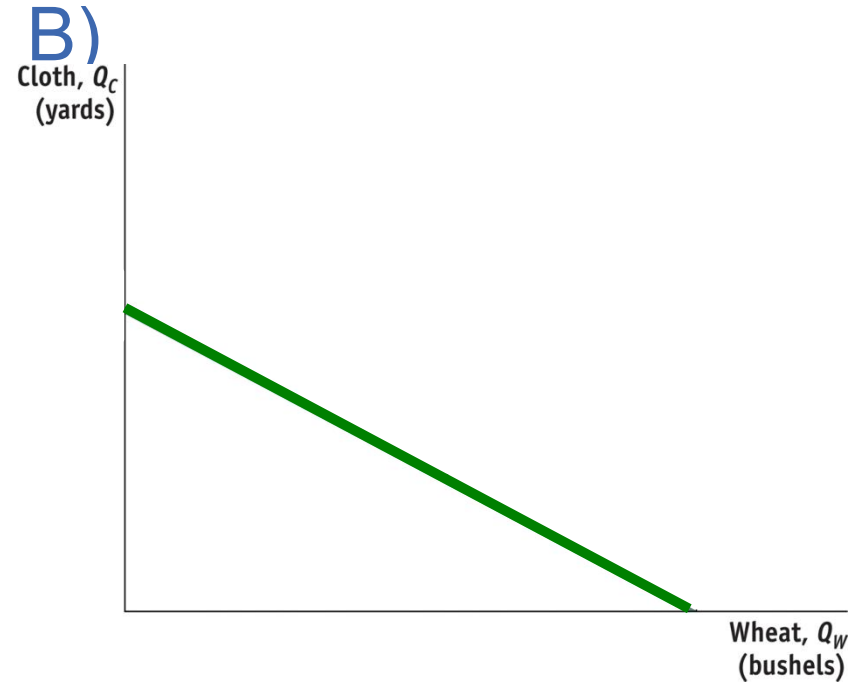
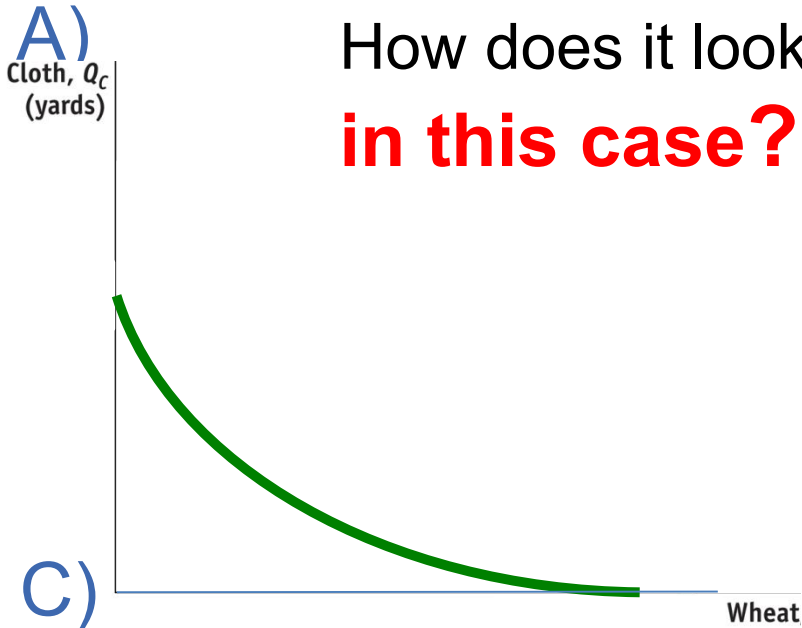
Marginal product of Capital and Land:

- MPK in Manufactures:  $MPK = \frac{1}{3} a_M (L_M/K)^{2/3}$   
Decreases with  $K/L_M$
- MPT in Agriculture:  $MPT = \frac{1}{3} a_A (L_A/T)^{2/3}$   
Decreases with  $T/L_A$



