



LISBON
SCHOOL OF
ECONOMICS &
MANAGEMENT
UNIVERSIDADE DE LISBOA

Carlos J. Costa

CLUSTERS ANALYSIS

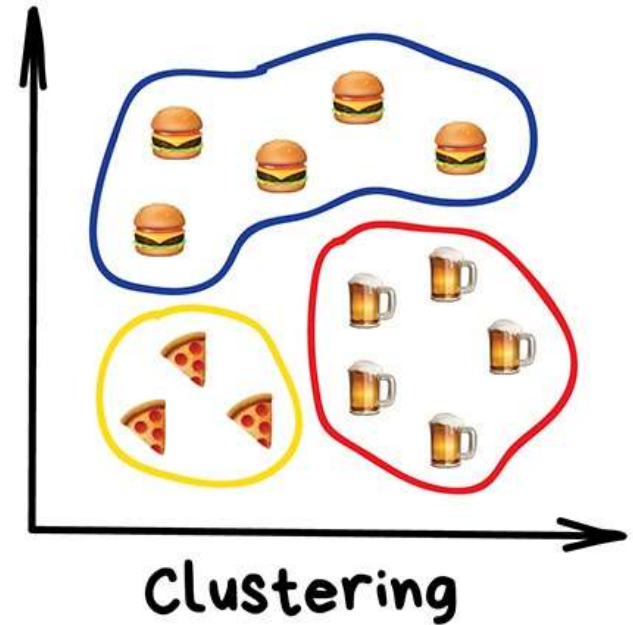
(2021)

Summary

- Cluster analysis Concept
- K-Means Clustering
- Means Shift Clustering
- Validation of Clusters

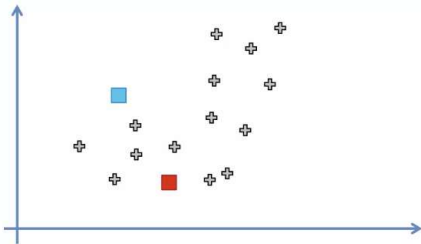
Cluster Analysis

- Multivariate method
- aims to classify a sample of subjects (or objects) into several different groups
- based on a set of measured variables

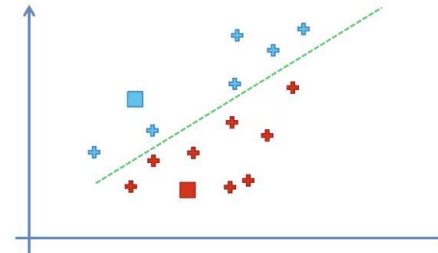


K-means Clustering

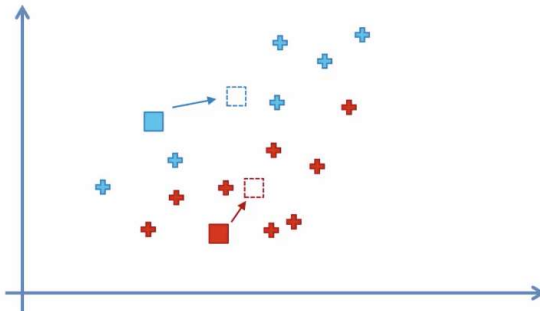
- 1. Select K (i.e. 2) random points as cluster centres called centroids



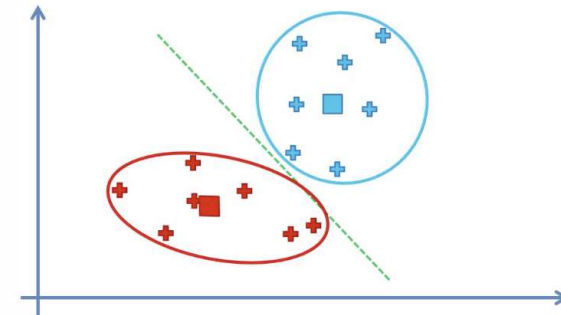
- 2. Assign each data point to the closest cluster by calculating its distance with respect to each centroid



