Microeconomics

Chapter 13
Competitive markets

Fall 2025

From Individual Behavior to Markets

Up until now we have studied **maximizing** behavior of **individual** economic agents: firms and consumers. We have taken the **economic environment** as **given**, completely summarized by the vector of market prices.

In this chapter, we begin to study of how **market prices** are **determined** by the actions of individual agents. We start with the simplest model, a single competitive market.

Real world markets do not often achieve this ideal, but looking at a model of **perfect competition** can still generate useful **insights** in the economics world.

Perfect competition

Perfect competition has two main characteristics:

- (1) large number of firms that
- (2) sell a homogeneous good

This ensures that perfectly competitive firms are price takers.

One firm's output is a perfect substitute for another firm's output (good is homogenous) and each firm is a small part of the market (large number of firms).

It follows that each firm cannot unilaterally influence the market price at which it can sell its good or service. It must accept, or "take" the market equilibrium price. Hence the term, price taker.

Perfect competition and demand curve

Let p^* be the equilibrium market price, then a firm's demand curve D(p) can be characterized as follows:

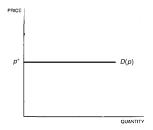
$$D(p) = \begin{cases} 0 & \text{if } p > p^* \\ \text{any amount} & \text{if } p = p^* \\ \infty & \text{if } p < p^* \end{cases}$$

We will later discuss how the equilibrium price p^* is determined. Next, we discuss the firm's demand curve.

A firm's demand curve

The market demand curve for given good in a perfectly competitive market is downward sloping.

However, **no single firm** in this market can influence the price at which it sells its output. This point means a firm that is a price taker must take the **equilibrium market price as given**, and the firm faces a **perfectly elastic** demand.



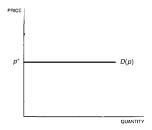
Therefore, demand curve for a perfectly competitive firm is **horizontal**: against the given market price p^* it can sell any amount.

Note that the graph shows the **inverse demand curve**: price as a function of quantity. Instead, the **demand curve** is: quantity as a function of price.

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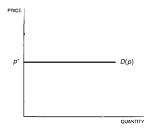
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From the perspective of a single competitive firm, the price *p* is given. This makes profit maximization simple: **choose output** *y* as to maximize profits while *y* does not affect the price,

$$\max_{y} py - c(y),$$

where c(y) is a cost function discussed in Chapter 4.

The FOC for profit maximization sets the first derivative to zero,

$$\frac{\partial \pi(y)}{\partial y} = p - \frac{\partial c(y)}{\partial y} = 0.$$

Which can be written as,

$$\underbrace{p}_{MR} = \underbrace{\frac{\partial c(y)}{\partial y}}_{MC(y)}$$

Intuitively, making an additional y costs MC(y) and selling an additional y generates revenue p, and so if p > MC(y) the firm should make and sell additional y. In turn, if p < MC(y) the firm should make and sell less y.

Hence, a perfectly competitive firm produces output y until MC(y) is equal to the fixed price p:

$$p = MC(y)$$
.

The FOC pins down a **firm's supply**: for each price p you can trace out the quantity y so that p = MC(y), which is the quantity the firm will produce.

Note that the FOC above gives the **inverse supply function**: p = MC(y) gives p as a function of y. This measures the price that must prevail in order for a firm to find it profitable to supply a given amount of output.

Taking the inverse of this FOC gives us the **supply function**: $y = MC^{-1}(p) = y(p)$ gives y as a function of p. This is the profit-maximizing output at each price.

We have focused so far on the **interior solution**, i.e., solution to the FOC with y(p) > 0. However, it is of interest to understand when the interior solution is **chosen**.

Indeed, despite a FOC with y(p) > 0, a firm may prefer not to produce at all with y = 0, which is a **corner solution**.

Consider a firm's short-run cost function as follows

$$c(y) = c_{\nu}(y) + FC,$$

where $c_v(y)$ are the variable costs and FC are the fixed costs.

The firm will only find it profitable to produce the solution to the FOC y(p) > 0 if the profits of doing so exceed the profits of producing nothing:

$$\underbrace{p \cdot y(p) - c_{\nu}(y(p)) - FC}_{\pi(y(p))} \ge \underbrace{-FC}_{\pi(y=0)}.$$

Note that FC have to be paid even if the firm producers nothing.

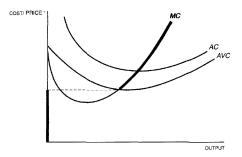


Eliminating FC on both sides, we can write this as,

$$p \geq \underbrace{\frac{c(y(p))}{y(p)}}_{AVC}$$

Hence, if $p \ge AVC(y(p))$ the firm will choose the output y given by the FOC y(p) > 0. However, if p < AVC(y(p)) the firm will choose y = 0 despite a FOC with y(p) > 0.