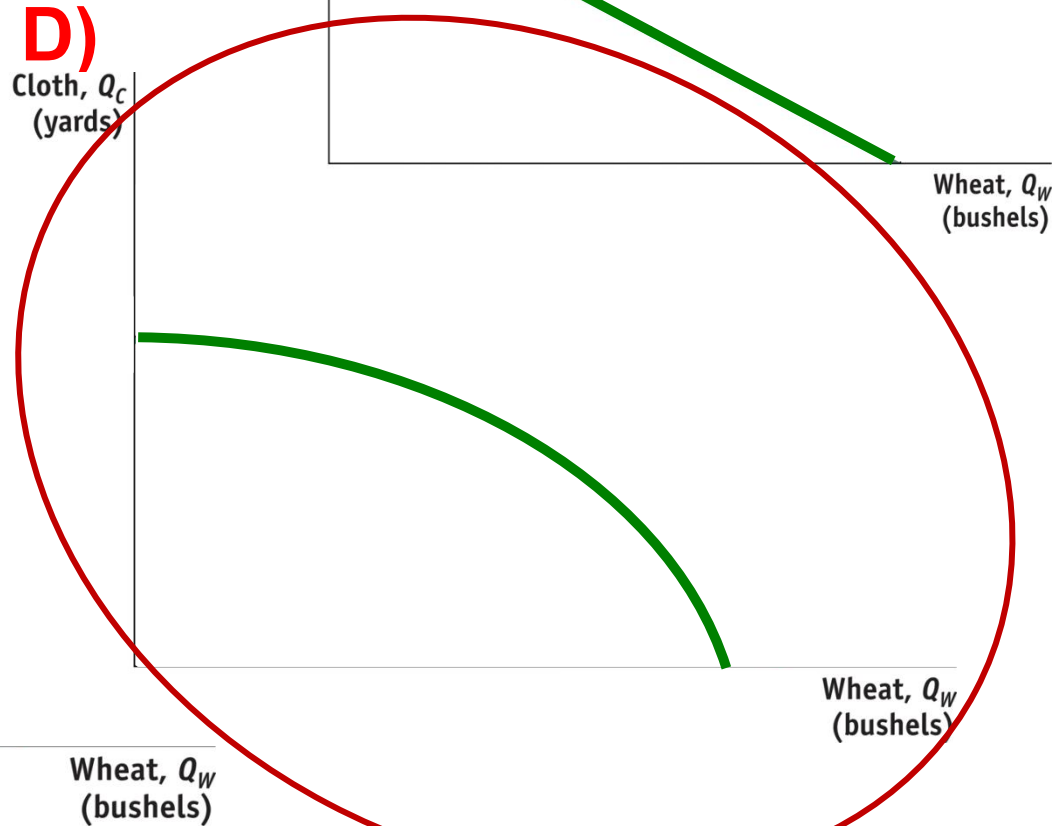
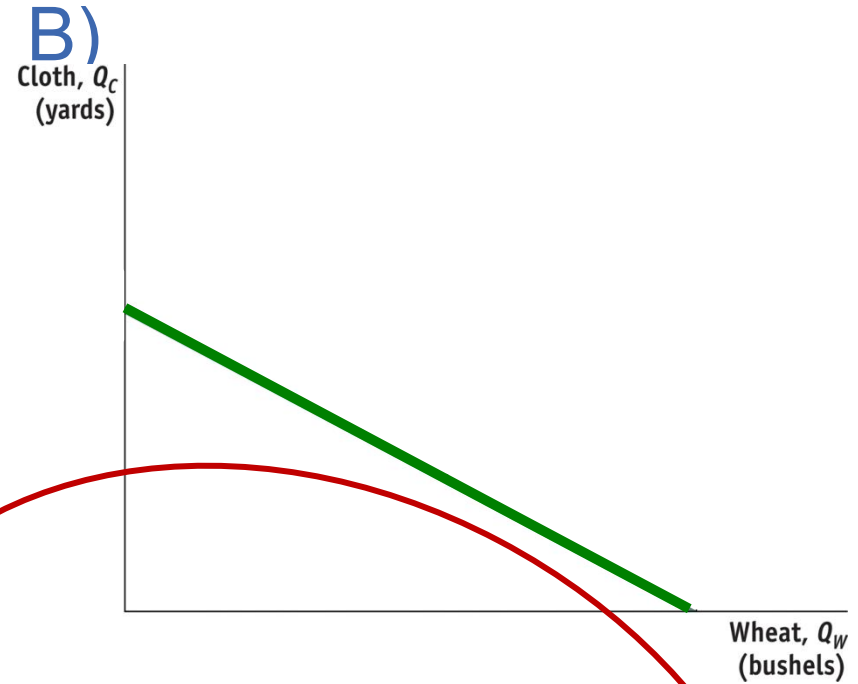
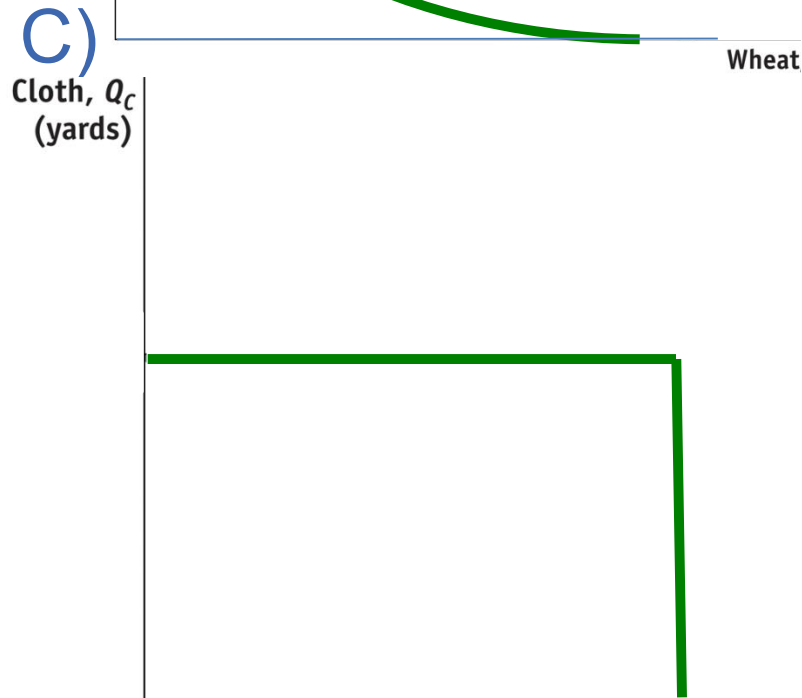
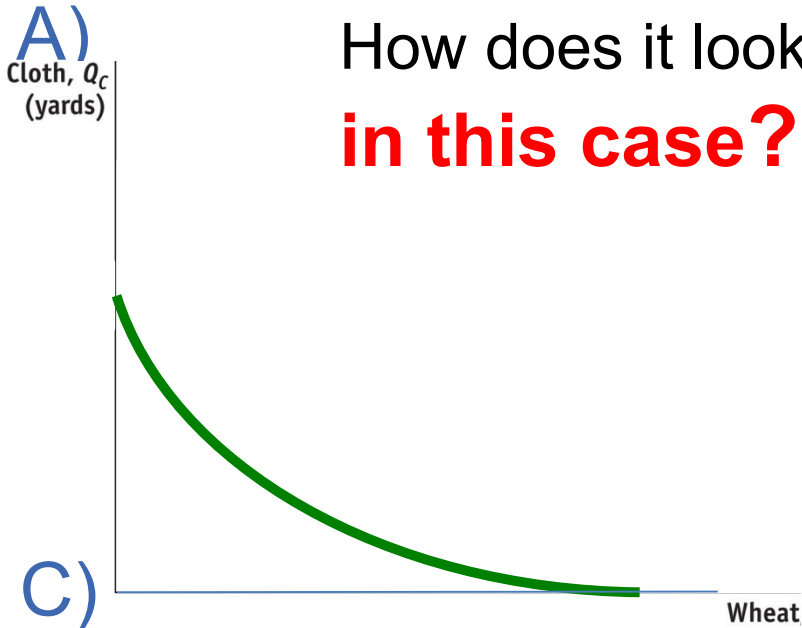
# Production Possibility Frontier:

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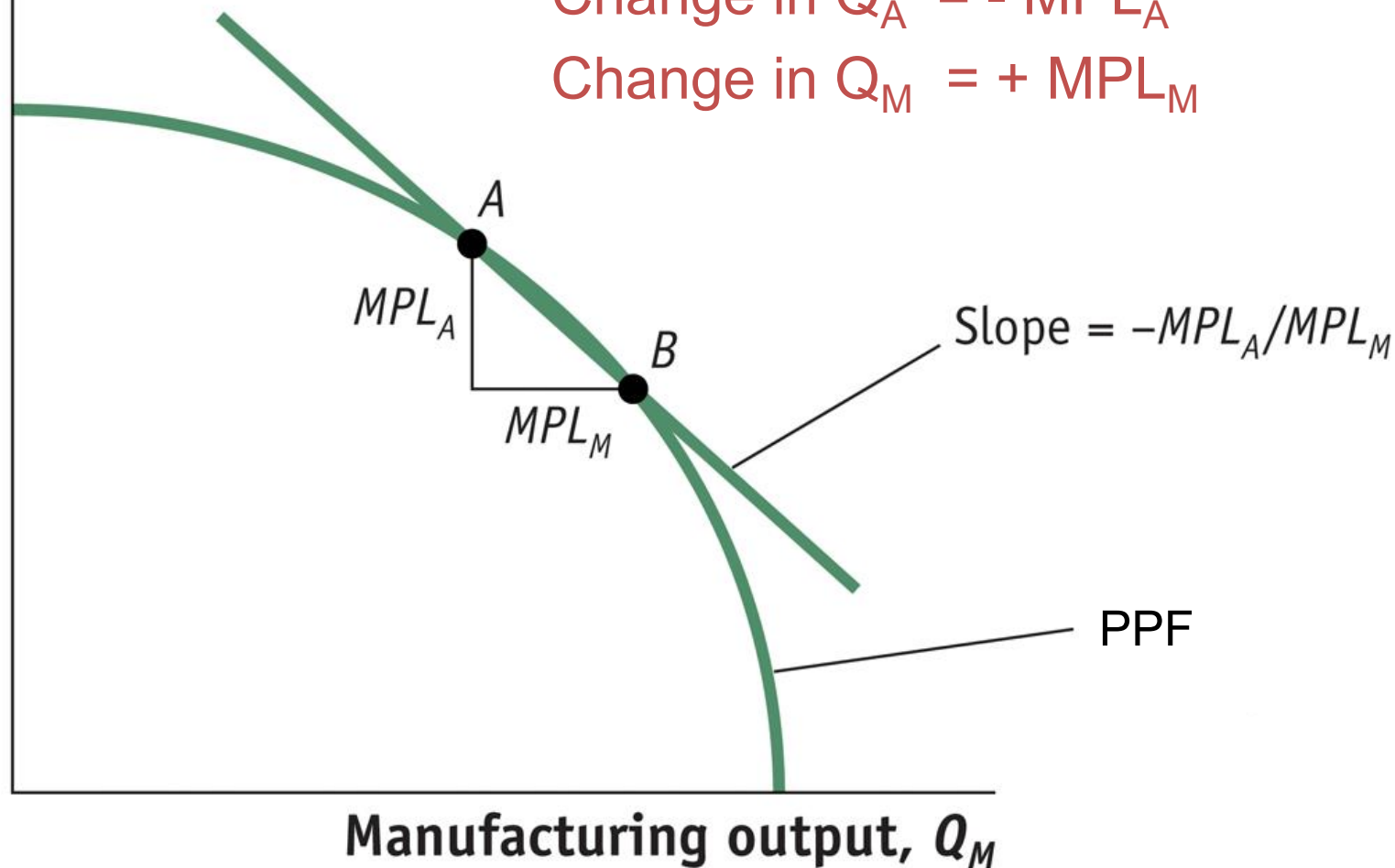
Slope of PPF reflects the opportunity cost of manuf. output:

Agriculture  
output,  $Q_A$

If one worker moves from A to B  
(i.e. from Ag to Manufacturing):