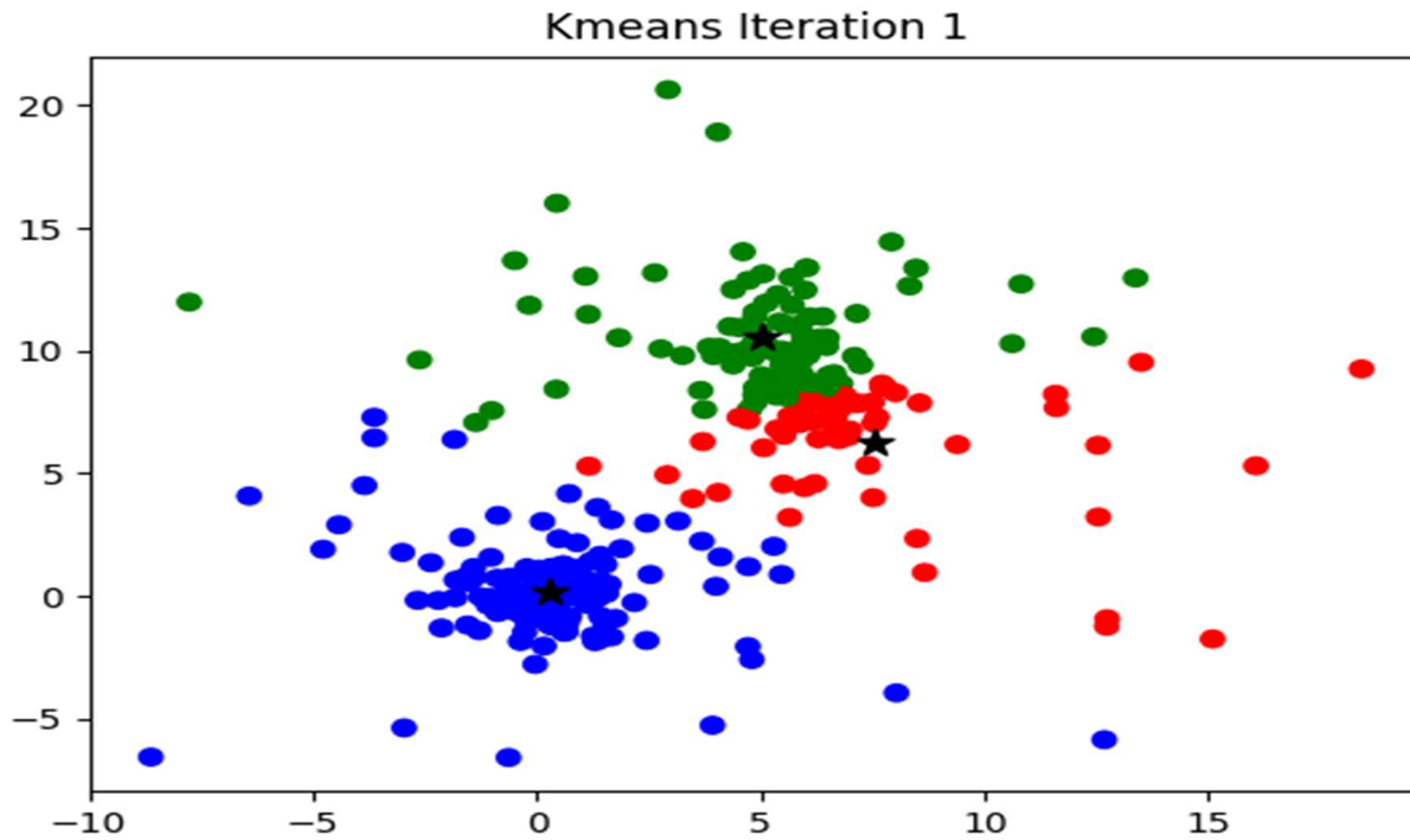
- 3. Determine the new cluster centre by computing the average of the assigned points