A price that is equal to the average variable cost is often referred to as the **shutdown price**.



A perfectly competitive firm's **supply function** equals the MC curve as long as the price is above AVC. If the price is below the AVC, then supply shoots to zero. We can summarize this as,

$$y(p) = \begin{cases} 0 & \text{if } p < AVC(y(p)) \\ y(p) & \text{if } p \ge AVC(y(p)) \end{cases}$$

Market equilibrium

Recall that each **single firm** is a **price taker**: it takes the **market equilibrium price** p^* as given, which determines their perfectly elastic demand $D(p^*)$ and their supply $y(p^*)$.

However, how is the equilibrium price p^* determined?

Let there be i = 1, ..., m identical firms: same cost functions. Let a single firms' supply curve be denoted by $y_i(p)$. Then the **market supply curve** is

$$Y(p) = \sum_{i=1}^{m} y_i(p) = m \cdot y_i(p).$$

Let there be j = 1, ..., n identical consumers: same preferences. Let a single (Marshallian) demand be given by $x_j(p)$. Then the **market demand curve** is

$$X(p) = \sum_{j=1}^{n} x_j(p) = n \cdot x_j(p).$$

Market equilibrium

The market equilibrium is a point where market supply equals market demand:

$$Y(p) = X(p)$$
.

The equilibrium price $p = p^*$ solves $Y(p^*) = X(p^*)$. This is an equilibrium since at this point no agent has an incentive to unilaterally change its behavior.

It is this equilibrium price p^* that each single firm takes as given, which determines their perfectly elastic demand $D(p^*)$ and their supply $y(p^*)$.

Hence, although each firm's demand D(p) is perfectly elastic, the market demand X(p) is not.



In **the long run**, truly competitive markets have a third characteristic:

(3) entry and exit

This ensures that perfectly competitive firms make **zero profits** in the long run. Intuitively, if perfectly competitive firms make positive (negative) profits in the short run, then firms enter (exit) the market and the equilibrium price p^* decreases (increases), until profits are zero.

This third characteristic in the long run guarantees that the **long-run equilibrium** is characterized by two conditions:

$$Y(p) = X(p),$$

 $\pi_i(y_i(p)) = 0, \forall i.$

Hence, the long-run equilibrium is additionally characterized by $\pi_i(y_i(p)) = \pi_i(p) = 0$ for all i.

How does entry and exit guarantee that $\pi_i(p) = 0$?

If $\pi_i(p) > 0$ then firms **enter** until $\pi_i(p) = 0$:

$$\pi_i(p) > 0 \to \text{entry} \to Y(p) \uparrow \to p^* \downarrow \to y_i(p) \downarrow \to \pi_i(p) \downarrow \text{ until } \pi_i(p) = 0.$$

If $\pi_i(p) < 0$ then firms **exit** until $\pi_i(p) = 0$:

$$\pi_i(p) < 0 \rightarrow \text{exit} \rightarrow Y(p) \downarrow \rightarrow p^* \uparrow \rightarrow y_i(p) \uparrow \rightarrow \pi_i(p) \uparrow \text{ until } \pi_i(p) = 0.$$

Consider that at some point in time $\pi_i(p) = 0$. Then, consumer preferences change so that $X(p) \uparrow$.

In the short run, it may be that $p^* \uparrow$ since X(p) = Y(p) at higher p, so that $y_i(p) \uparrow$ and $\pi_i(p) > 0$. However, in the long run entry will take place so that $Y(p) \uparrow$ until $\pi_i(p) = 0$.



Hence, the **long-run equilibrium** is additionally characterized by $\pi_i(p) = 0$. Recall that the firm's profits can be represented by:

$$\pi_i(p) = p \cdot y_i(p) - c(y_i(p)).$$

Using that $c(y_i(p)) = ATC(y_i(p)) \cdot y_i(p)$, we can write the profits as,

$$\pi_i(p) = (p - ATC(y_i(p))) \cdot y_i(p).$$

Hence, the **long-run equilibrium price** p^* in a competitive market with entry and exit is as follows,

$$p^* = MC(y_i(p^*)) = \min(ATC(y_i(p^*))).$$

The price that is equal to the minimum of the average total cost is often referred to as the **break-even price**.

Exercise

Consider a perfect competitive market. Let the cost function of a single firm be equal to:

$$c(y)=y^2+1.$$

Let the market demand be given by:

$$X(p) = 10 - p$$
.

- 1. Find the individual's firm supply curve.
- 2. Consider that in the short run 2 identical firms are active in the market: both firms have the above cost function. Find the market supply curve.
- 3. Determine the market equilibrium price and supply with the 2 firms.
- 4. How much profit do the 2 firms make in the short run? (the solution will not be an integer)
- 5. How many firms will there be active in this market in the long run? Consider that all potential firms have the same cost function as above.

Homework exercises

Exercises: exercises on the slides