$$\text{Change in } Q_A = -MPL_A$$

$$\text{Change in } Q_M = +MPL_M$$

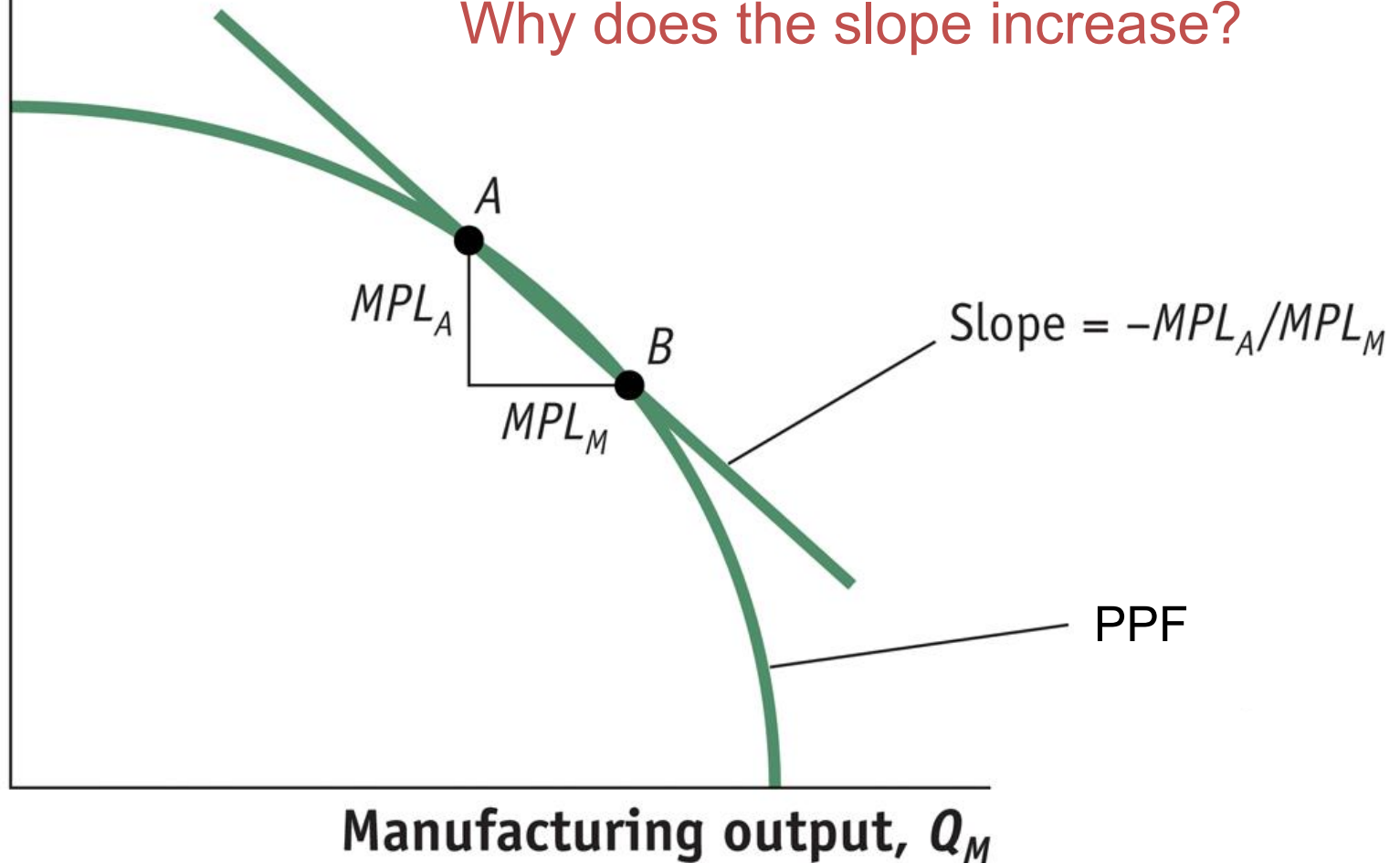


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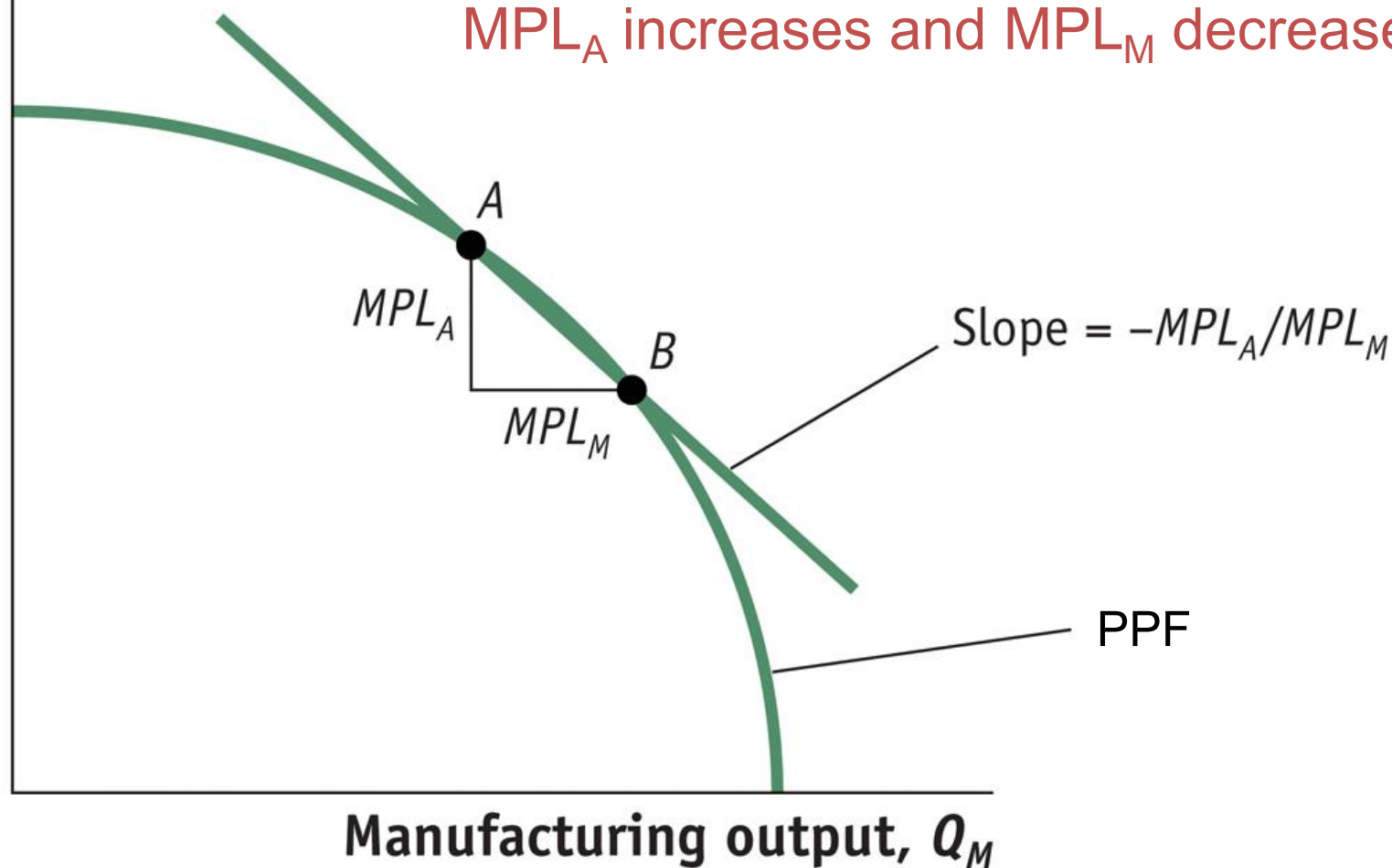
Why does the slope increase?



Slope of PPF reflects the opportunity cost of manuf. output:

Agriculture  
output,  $Q_A$

If one worker moves from A to B:  
Why does the slope increase?  
 $MPL_A$  increases and  $MPL_M$  decreases



# 1 Setup of Factor-Specific Model

## Slope of PPF

Why does the slope increase from point A to B?

- Slope equals  $MPL_A/MPL_M$
- As  $L_A$  decreases,  $MPL_A$  increases
- As  $L_M$  increases,  $MPL_M$  decreases

→ Hence the ratio increases!

# 1 Setup of Factor-Specific Model

## Labor market and relative prices

- Labor is mobile across sectors
- Hence **wages** are equalized:

$$W = P_M \cdot MPL_M$$

$$W = P_A \cdot MPL_A$$

- And should be the same across sectors. Hence:

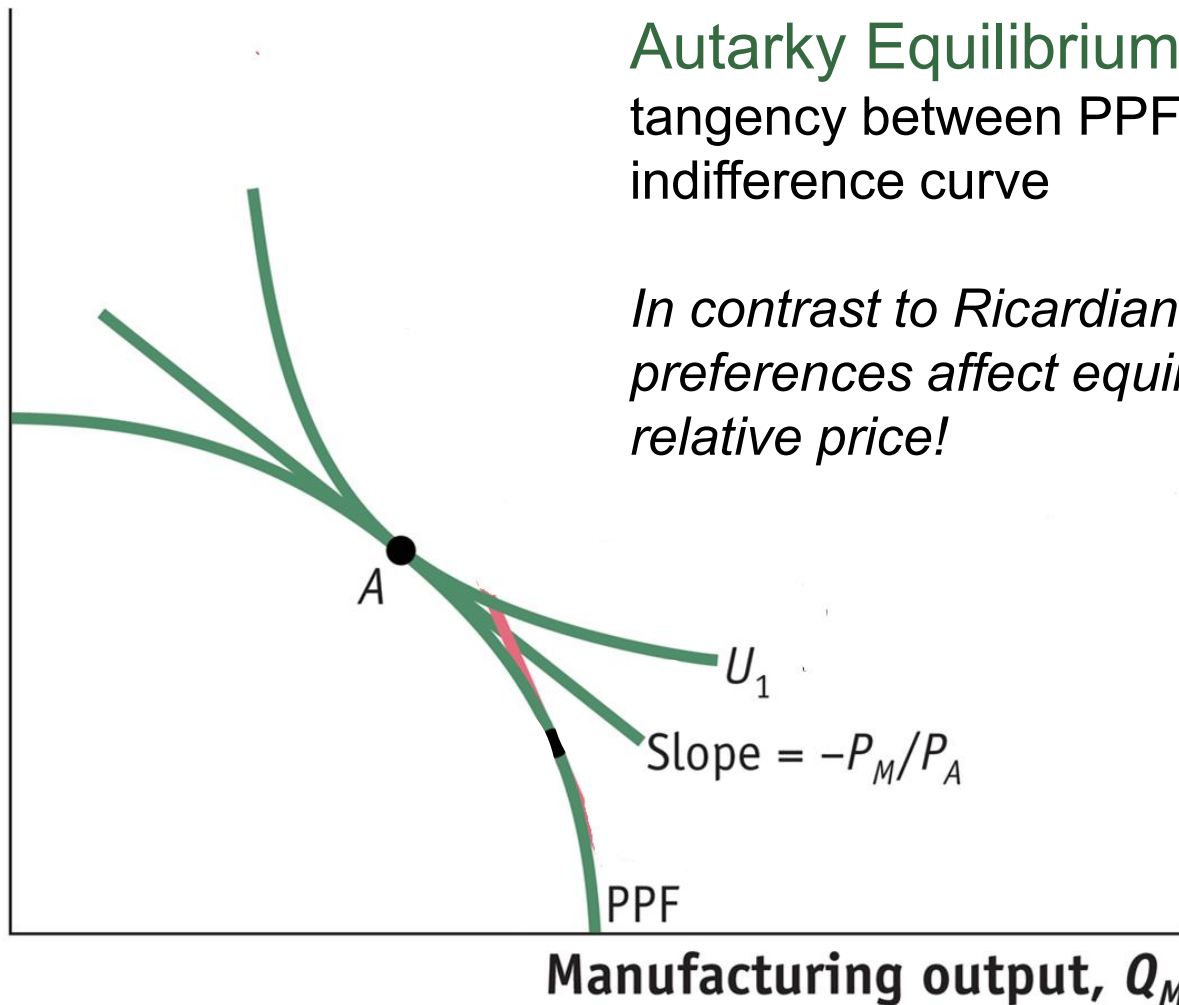
$$\frac{P_M}{P_A} = \frac{MPL_A}{MPL_M}$$

= Slope of the PPF

# 1 Setup of Factor-Specific Model

Equilibrium in Autarky:

Agriculture  
output,  $Q_A$





## CHAPTER 3

- Setting up the specific factor model

→ Change in production and employment

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## 2 Effect of Trade on production

### The Foreign Country

- Let us assume that Home has a comparative advantage in manufacturing

⇔ *Equivalent to assuming that the Home no-trade relative price of manufacturing is lower than Foreign rel. price:*

$$(P_M / P_A) < (P^*_M / P^*_A).$$

New world price?

## 2 Effect of Trade on production

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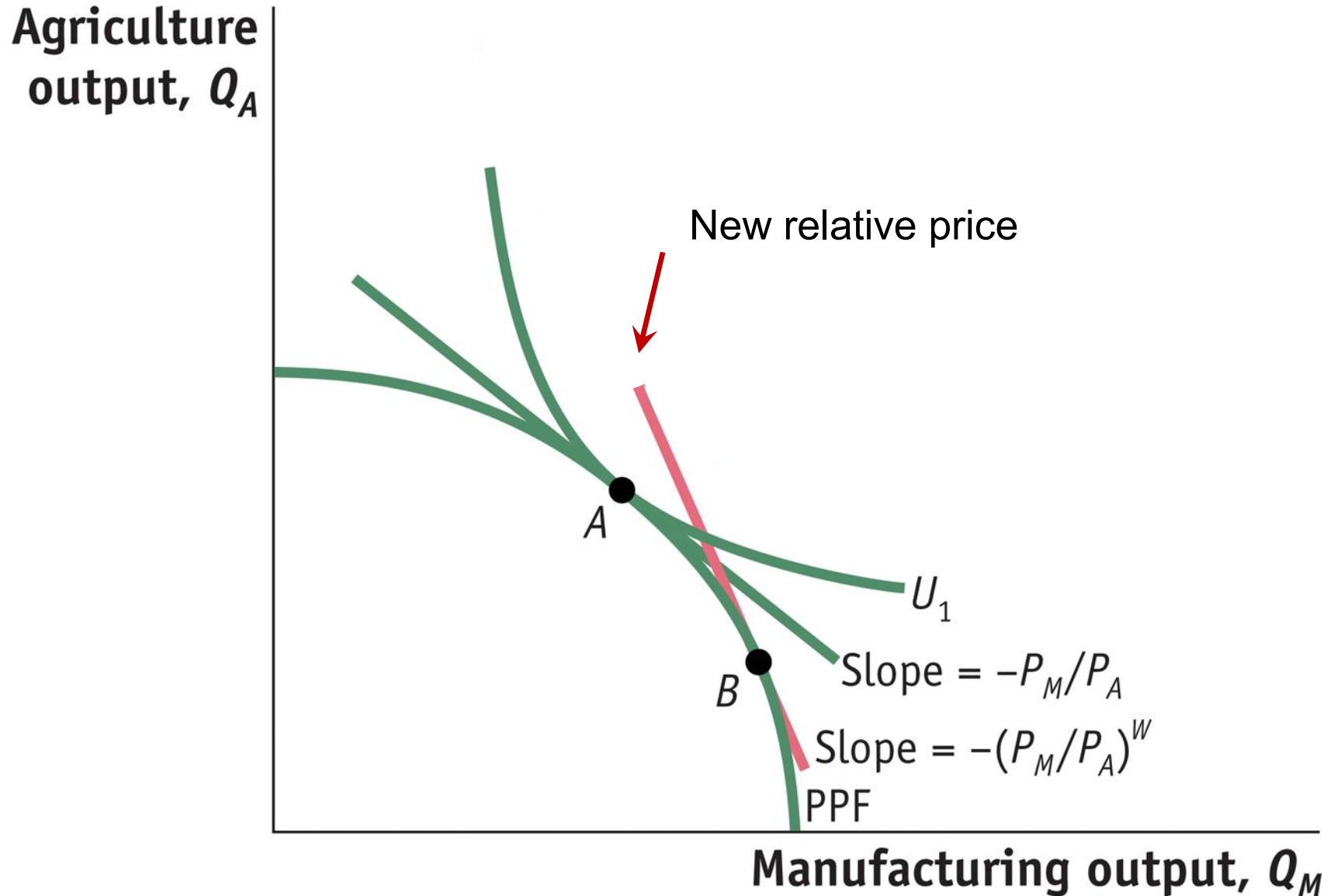
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New world price:

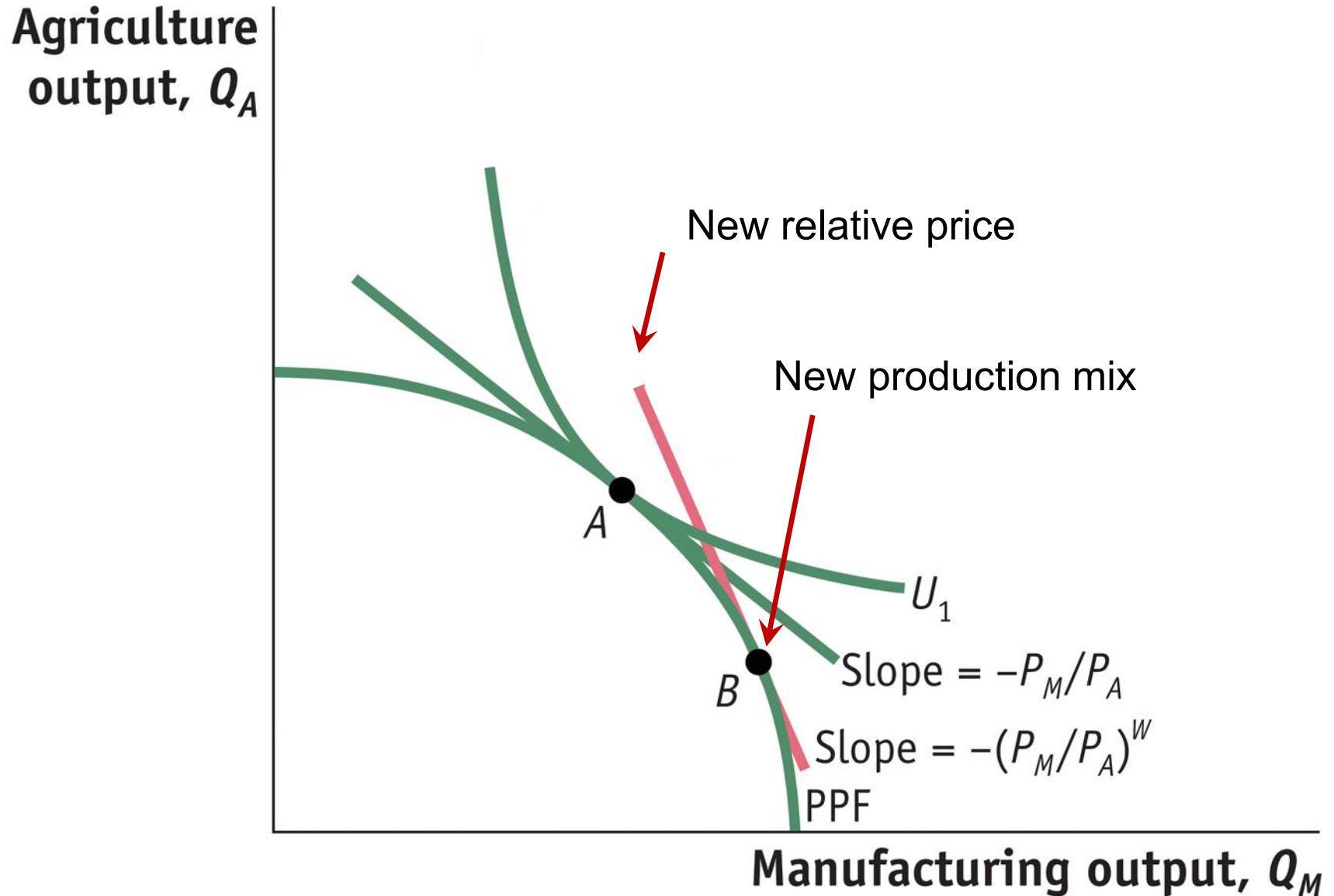
$$(P_M / P_A) < (P_M / P_A)^W < (P^*_M / P^*_A).$$

Effect on production?

## 2 Effect of Trade on production



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## 2 Effect of Trade on production

Quantitative example:

In the next example with Cobb-Douglas production, I would like to show you:

- How to link ratio of MPL to employment
- How to link ratio of MPL to prices
- ➔ How to link employment to prices

## 2 Effect of Trade on production

Quantitative example:

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→ Slope of PPF: 
$$Slope = \frac{MPL_A}{MPL_M} = \frac{a_A T^{1/3}}{a_M K^{1/3}} \left( \frac{L_M}{L_A} \right)^{1/3}$$



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Quantitative example:

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Constant term x Employment ratio

## 2 Effect of Trade on production

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- At equilibrium:  $Slope = \frac{P_M}{P_A}$
- How does a change in prices affects  $\frac{L_A}{L_M}$ ?

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Quantitative example:

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- At equilibrium:  $Slope = \frac{P_M}{P_A}$
- How does a change in prices affects  $\frac{L_A}{L_M}$ ?

$$\frac{P_M}{P_A} = \frac{a_A T^{1/3}}{a_M K^{1/3}} \left( \frac{L_M}{L_A} \right)^{1/3} \Rightarrow \frac{L_A}{L_M} = \frac{a_A^3 T}{a_M^3 K} \left( \frac{P_A}{P_M} \right)^3$$

If the relative price of manufacturing goods increases by 1%, relative employment in manufacturing  $L_M / L_A$  increases by:

- a) A negative percentage, i.e. decreases!!
- b) Increases by 1%
- c) Increases by 0.33%
- d) Increases by 3%

Answer:

If the relative price of manufacturing goods increases by 1%, relative employment in manufacturing  $L_M / L_A$  increases by:

## Some useful algebra...

Quantifying changes with exponents, etc.:

- Suppose  $Z = a X^\beta$
- If X increases by 1% then Z increases by  $\beta$  %.
- If Z increases by 1% then X increases by  $1/\beta$  %.