- 4. Repeat steps 2 and 3 until none of the cluster assignments change

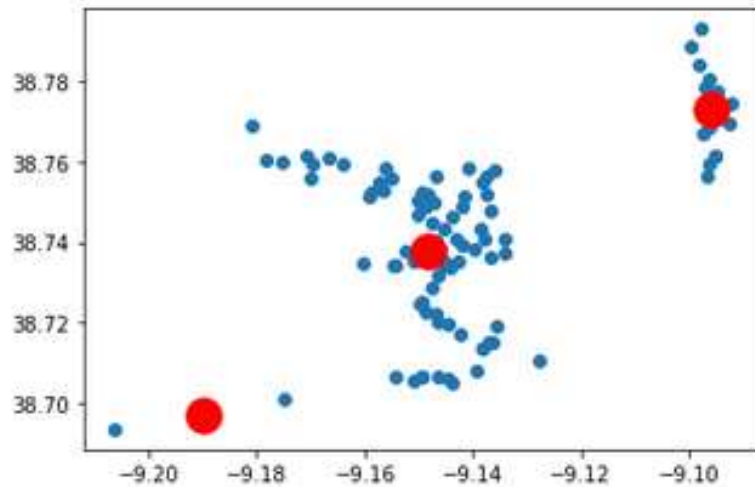


K-means Clustering

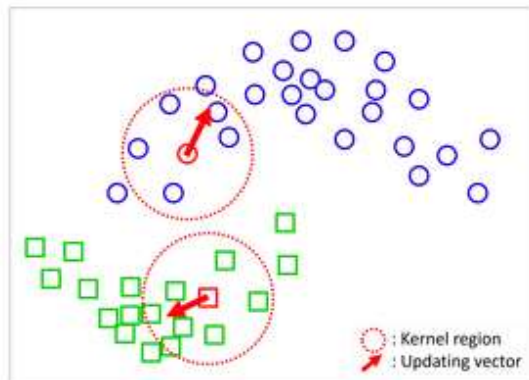


K-Means Clustering

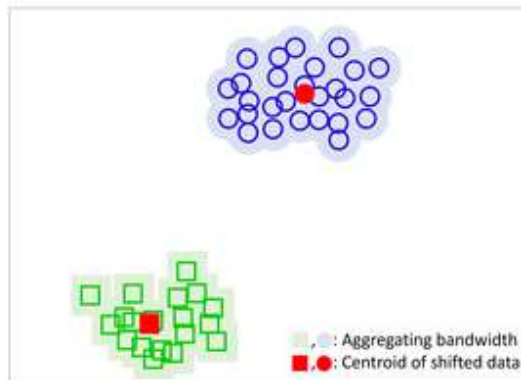
```
from sklearn.cluster import KMeans
modell = KMeans(n_clusters=3, init='k-means++', max_iter=400, n_init=10, random_state=0)
modell.fit_predict(df1)
plt.scatter(df1["long"], df1["lat"])
plt.scatter(modell.cluster_centers_[:, 0], modell.cluster_centers_[:, 1], s=300, c='red')
plt.show()
```



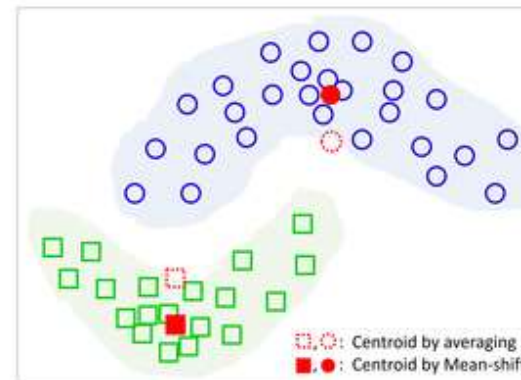
Means Shift Clustering



Updates (shifts) all data point toward high density region until all the points converge