- Suppose  $Z = X \cdot Y$

- If X increases by  $x$  %

- If Y increases by  $y$  %

→ Then Z increases by:  $x+y$  %.

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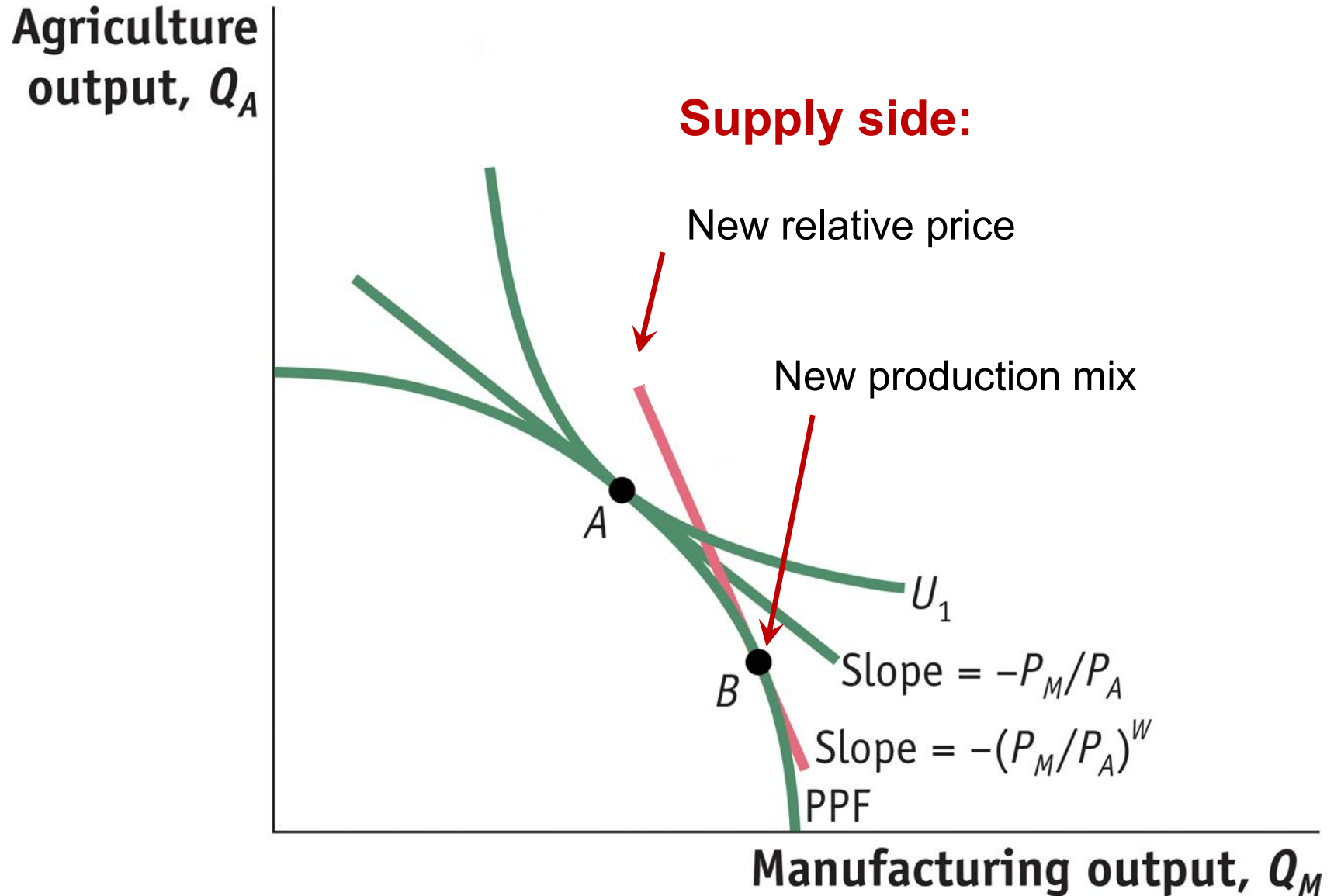
# 3 Gains from Trade

## Overall Gains from Trade?

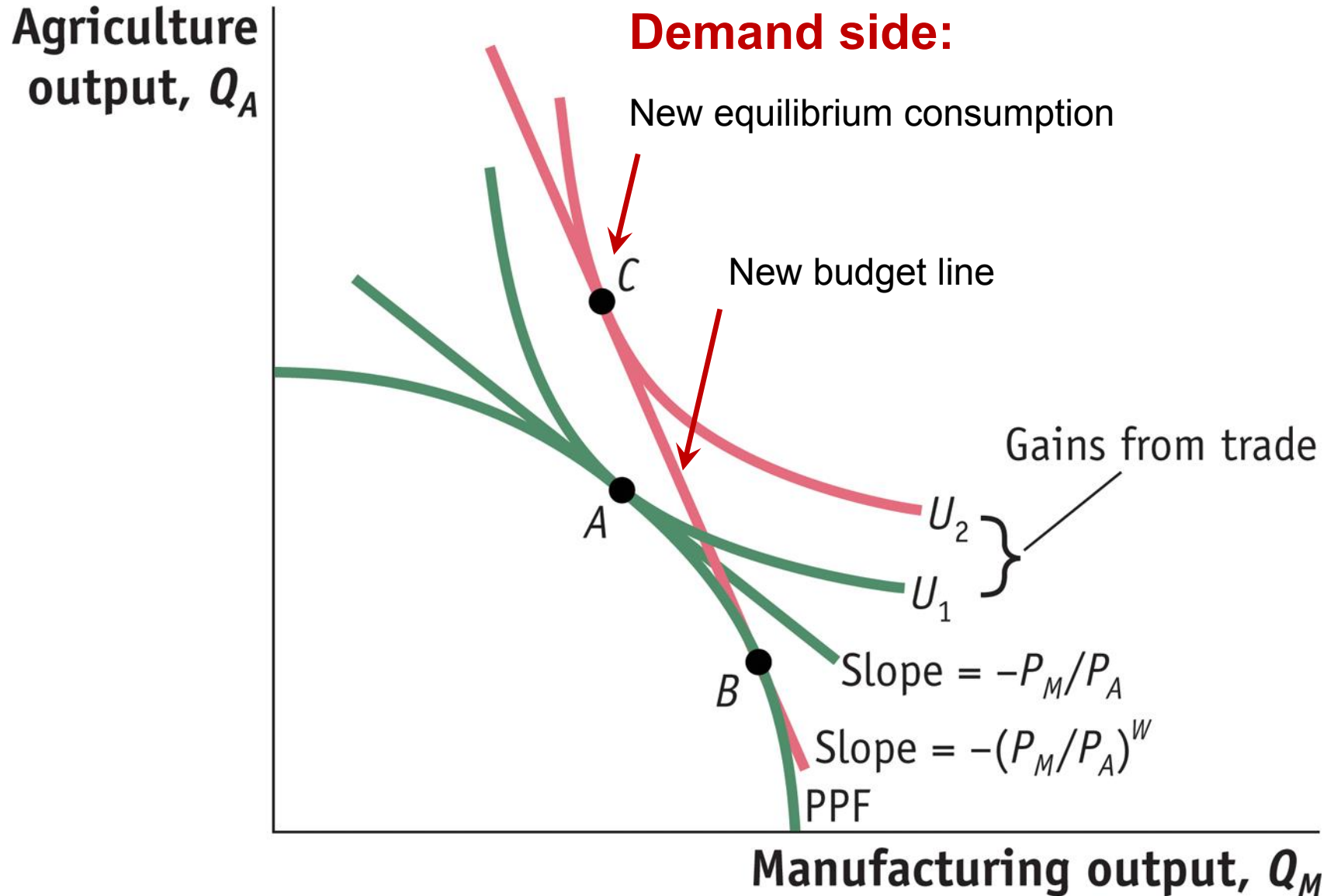
- We start by looking at the average consumer