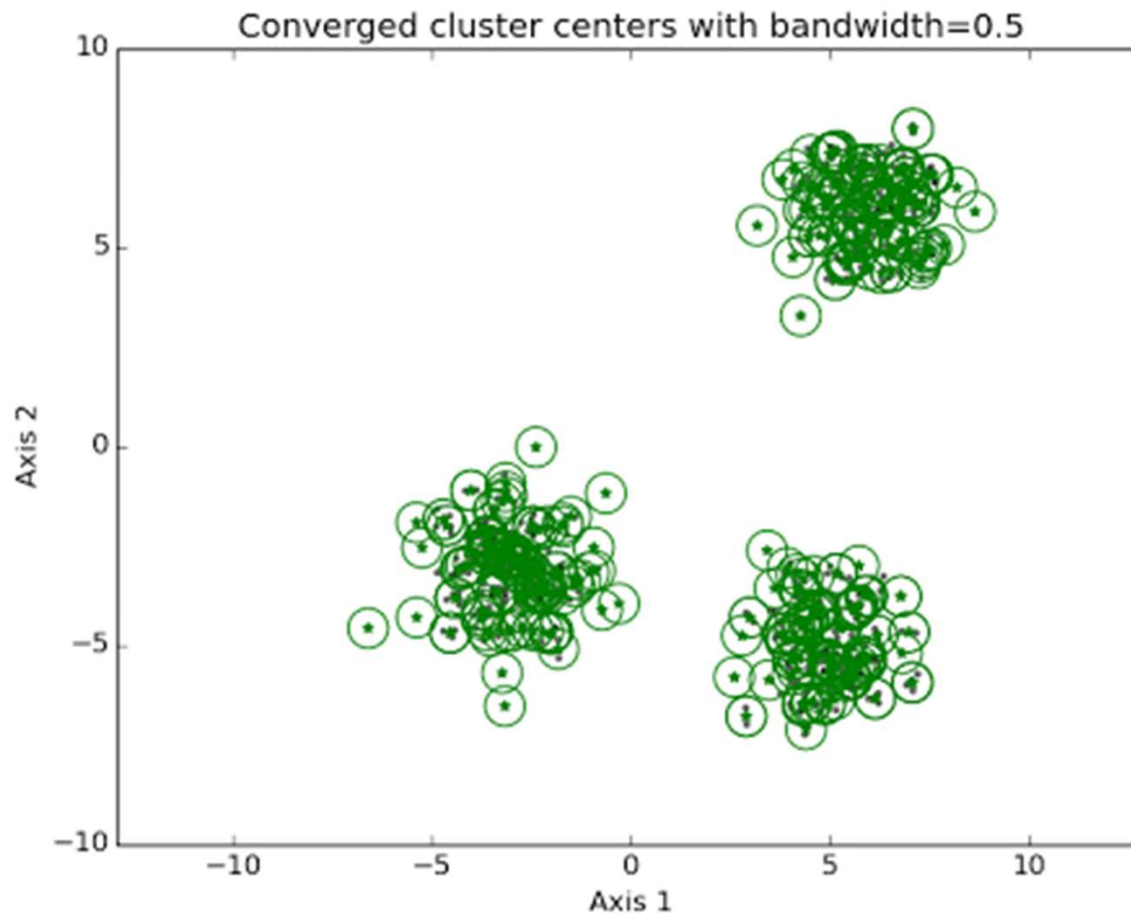


Aggregate the nearby shifted data points into a cluster whose centroid is their average



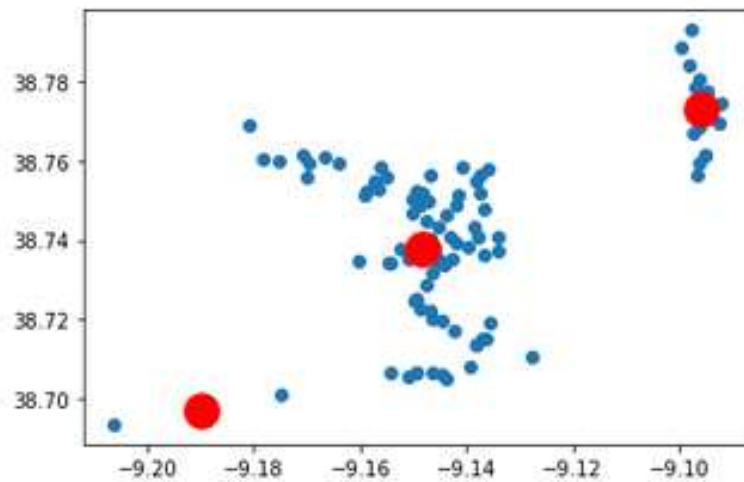
Assign the original data into the according clusters, But keep the centroid calculated with shifted data

Means Shift Clustering



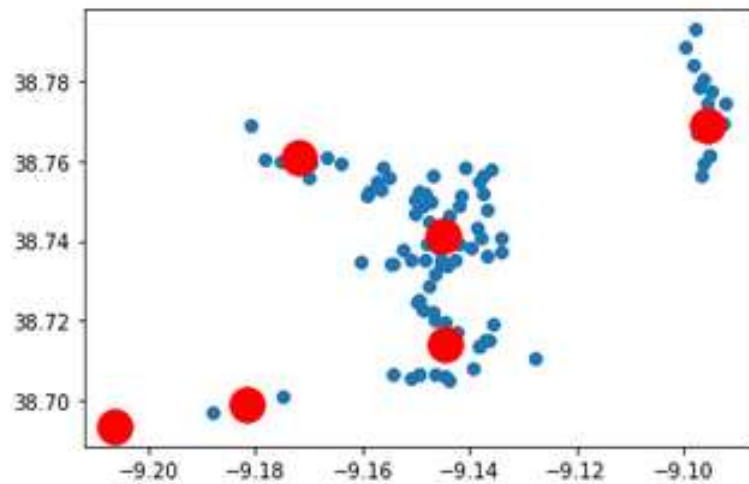
Means Shift Clustering

```
from sklearn.cluster import MeanShift
modell = MeanShift(bandwidth=1)
modell.fit_predict(df1)
plt.scatter(df1["long"], df1["lat"])
plt.scatter(modell.cluster_centers[:, 0], modell.cluster_centers[:, 1], s=300, c='red')
plt.show()
```



Means Shift Clustering

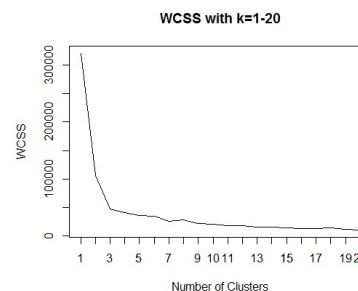
```
from sklearn.cluster import MeanShift
modell = MeanShift(bandwidth=0.02)
modell.fit_predict(df1)
plt.scatter(df1["long"], df1["lat"])
plt.scatter(modell.cluster_centers_[ :, 0], modell.cluster_centers_[ :, 1], s=300, c='red')
plt.show()
```



WCSS

- Within-Cluster-Sum-of-Squares (WCSS) - Implicit **objective function in k-Means** measures sum of distances of observations from their cluster centroids.

$$WCSS = \sum_{i \in n} (X_i - Y_i)^2$$

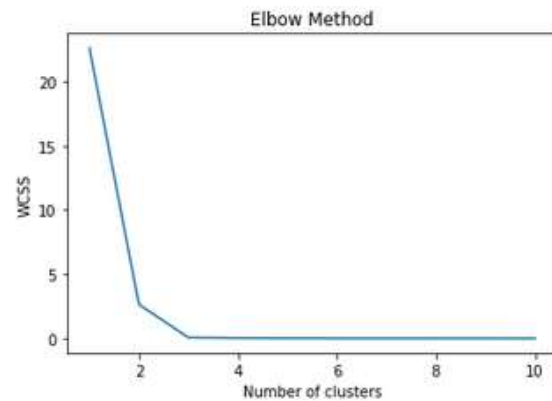


Y_i is centroid for observation X_i .

- Given that k-Means has no in-built preference for right number of clusters, following are some of the common ways k can be selected:
 - Domain Knowledge
 - Rule of Thumb
 - Elbow-Method using WCSS
 - Cluster Quality using Silhouette Coefficient

WCSS

```
wcss = []  
for i in range(1, 11):  
    model =KMeans(n_clusters=i, random_state=1)  
    model.fit(df1)  
    wcss.append(model.inertia_)  
plt.plot(range(1, 11), wcss)  
plt.title('Elbow Method')  
plt.xlabel('Number of clusters')  
plt.ylabel('WCSS')  
plt.show()
```



Silhouette Coefficient

- Is a measure of how similar an object is to its own cluster (cohesion) compared to other clusters (separation).
- The silhouette ranges from -1 to $+1$
- high value indicates that the object is well matched to its own cluster and poorly matched to neighbouring clusters.
- If most objects have a high value, then the clustering configuration is appropriate.

```
from sklearn import metrics
kmeans_model = KMeans(n_clusters=3, random_state=1).fit(df1)
labels = kmeans_model.labels_
metrics.silhouette_score(df1, labels, metric='euclidean')
```

```
0.9678966629839983
```

Summary

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- Means Shift Clustering
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References

- Peter J. Rousseeuw (1987). "Silhouettes: a Graphical Aid to the Interpretation and Validation of Cluster Analysis". *Computational and Applied Mathematics* 20: 53-65.