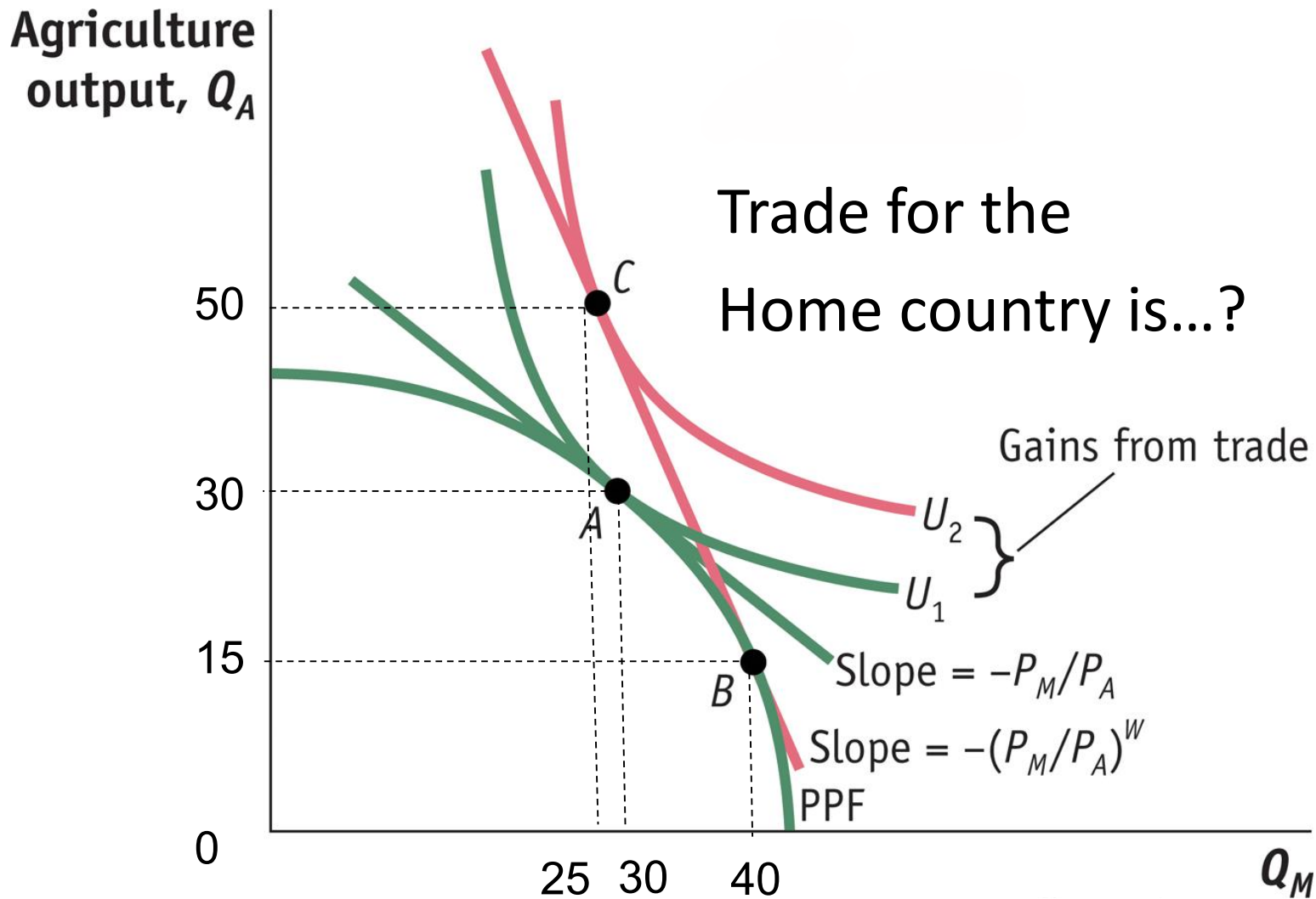


# 3 Gains from Trade



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- a)  $X_M = 5, M_A = 20$ ;    b)  $X_M = 20, M_A = 20$ ;  
 c)  $X_M = 15, M_A = 35$ ;    d)  $X_M = 20, M_A = 15$ ;

# 3 Gains from Trade

## Overall Gains from Trade

*So far, things are not very different from Ricardo:*

New world price:

$$(P_M / P_A) < (P_M / P_A)^W < (P_M^* / P_A^*).$$

- Manufacturing goods are exported,
- Agricultural goods are imported
- For an average consumer, Home is better off with trade.

# 3 Gains from Trade

## Gains for everyone?

- When there are gains from trade *on average*, it does not imply that everyone gains from trade
- The interesting part of the model is to examine what happens to the return to each factor:
  - 1) Labor wage
  - 2) Rental rate of Capital and Land

Do workers gain? Do land and capital owner gain?